

Teresa Bister  
for the Pierre Auger Collaboration

ICRC 2021, Berlin / Online

PIERRE  
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OBSERVATORY

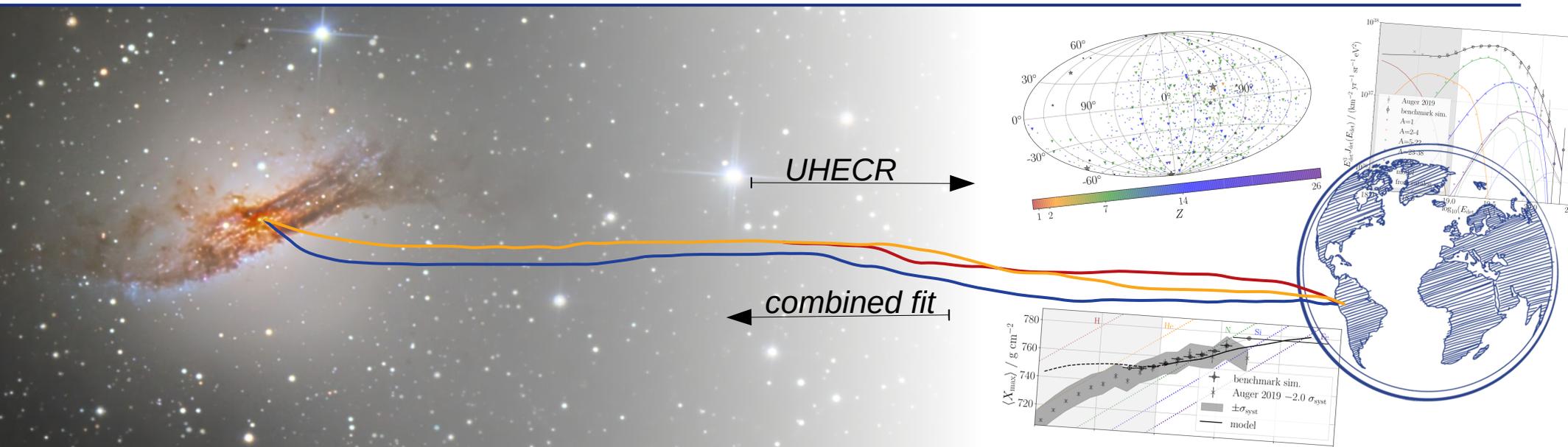


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# A combined fit of energy spectrum, shower depth distributions and arrival directions to constrain models of UHECR sources



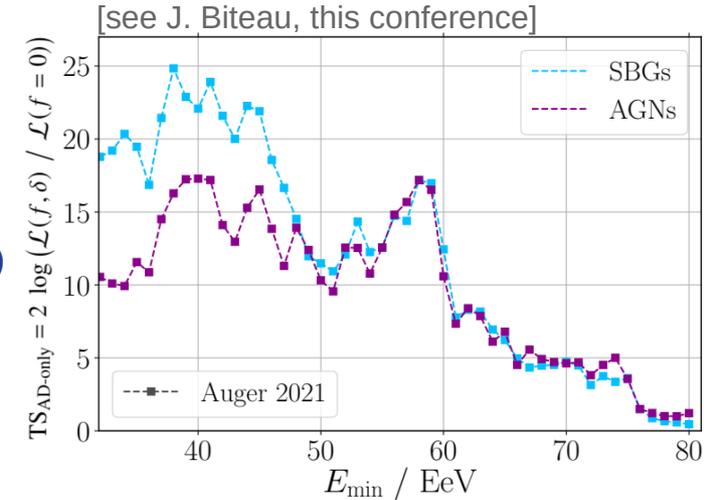
# Introduction

- UHECR flux  $\leftrightarrow$  correlation with **catalogs of starburst galaxies (SBGs) / active galactic nuclei (AGNs)**  
 $\rightarrow \sigma_{\text{SBG}} = 4.0, \sigma_{\text{AGN}} = 3.1, E \gtrsim 38 \text{ EeV}$

- **likelihood analysis:**

$$\log \mathcal{L}_{\text{AD-only}}(f, \delta) = \sum_i \log (f \cdot S_{\delta}(\vec{v}_i) + (1 - f)B(\vec{v}_i))$$

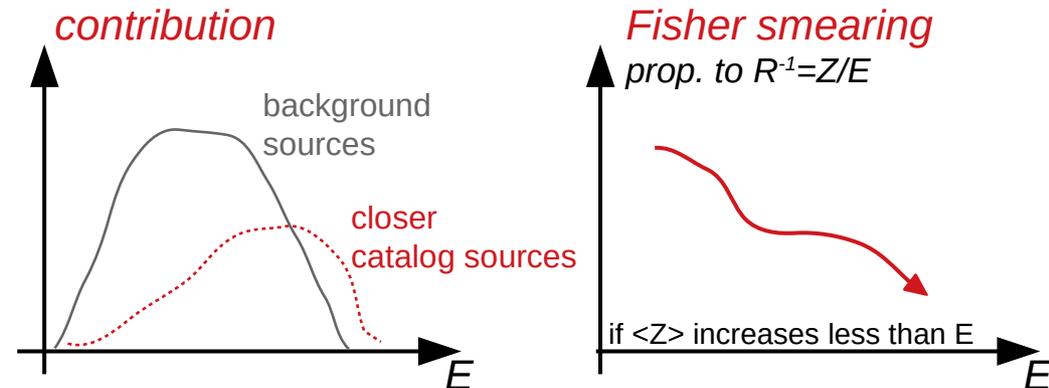
$\uparrow$  only arrival directions       $\uparrow$  signal fraction       $\uparrow$  Fisher smearing  
*catalog model*      *background model (isotropy)*



but: **only with arrival directions no clear distinction possible** (similar source directions)

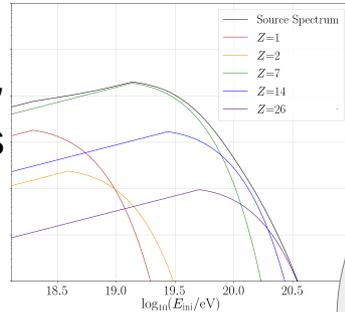
$\rightarrow$  **combined fit of energy, shower depth Xmax & arrival directions**

- include **energy spectrum & Xmax as observables**
- describe **energy dependency** of catalog contribution & Fisher smearing



# Universe model setup

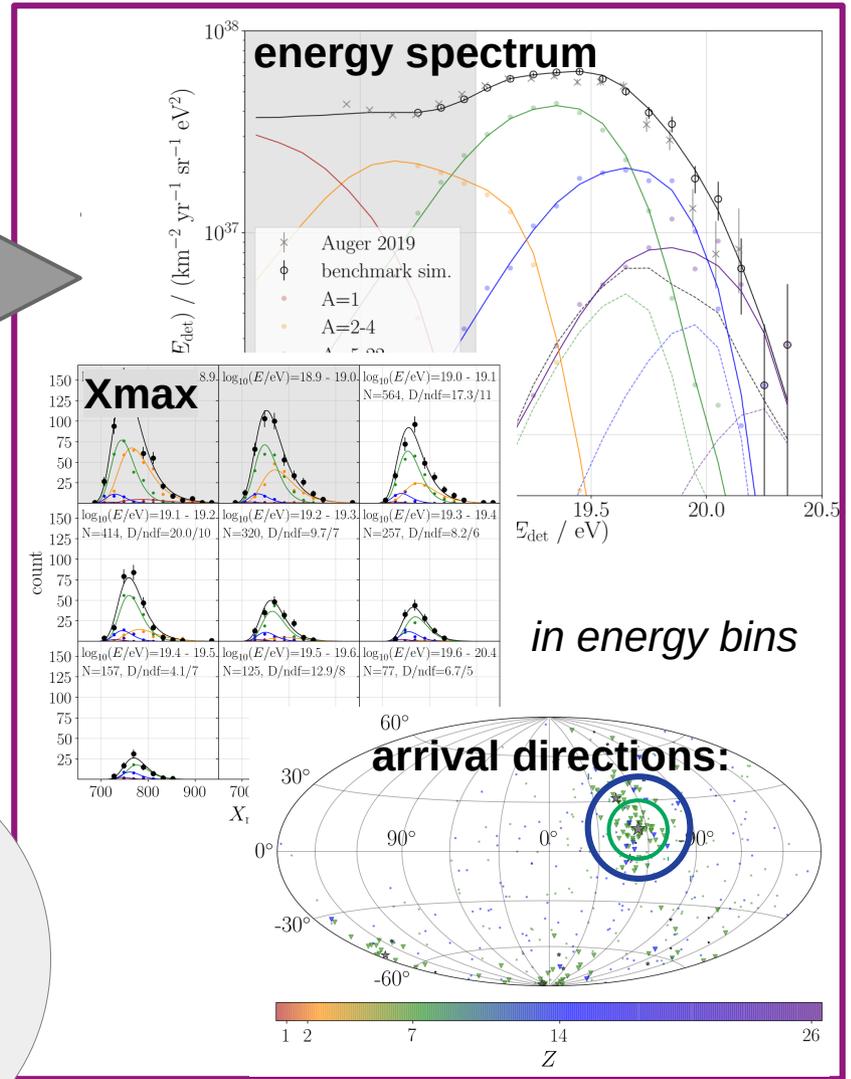
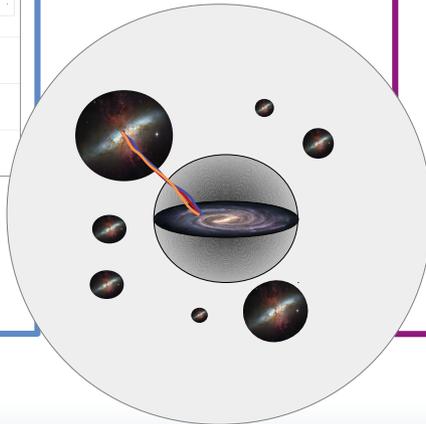
- homogeneous background
  - with source evolution  $\sim(1+z)^m$
  - isotropic arrival directions
- catalog sources: SBGs / AGNs
  - flux weight & distance considered
  - arrival directions  
~ rigidity-dependent Fisher
- injection: power law + exp. cutoff



add above  $10^{18.7}$  eV:  
 $f_0$  \* catalog+  $(1-f_0)$  \* background



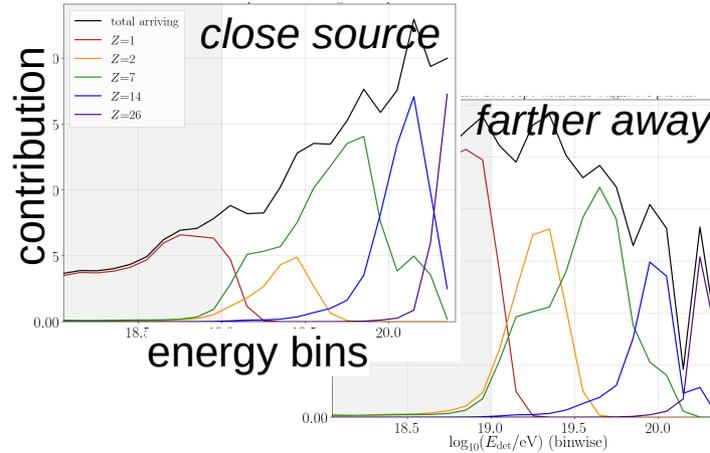
1d CRPropa3  
simulations  
+  
reweighting



# From injection to energy-dependent arrival directions

- calculate **source contribution for each energy bin e**

depending on: flux weight, exposure, distance injection + propagation  
(1d CRPropa3 simulations)



- build **pdfs for arrival distributions in energy bins e**:

$$\text{pdf}_e = \underbrace{f_S(f_0, E_{\text{det}}^e)}_{\text{signal contribution}} \cdot \underbrace{S(E_{\text{det}}^e, \delta_S(E_{\text{det}}^e))}_{\text{Fisher smearing}} + (1 - f_S(f_0, E_{\text{det}}^e)) \cdot \underbrace{B}_{\text{source distribution}}$$

signal contribution:  
depends on propagation,  
source distribution

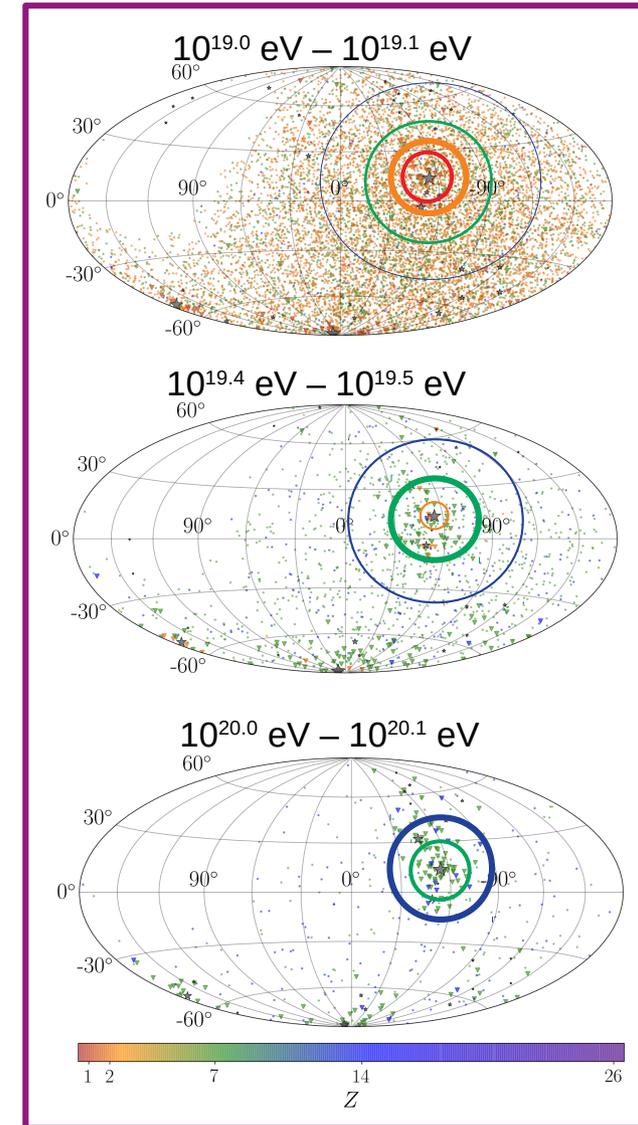
Fisher smearing for each source  
& each arriving element with:

$$\delta_S = \delta_0 Z_{\text{det}} \frac{10 \text{ EeV}}{E_{\text{det}}}$$

- one fully energy-dependent universe model:**

- E, Xmax, ADs: information about source distribution
- E-dependency of smearing & signal fraction: 2 fit parameters  $\delta_0, f_0$

→ increased sensitivity to distinguish source models

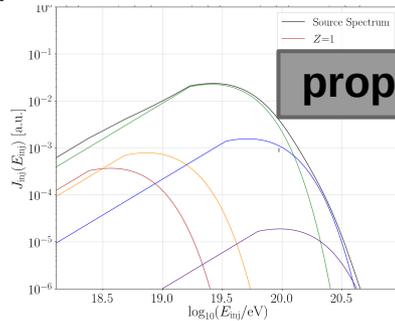


# Fit method overview

Universe model setup:

injected spectrum:

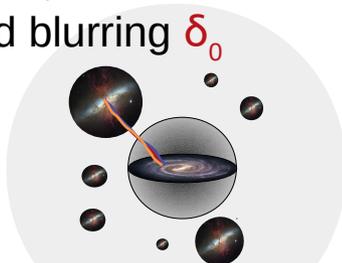
$\gamma, R_{cut}, a_i$



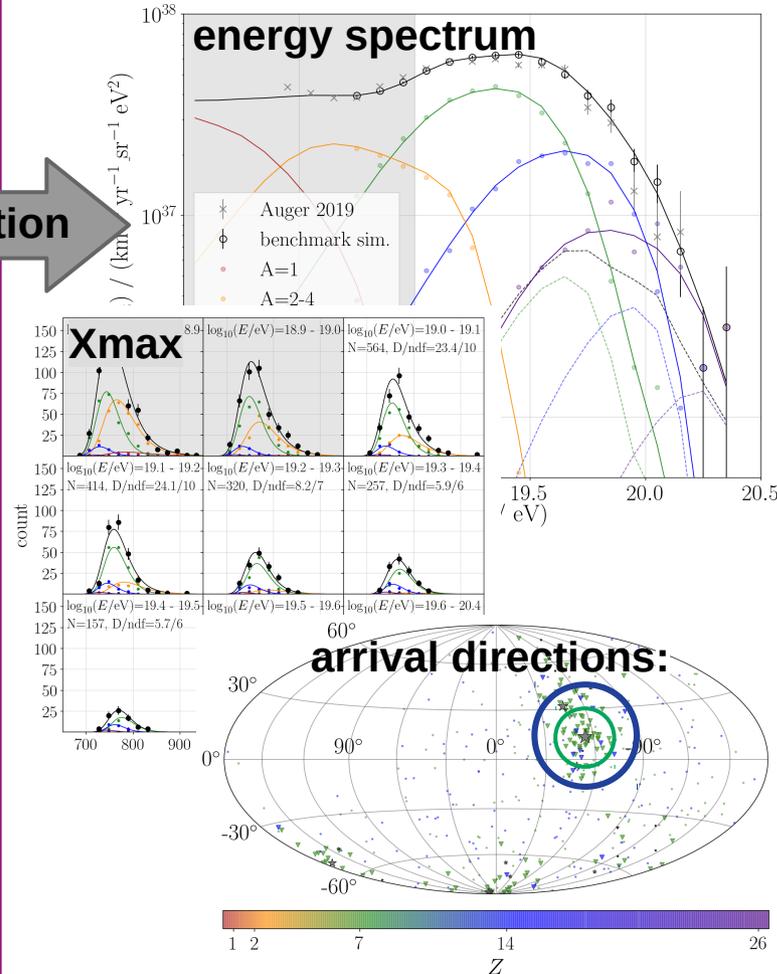
3d setup:

signal fraction  $f_0$ ,

magnetic field blurring  $\delta_0$



Simulated observables:



compare to data  
via Likelihood:

spectrum: Poissonian

$$\mathcal{L}_E = \prod_e \frac{(p^e)^{k^e}}{k^e!} \exp(-p^e)$$

Xmax: Multinomial

$$\mathcal{L}_{X_{\max}} = \prod_{\tilde{e}} k^{\tilde{e}}! \prod_x \frac{(G^{\tilde{e},x})^{k^{\tilde{e},x}}}{k^{\tilde{e},x}!}$$

arrival directions:  
compare to modeled  
arrival pdf

$$\mathcal{L}_{AD} = \prod_e \prod_{i \in e} \text{pdf}_e(\vec{v}_i)$$

from:

Auger Combined Fit  
Auger ADs comparison to astrophysical catalogs

adjust parameters

$\gamma, R_{cut}, a_i, f_0, \delta_0$

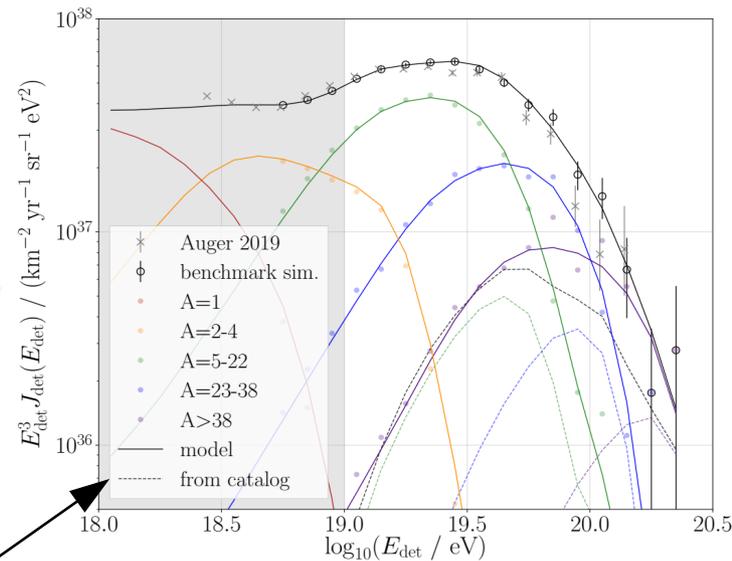
# Benchmark simulation: starburst galaxies + background

- from fit of  $E + X_{\max}$  on Auger data (*backup*)  
with source evolution = star formation rate ( $m=3.4$ )

$\gamma$	$\log_{10}(R_{\text{cut}}/V)$	$a_{\text{H}}$	$a_{\text{He}}$	$a_{\text{N}}$	$a_{\text{Si}}$	$a_{\text{Fe}}$	$v_{X_{\max}}/\sigma$	$v_E/\sigma$
-0.65	18.29	23%	2%	70%	4.0%	0.15%	-2.0	0.0

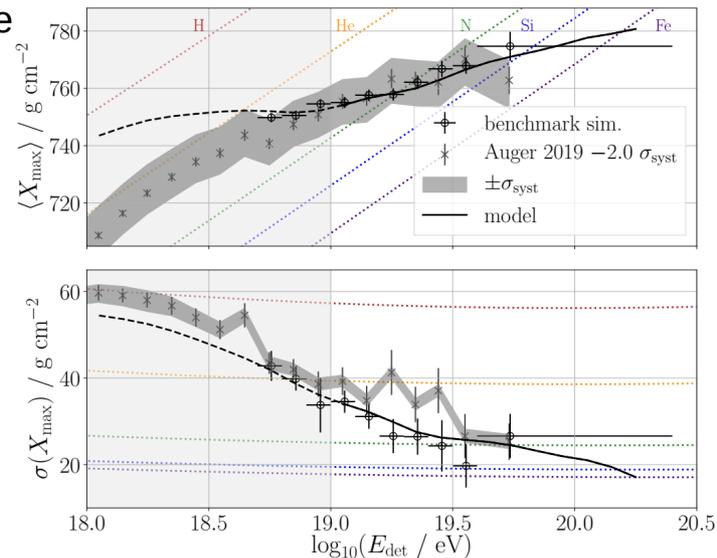
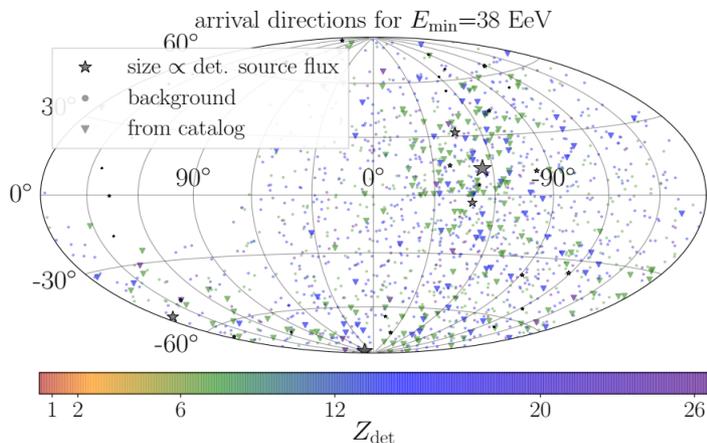
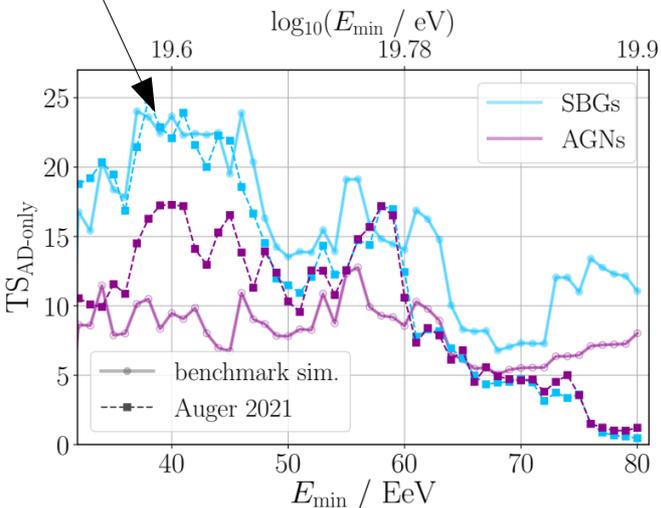
← systematic scale shift

- add  $f_0 = 1.2\%$  signal fraction from **SBG catalog** (def.  $> 10^{18.7}$  eV = 5 EeV)
- magnetic blurring  $\delta_0 = 14.3^\circ$  (for  $R = 10$  EV)
- spectrum, composition, arrival directions,  $N_{\text{CRs}}$   
 $\approx$  Auger measurements



catalog contribution  $f_s(f_0, E_{\text{det}}^j)$   
grows with energy: SBGs close

simulated ADs  $\approx$  measured ones

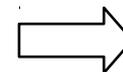


# Fit with reference models

reminder:  
benchmark sim. contains  
SBG catalog as input,  $m=3.4$

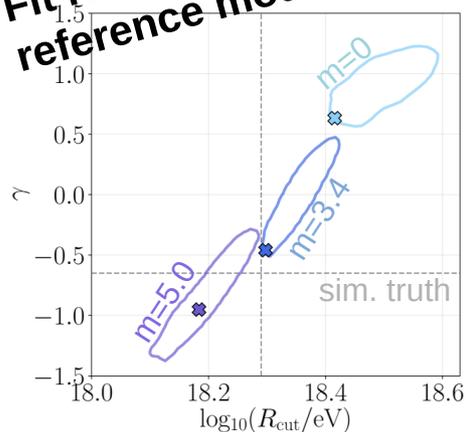
Fit different models to simulation:

- **SBG model,  $m=3.4$**  (= simulated truth)
- **AGN model,  $m=3.4$  /  $m=5.0$**
- **reference model (with  $f_0=0$ ),  $m=0.0$  /  $m=3.4$  /  $m=5.0$**

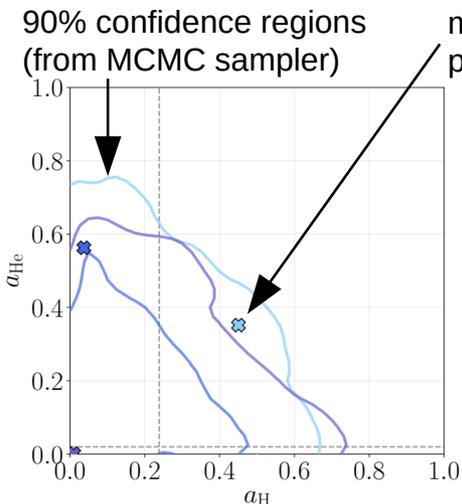


fit goal: identify  
best model = sim. truth

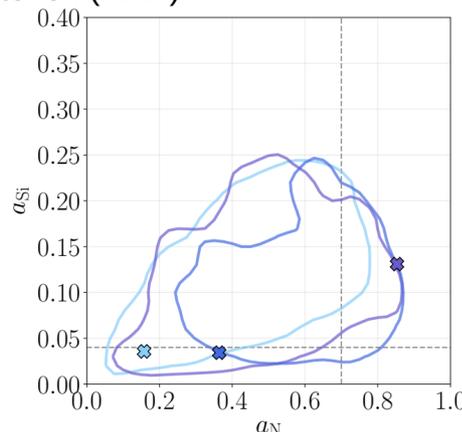
Fit results using  
reference models:



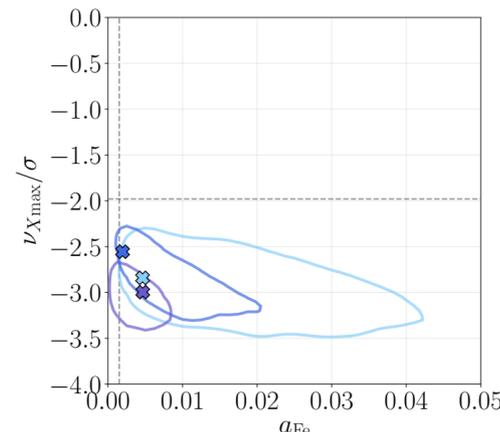
source evolution-  
dependent correlation



light fractions below cutoff,  
not reconstructable



heavier fractions  
can be determined



Xmax scale shift  
correlated with composition

	$D_E$	$D_{X_{\max}}$	$D_{\text{total}}$
$m = 0$	6.0	82.1	88.1
$m = 3.4$	5.8	81.5	87.3
$m = 5.0$	12.9	84.0	96.9

- reference model with *true*  $m=3.4$ : lowest deviance
- spectrum & Xmax well described  
even with only background sources

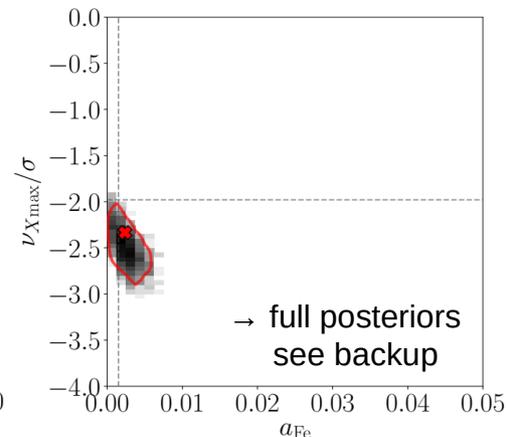
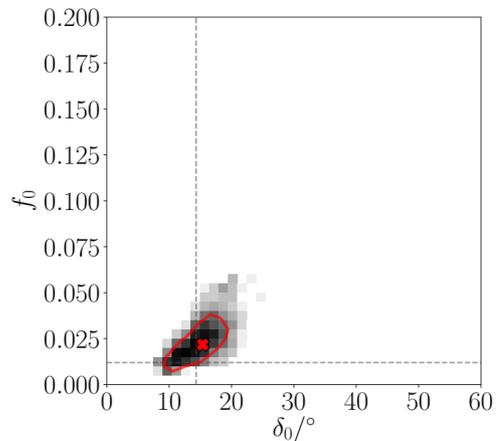
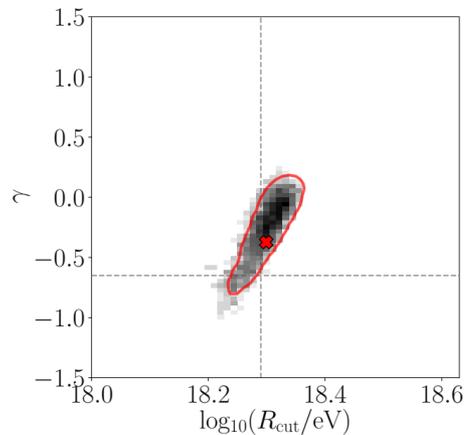
# Fit with catalog models

reminder:  
benchmark sim. contains  
SBG catalog as input,  $m=3.4$

## SBG model ( $m=3.4$ )

= simulated truth

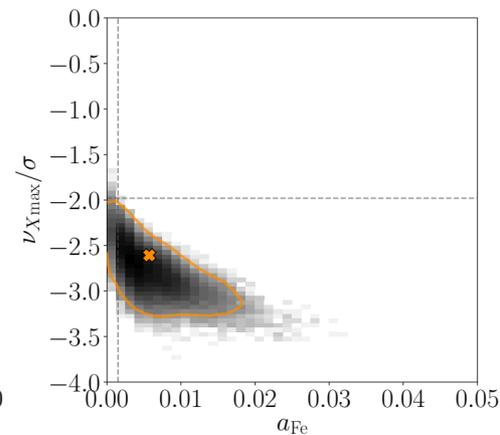
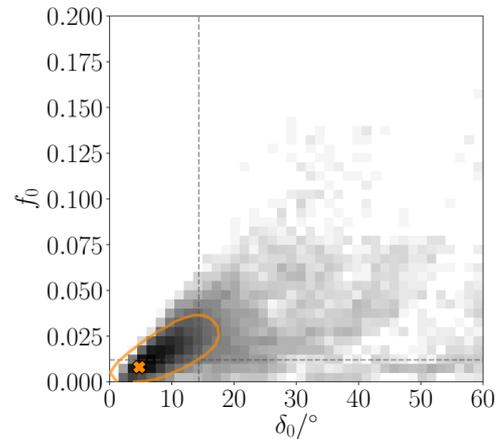
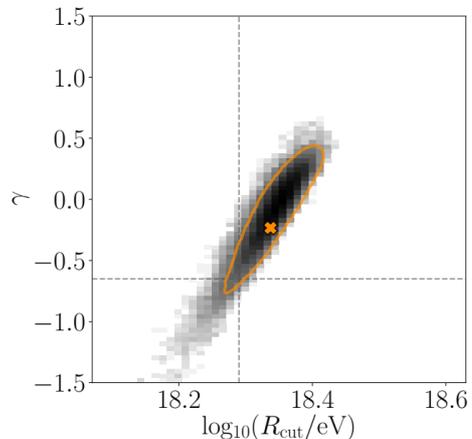
- parameters can be reconstructed well
- correlations visible ( $\gamma \leftrightarrow R_{\text{cut}}$ ), ( $f_0 \leftrightarrow \delta_0$ )



as in: [Auger Combined Fit](#), [Auger ADs comparison to astrophysical catalogs](#)

## AGN model ( $m=3.4$ )

- larger uncertainties
- true simulated values still within uncertainties even for false AGN model
- best-fit (MAP) further away from truth



# Fit with catalog models

reminder:  
benchmark sim. contains  
SBG catalog as input,  $m=3.4$

spectrum and composition  
can be described by both models

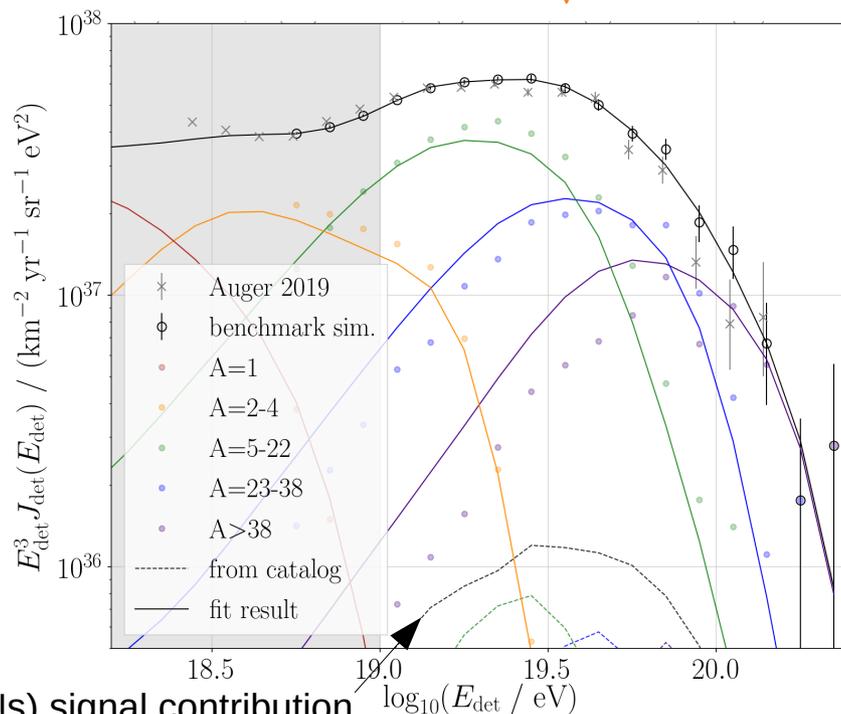
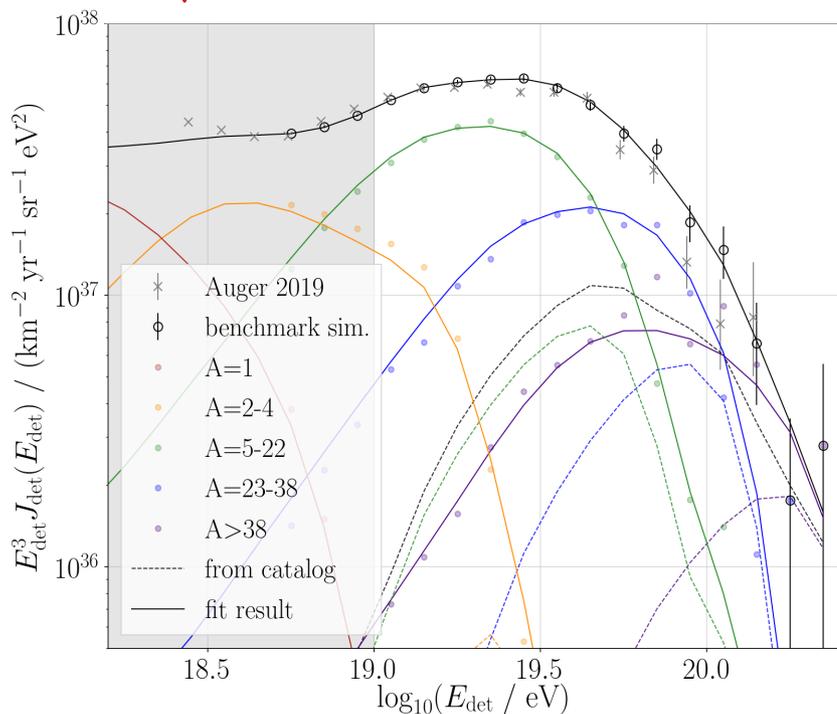
energy-dependent arrival directions not  
described by *false* AGN model (directions, distances ↴)

$D_E$	$D_{X_{\max}}$	$D_{\text{total}}$	$2 \log \frac{\mathcal{L}_{\text{AD}}}{\mathcal{L}_{\text{AD}}^{\text{ref}, m=3.4}}$	$2 \log \frac{\mathcal{L}_{\text{sum}}}{\mathcal{L}_{\text{sum}}^{\text{ref}, m=3.4}}$
5.5	80.2	85.7	30.6	32.4
6.0	81.8	87.8	11.2	10.8
5.6	84.1	89.9	1.4	-1.0

SBG model

- SBG model ( $m = 3.4$ ) → *sim. truth*
- AGN model ( $m = 3.4$ )
- AGN model ( $m = 5.0$ )

AGN model



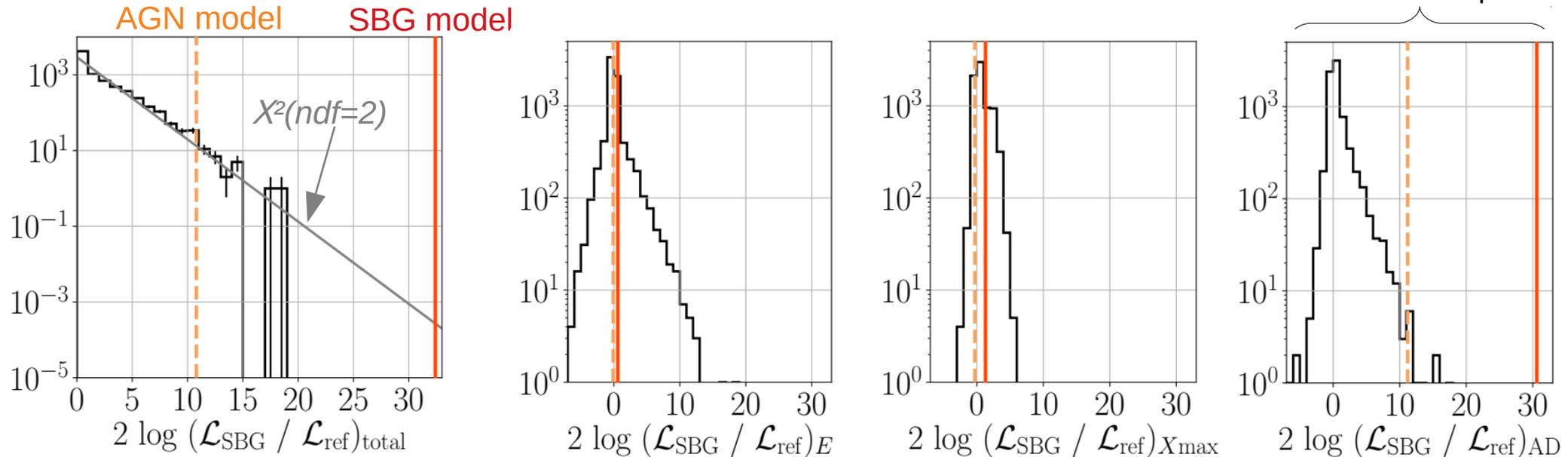
model (AGNs) signal contribution  
energy dependency different from simulated input (SBGs)

# Estimation of the significance

- apply analysis on **isotropic simulations** ( $m=3.4$ , benchmark simulation parameters)
- isotropy tail follows  $X^2$  distribution with  $ndf=2$  (SBG model has 2 more fit parameters:  $f_o, \delta_o$ )

→  $p_{\text{SBG}} \simeq 9 \cdot 10^{-8}$      $p_{\text{AGN}} \simeq 5 \cdot 10^{-3}$     → **analysis can identify true simulated SBG model**

- **more sensitive** than AD-only analysis on same simulation:  $p_{\text{SBG}}^{\text{AD-only, pre-trial}} \simeq 6.1 \cdot 10^{-6}$      $p_{\text{AGN}}^{\text{AD-only, pre-trial}} \simeq 1.7 \cdot 10^{-3}$
- **no need for energy threshold scan** → **no penalization**



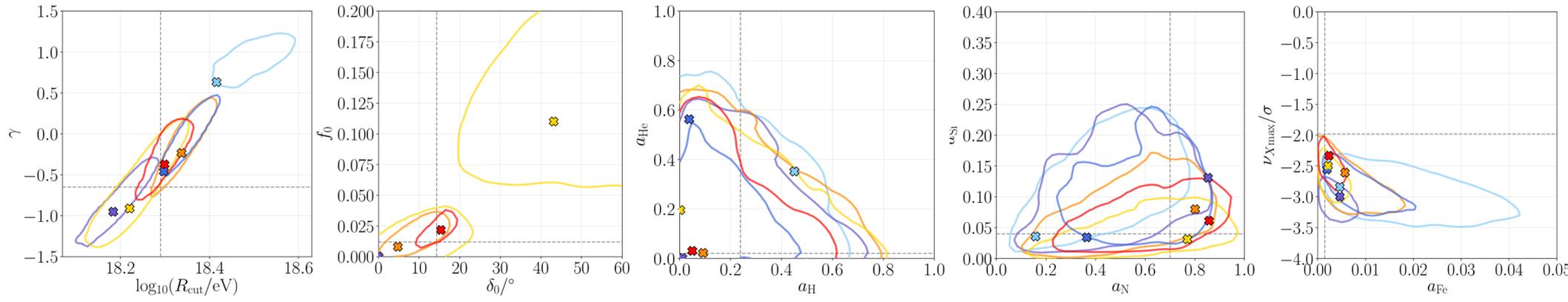
# Conclusions

- presented **combined fit including energy spectrum, Xmax distributions & energy-dependent arrival directions**
- on benchmark simulation (resembles Auger data):
  - source parameters can be reconstructed including uncertainties
  - additionally determine **energy-dependent signal contribution and magnetic field smearing**
  - enhanced sensitivity** compared to arrival directions-only analysis
  - simulated input catalog & source evolution can be identified

$p_{\text{SBG}} \approx 9 \cdot 10^{-8}$

$p_{\text{AGN}} \approx 5 \cdot 10^{-3}$

	$D_E$	$D_{X_{\text{max}}}$	$D_{\text{total}}$	$2 \log \frac{\mathcal{L}_{\text{AD}}}{\mathcal{L}_{\text{AD}}^{\text{ref}, m=3.4}}$	$2 \log \frac{\mathcal{L}_{\text{sum}}}{\mathcal{L}_{\text{sum}}^{\text{ref}, m=3.4}}$
ref. model ( $f_0 = 0, m = 0$ )	6.0	82.1	88.1	0	-0.8
ref. model ( $f_0 = 0, m = 3.4$ )	5.8	81.5	87.3	0	0
ref. model ( $f_0 = 0, m = 5.0$ )	12.9	84.0	96.9	0	-9.6
SBG model ( $m = 3.4$ ) $\rightarrow$ <i>sim. truth</i>	5.5	80.2	85.7	30.6	32.4
AGN model ( $m = 3.4$ )	6.0	81.8	87.8	11.2	10.8
AGN model ( $m = 5.0$ )	5.6	84.1	89.9	1.4	-1.0



# Backup

# Signal contribution & smearing as a function of energy

pdfs are constructed via

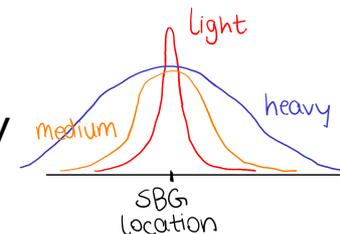
$$\text{pdf}_e = f_S(f_0, E_{\text{det}}^e) \cdot S(E_{\text{det}}^e, \delta_S(E_{\text{det}}^e)) + (1 - f_S(f_0, E_{\text{det}}^e)) \cdot B$$

signal contribution:  
depends on propagation,  
source distribution

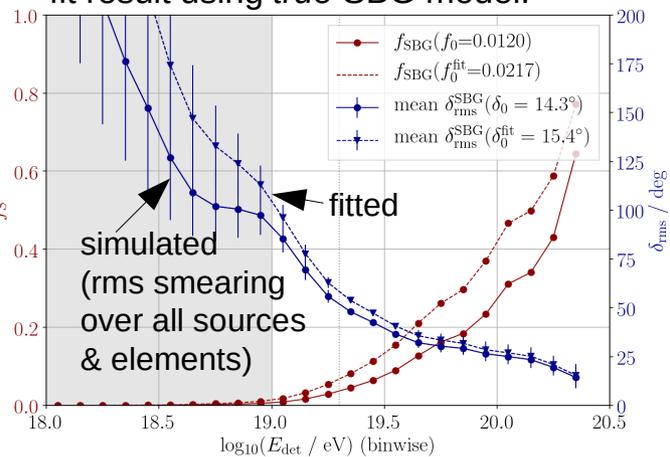
Fisher smearing for each source  
& each arriving element with:

$$\delta_S = \delta_0 Z_{\text{det}} \frac{10 \text{ EeV}}{E_{\text{det}}}$$

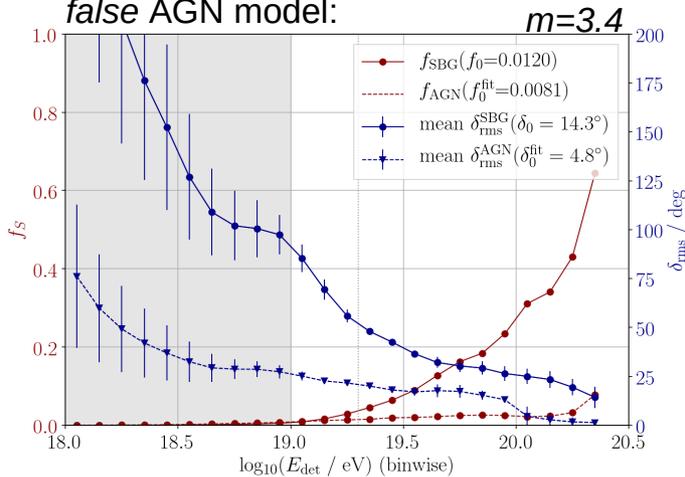
- other distances of AGNs:  
**different energy dependency of smearing & signal contribution**
- strong increase of signal contribution for SBGs not describable with AGN catalog
- need only 2 fit parameters:  
smearing of a R=10 EV particle & total signal fraction of complete data set  $E > 10^{18.7} \text{ eV}$
- even though total signal fraction  $f_0=1.2\%$  is very small, at highest energies signal contribution  $f_S(f_0)$  is large due to closeness of SBGs



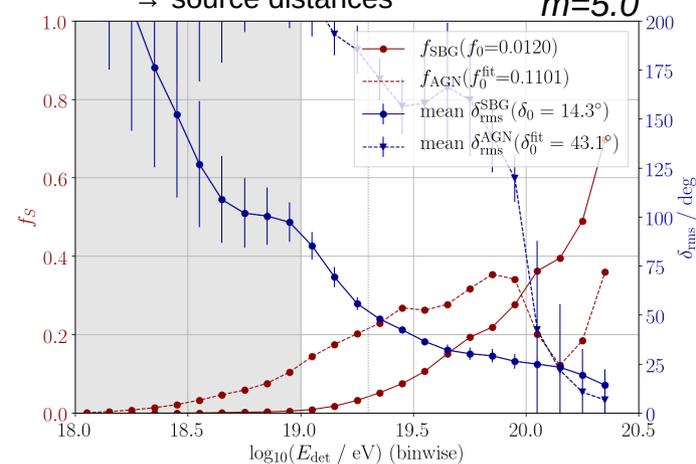
fit result using *true* SBG model:



false AGN model:

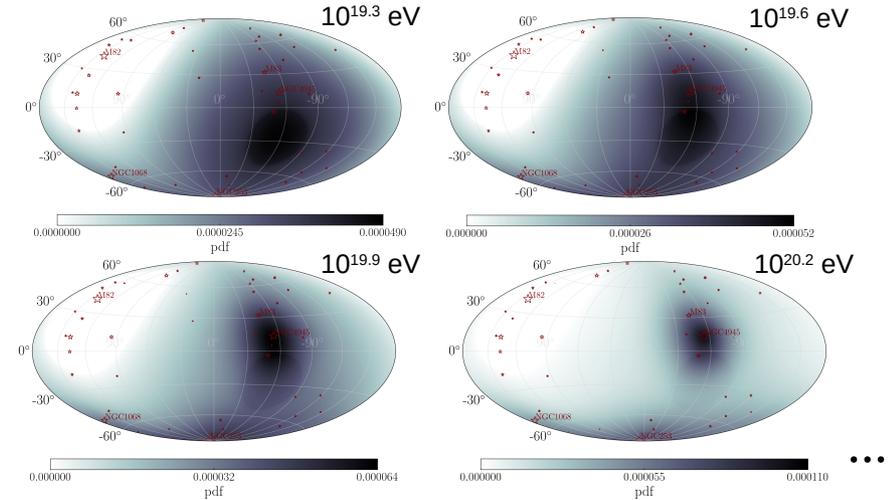
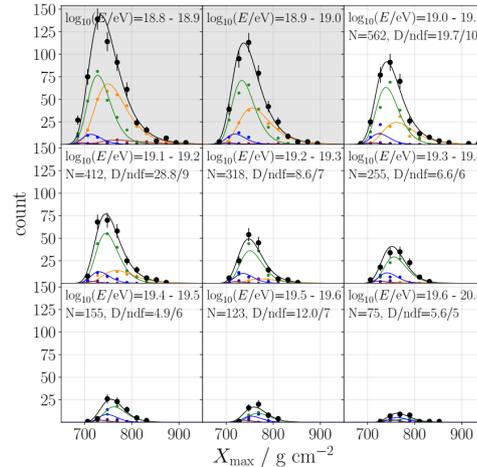
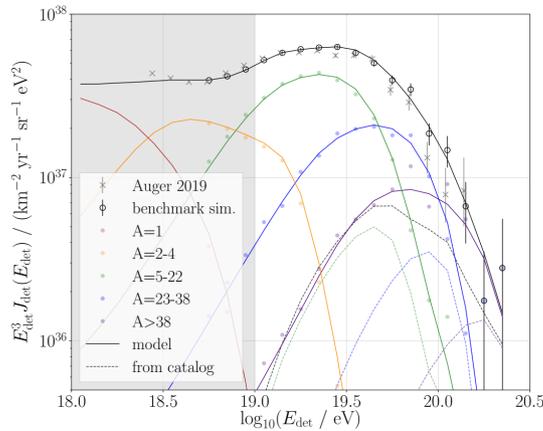


different energy dependency  
→ source distances



# Energy thresholds used in the fit

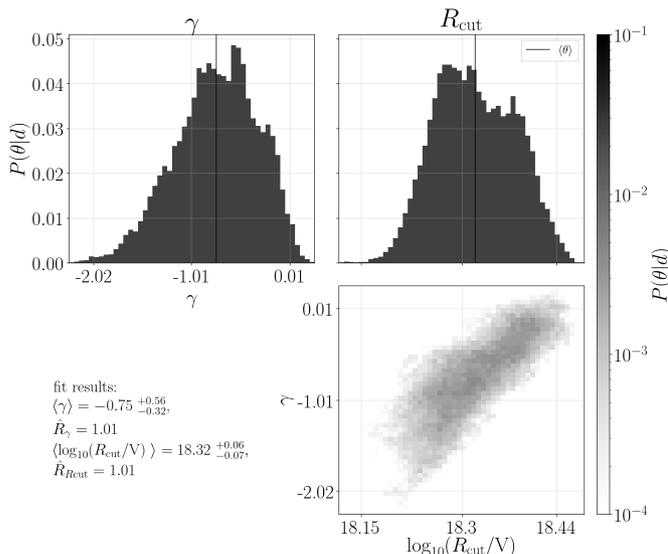
## benchmark simulation:



- **detected energy spectrum bins:**  $[10^{19.0}, 10^{19.1}, 10^{19.2} \dots 10^{20.3}, 10^{20.4}]$  eV  $\rightarrow O(20,000$  events)
- **Xmax distribution bins:**  $[10^{19.0}, 10^{19.1}, 10^{19.2} \dots 10^{19.6}, 10^{20.4}]$  eV  $\rightarrow O(2000)$  events
  - similar to Auger Paper, but threshold moved from  $10^{18.7}$  eV to  $10^{19.0}$  eV because no below-ankle CRs wanted which may come from different source class  
 $\rightarrow$  see E. Guido for the Pierre Auger Collaboration (this conference)
  - between  $10^{18.7}$  eV and  $10^{19.0}$  eV bins included in energy likelihood only if model overshoots data
- **arrival directions:**  $[10^{19.3}, 10^{19.4}, 10^{19.2} \dots 10^{20.4}]$  eV
  - dipole not modeled in arrival directions, so higher energy threshold necessary  
 $\rightarrow$  see R. Menezes for the Pierre Auger Collaboration (this conference)

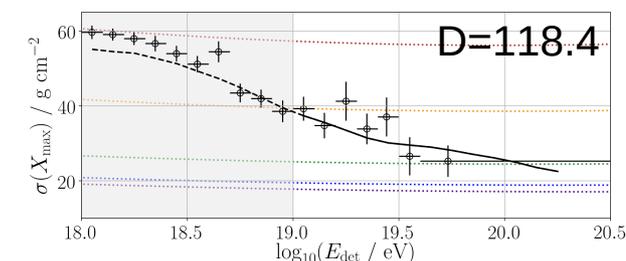
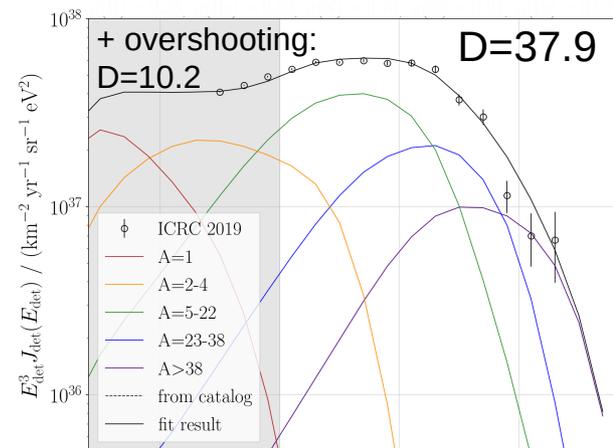
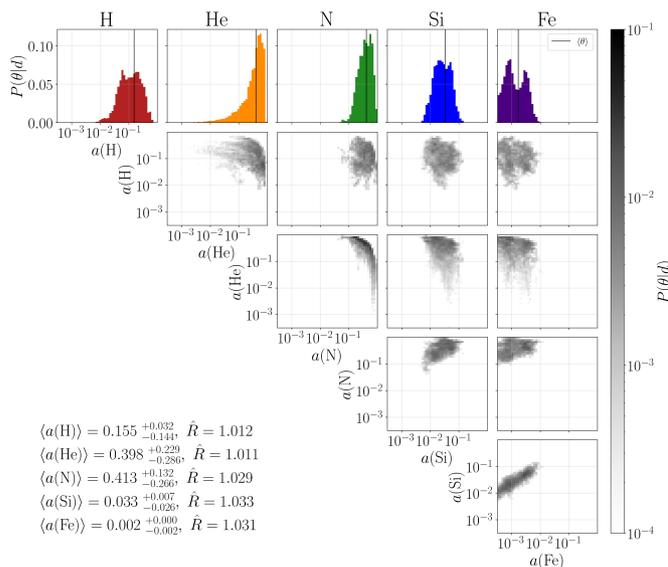
# Fit of the Auger ICRC 2019 data set > 10 EeV

→ with homogeneous reference model,  $m=3.4$ ,  $X_{\max}$  & energy scale shift

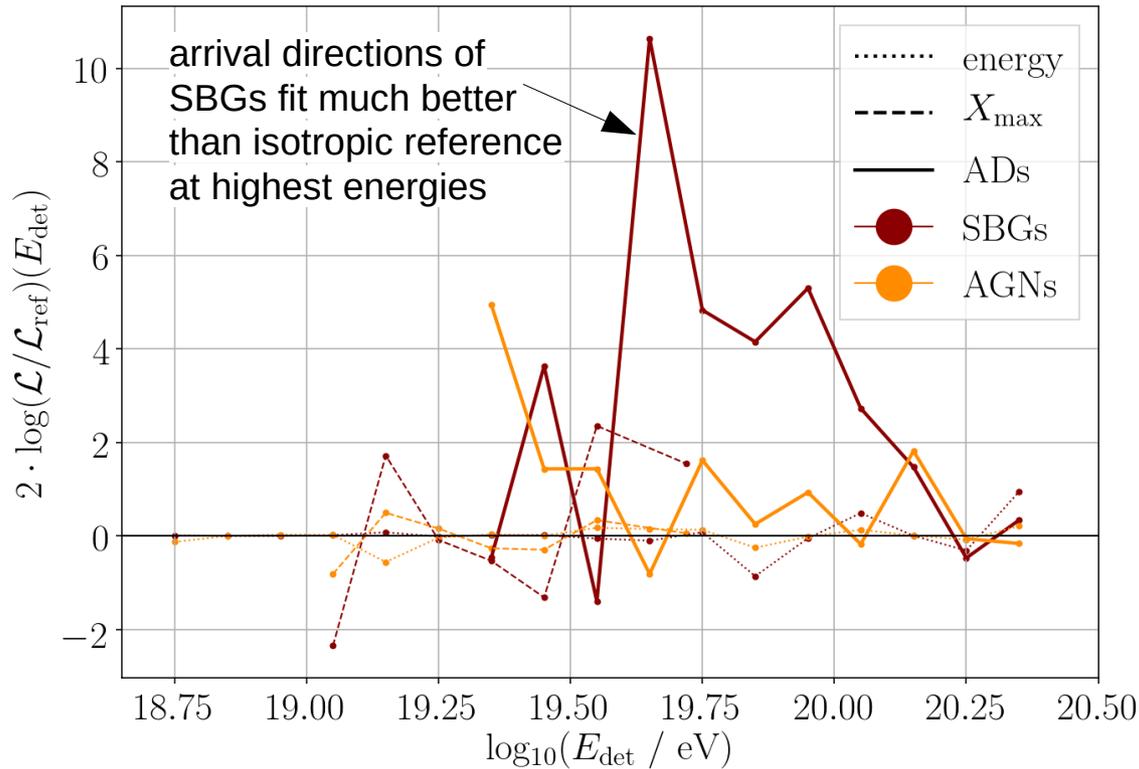


MAP:

$\gamma$	$\log_{10}(R_{\text{cut}}/V)$	$a_{\text{H}}$	$a_{\text{He}}$	$a_{\text{N}}$	$a_{\text{Si}}$	$a_{\text{Fe}}$	$\nu_{X_{\max}}/\sigma$	$\nu_E/\sigma$
-0.65	18.29	23%	2%	70%	4.0%	0.15%	-2.0	0.0



# Energy dependency of the likelihood ratio



compare SBG model & AGN model with reference model (all  $m=3.4$ )

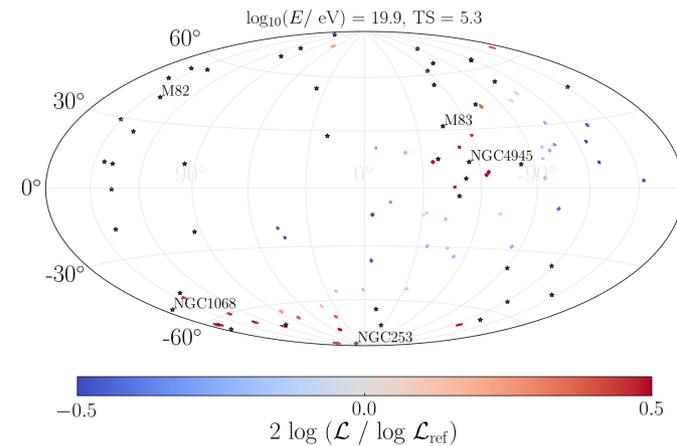
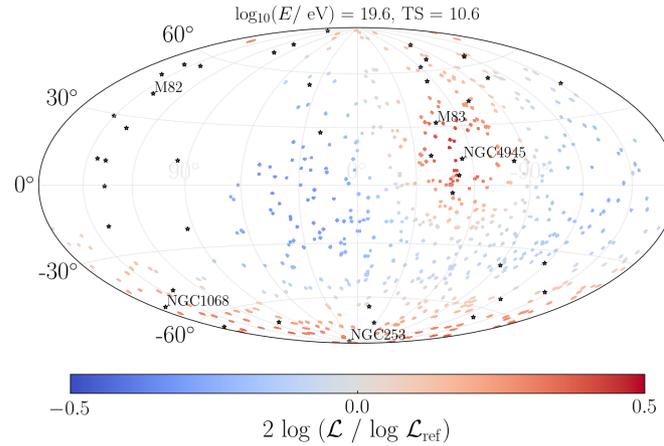
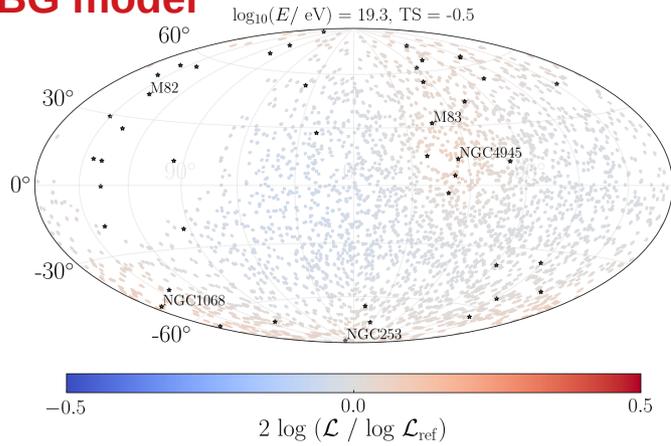
	$D_E$	$D_{X_{\max}}$	$D_{\text{total}}$	$2 \log \frac{\mathcal{L}_{\text{AD}}}{\mathcal{L}_{\text{ref}, m=3.4}^{\text{AD}}}$	$2 \log \frac{\mathcal{L}_{\text{sum}}}{\mathcal{L}_{\text{ref}, m=3.4}^{\text{sum}}}$
ref. model ( $f_0 = 0, m = 0$ )	6.0	82.1	88.1	0	-0.8
ref. model ( $f_0 = 0, m = 3.4$ )	5.8	81.5	87.3	0	0
ref. model ( $f_0 = 0, m = 5.0$ )	12.9	84.0	96.9	0	-9.6
SBG model ( $m = 3.4$ ) $\rightarrow$ <i>sim. truth</i>	5.5	80.2	85.7	30.6	32.4
AGN model ( $m = 3.4$ )	6.0	81.8	87.8	11.2	10.8
AGN model ( $m = 5.0$ )	5.6	84.1	89.9	1.4	-1.0

# Arrival directions likelihood ratio of best-fit models

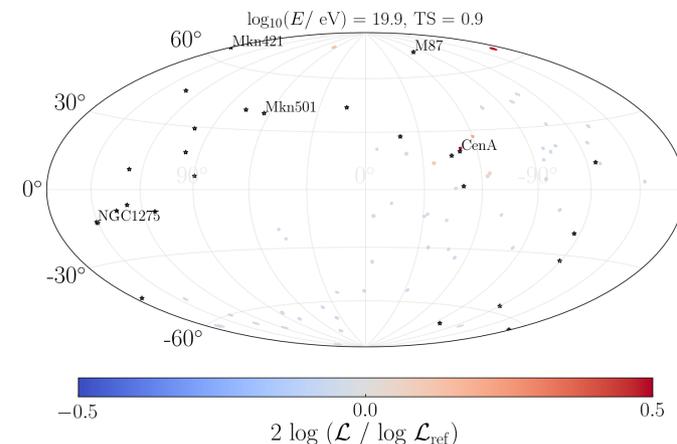
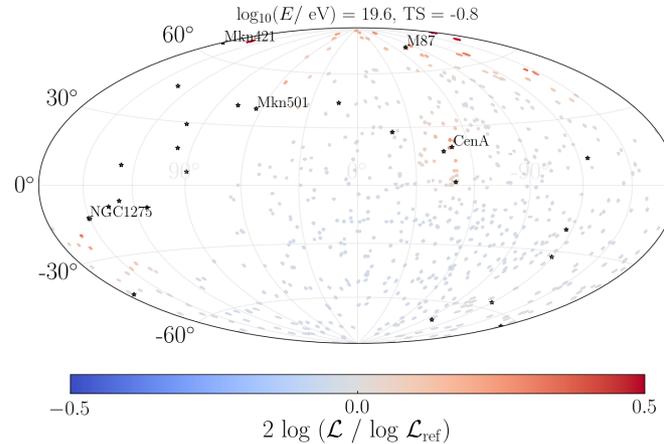
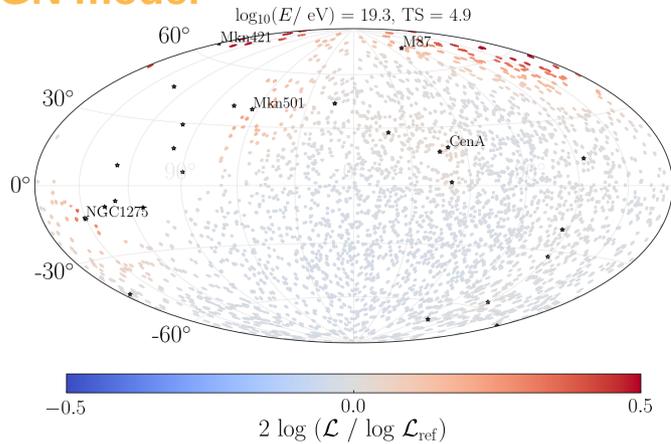
skymaps: show arrival direction pixels of benchmark simulation, colored as likelihood ratio between catalog (SBG / AGN) model and reference model (exposure).

Sum of likelihood ratio over all pixels given as TS (per energy bin), can be compared to slide 16

## SBG model



## AGN model



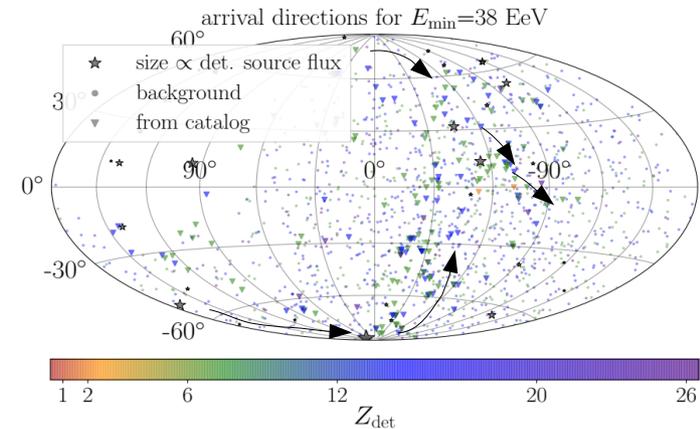
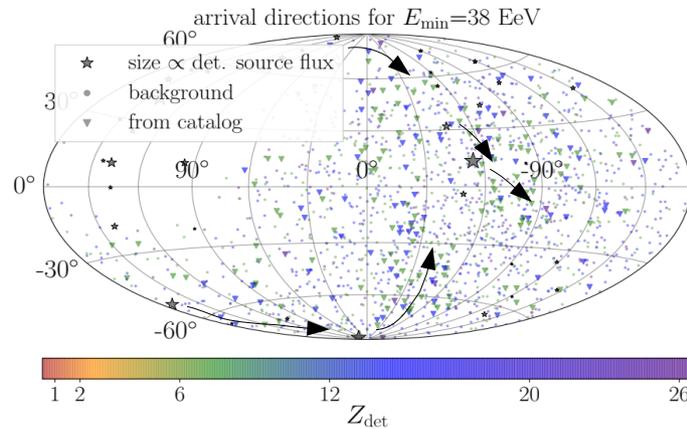
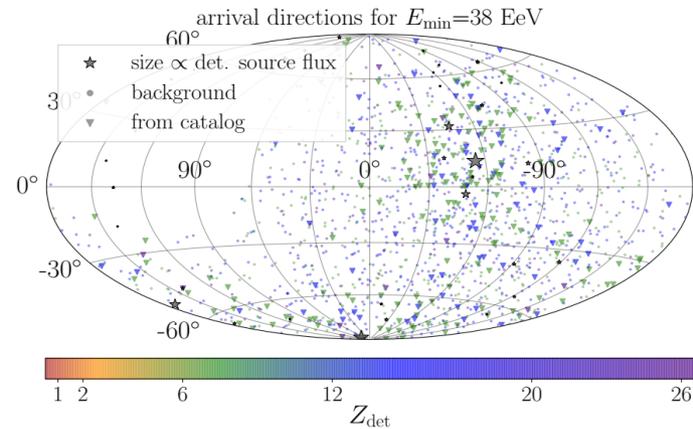
# Influence of the Galactic magnetic field on the benchmark simulation

- same source parameters etc.
- test influence of deflections by JF12 magnetic field

only turbulent smearing  
with  $\delta_0=14.3^\circ$  at R=1EV

turbulent smearing with  
 $\delta_0=14.3^\circ$  + JF12 regular

JF12 full (regular +  
turbulent + striated)

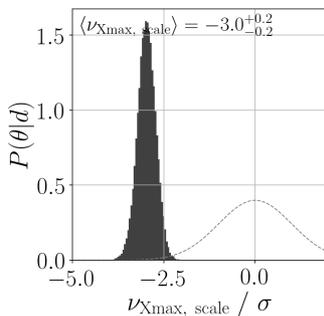
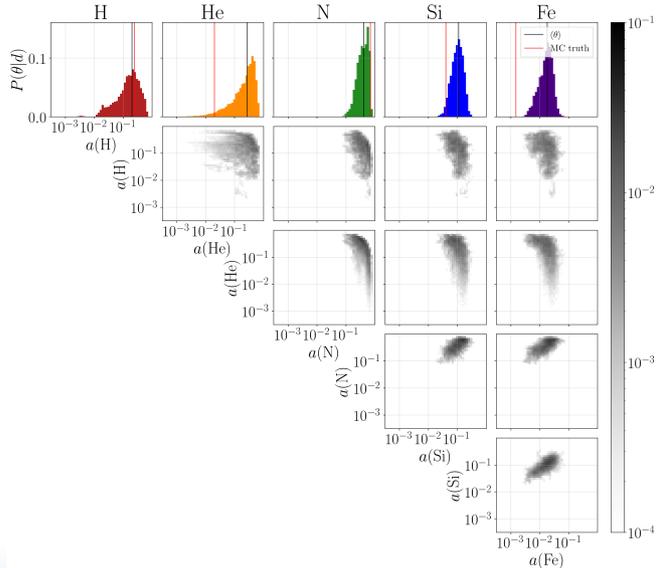
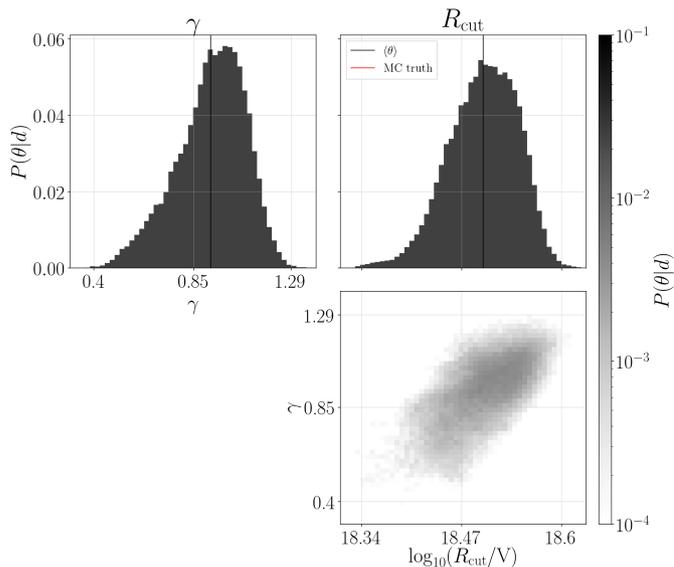


# Fit results on benchmark simulation

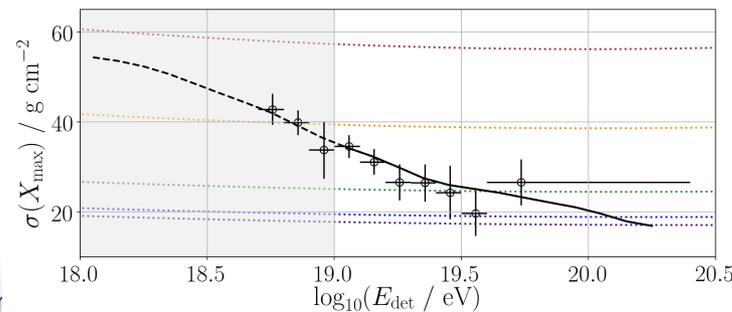
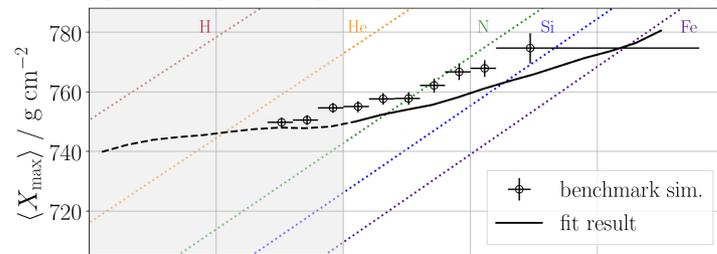
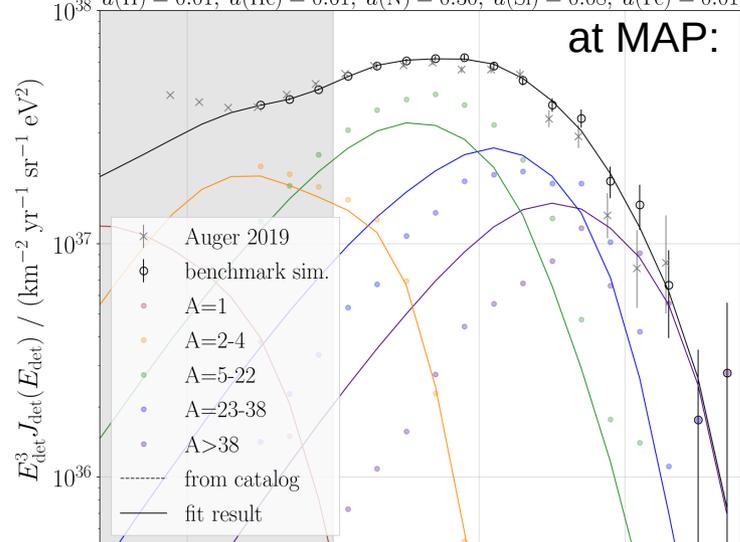
## posteriors and fitted observables

	$D_E$	$D_{X_{\max}}$	$D_{\text{total}}$	$2 \log \frac{\mathcal{L}_{\text{AD}}}{\mathcal{L}_{\text{AD}}^{\text{ref}, m=3.4}}$	$2 \log \frac{\mathcal{L}_{\text{sum}}}{\mathcal{L}_{\text{sum}}^{\text{ref}, m=3.4}}$
— ref. model ( $f_0 = 0, m = 0$ )	6.0	82.1	88.1	0	-0.8
— ref. model ( $f_0 = 0, m = 3.4$ )	5.8	81.5	87.3	0	0
— ref. model ( $f_0 = 0, m = 5.0$ )	12.9	84.0	96.9	0	-9.6
— SBG model ( $m = 3.4$ ) $\rightarrow$ <i>sim. truth</i>	5.5	80.2	85.7	30.6	32.4
— AGN model ( $m = 3.4$ )	6.0	81.8	87.8	11.2	10.8
— AGN model ( $m = 5.0$ )	5.6	84.1	89.9	1.4	-1.0

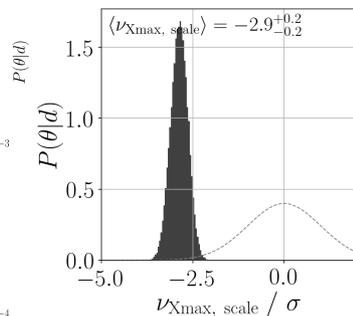
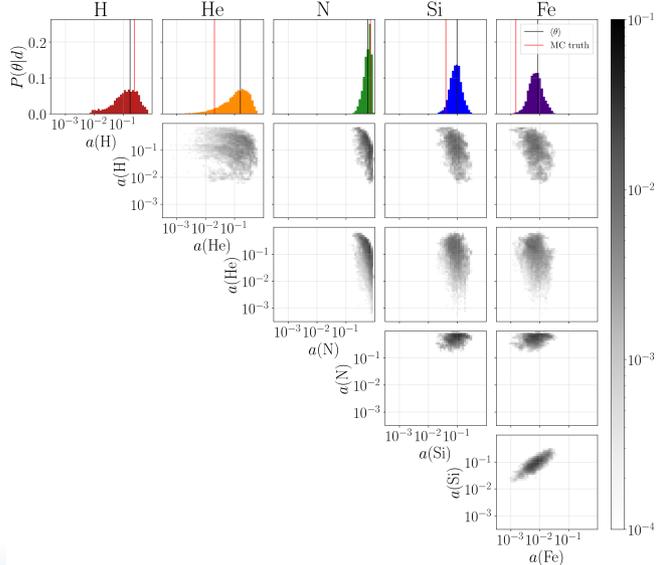
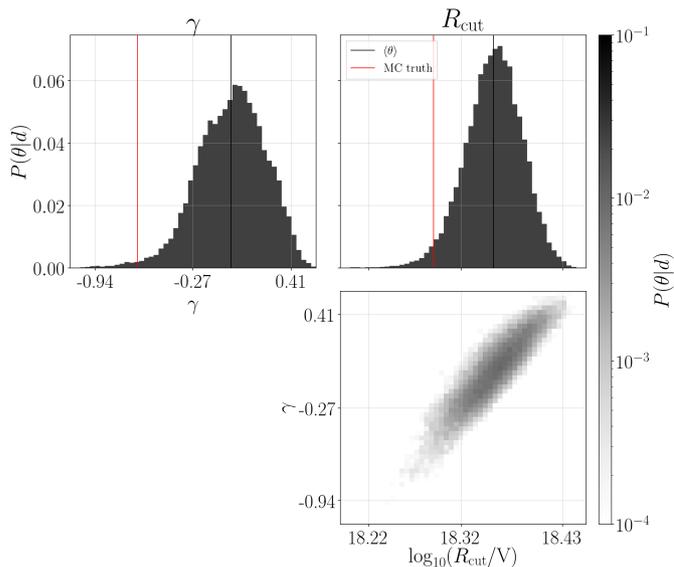
# Fit results: reference model (m=0.0)



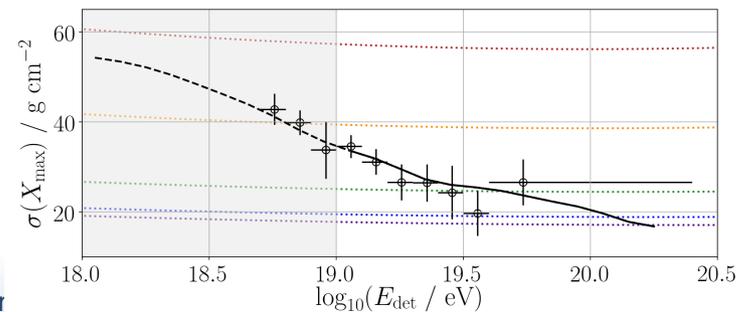
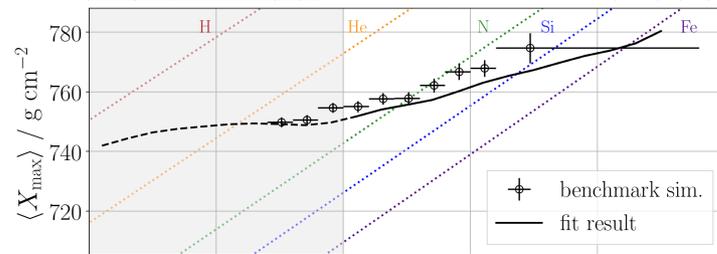
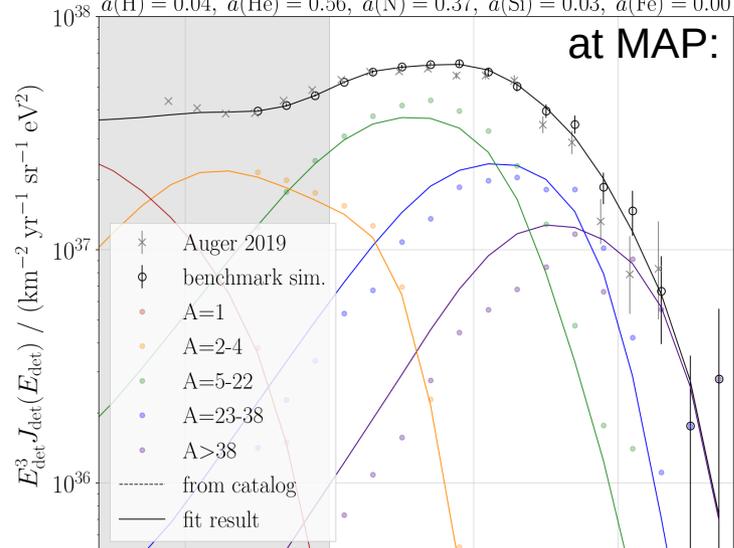
Fitted Source Parameters  
 $\gamma = 0.76$ ,  $\log_{10}(R_{\text{cut}}/V) = 18.46$ ,  $f_0 = 0.000$ ,  $\delta_0 = 0.00$ ,  $\nu_{X_{\text{max}}} = -2.82\sigma$   
 $a(\text{H}) = 0.01$ ,  $a(\text{He}) = 0.61$ ,  $a(\text{N}) = 0.30$ ,  $a(\text{Si}) = 0.08$ ,  $a(\text{Fe}) = 0.01$



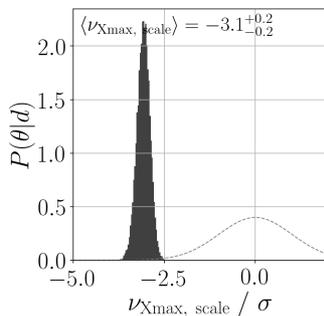
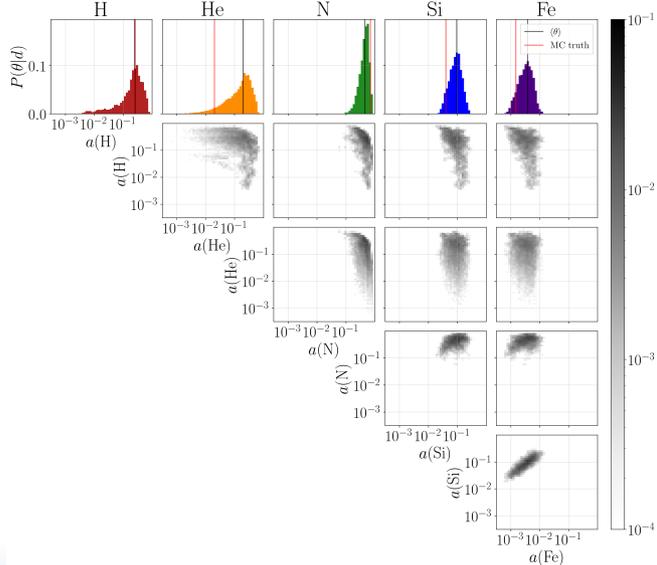
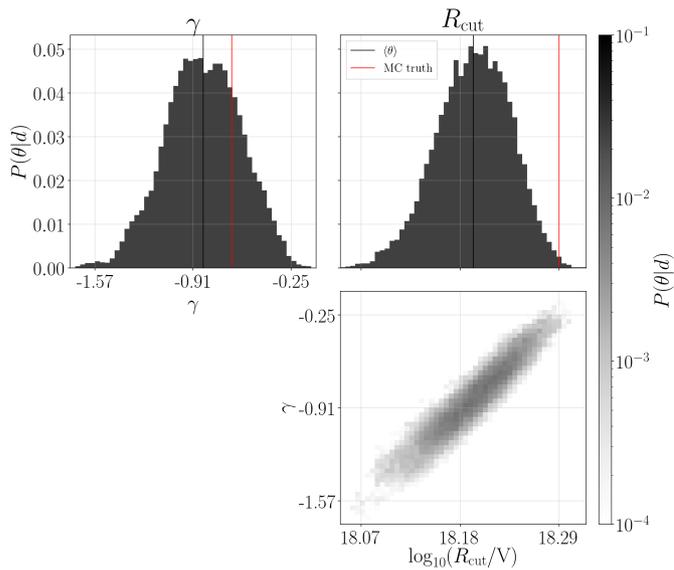
# Fit results: reference model (m=3.4)



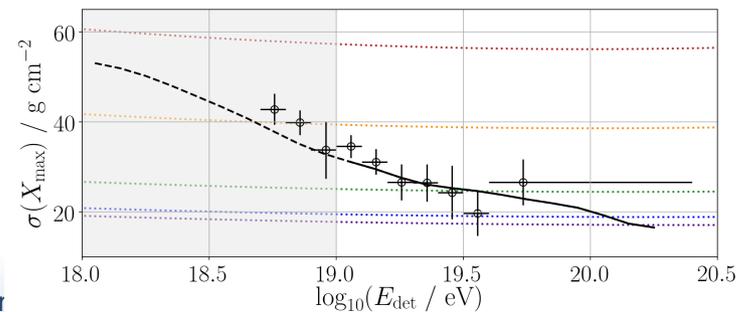
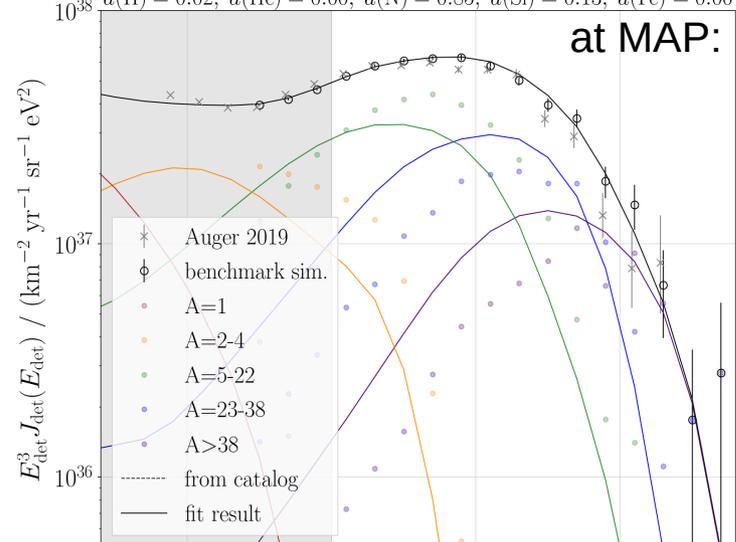
Fitted Source Parameters  
 $\gamma = -0.46$ ,  $\log_{10}(R_{\text{cut}}/V) = 18.30$ ,  $f_0 = 0.000$ ,  $\delta_0 = 0.00$ ,  $\nu_{X_{\text{max}}} = -2.55\sigma$   
 $a(\text{H}) = 0.04$ ,  $a(\text{He}) = 0.56$ ,  $a(\text{N}) = 0.37$ ,  $a(\text{Si}) = 0.03$ ,  $a(\text{Fe}) = 0.00$



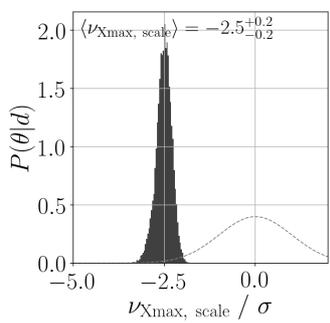
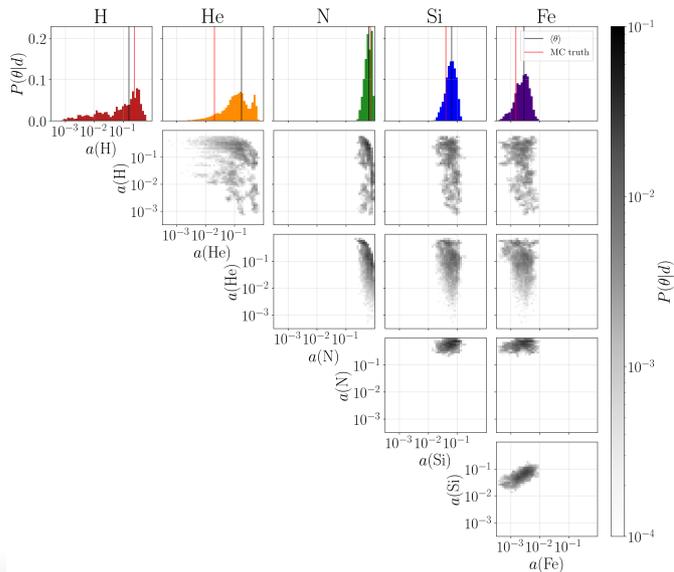
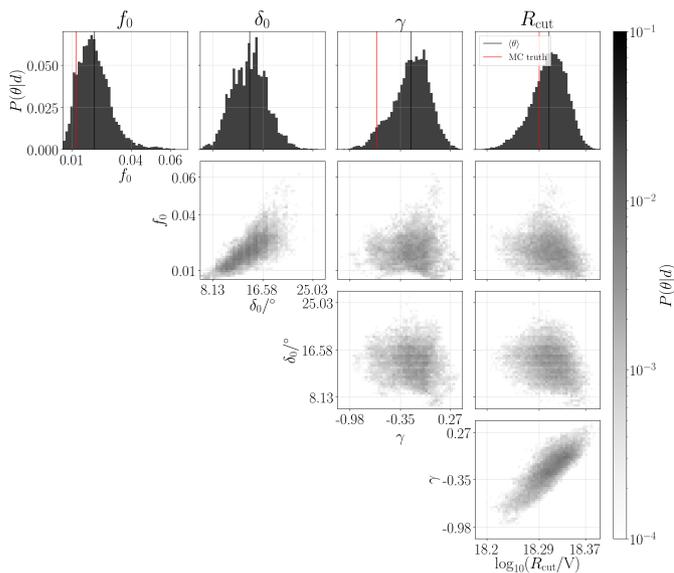
# Fit results: reference model (m=5.0)



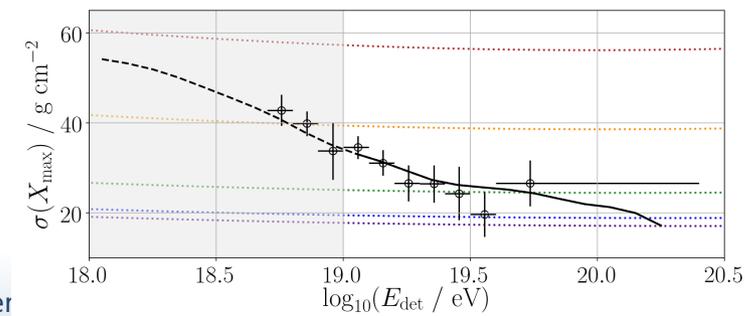
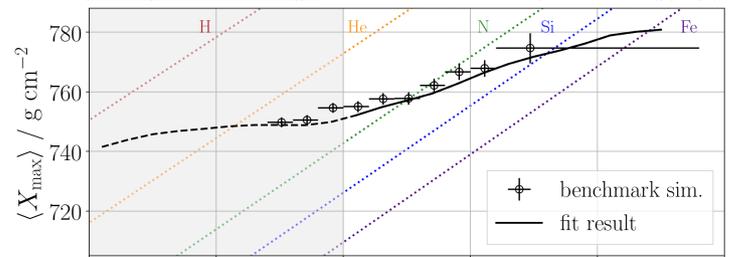
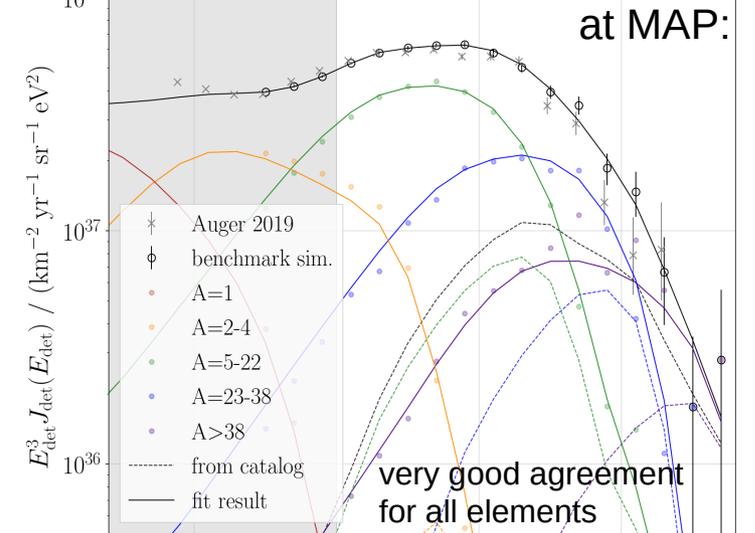
Fitted Source Parameters  
 $\gamma = -0.95$ ,  $\log_{10}(R_{\text{cut}}/V) = 18.18$ ,  $f_0 = 0.000$ ,  $\delta_0 = 0.00$ ,  $\nu_{X_{\text{max}}} = -3.00\sigma$   
 $a(\text{H}) = 0.02$ ,  $a(\text{He}) = 0.00$ ,  $a(\text{N}) = 0.85$ ,  $a(\text{Si}) = 0.13$ ,  $a(\text{Fe}) = 0.00$



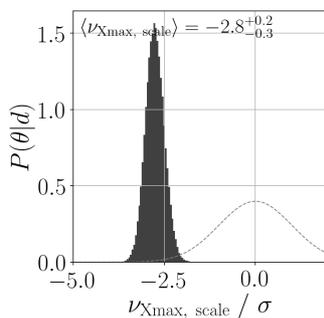
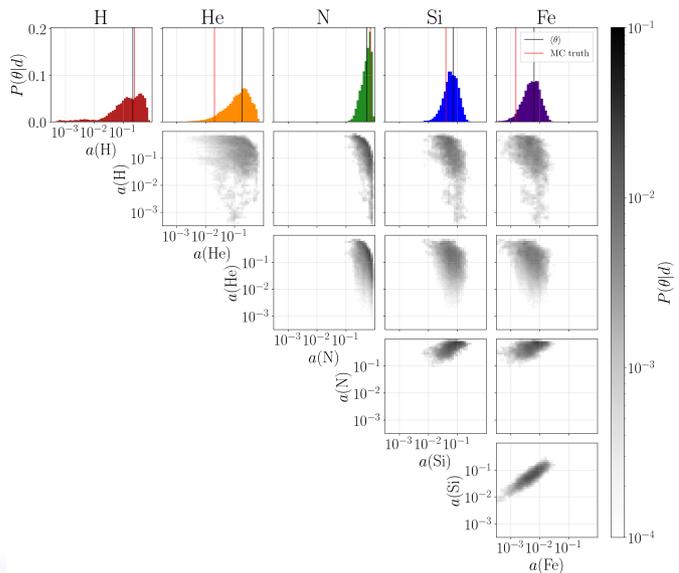
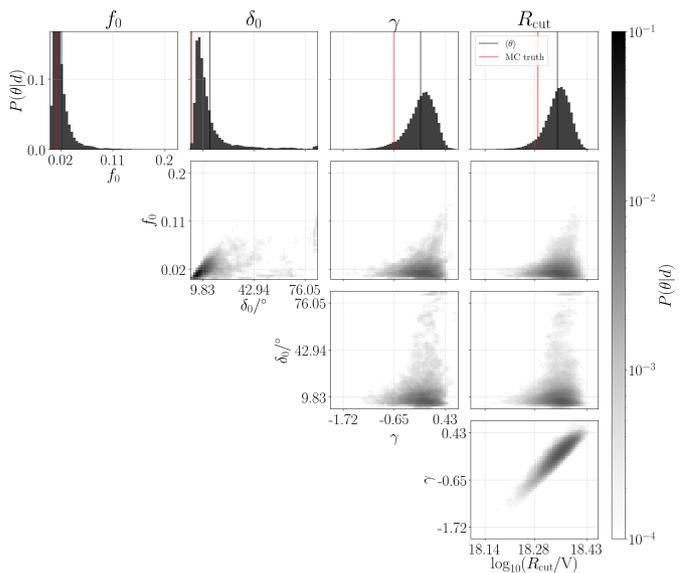
# Fit results: SBG model (m=3.4)



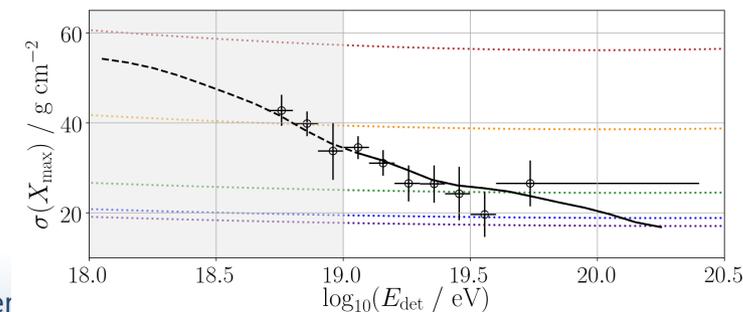
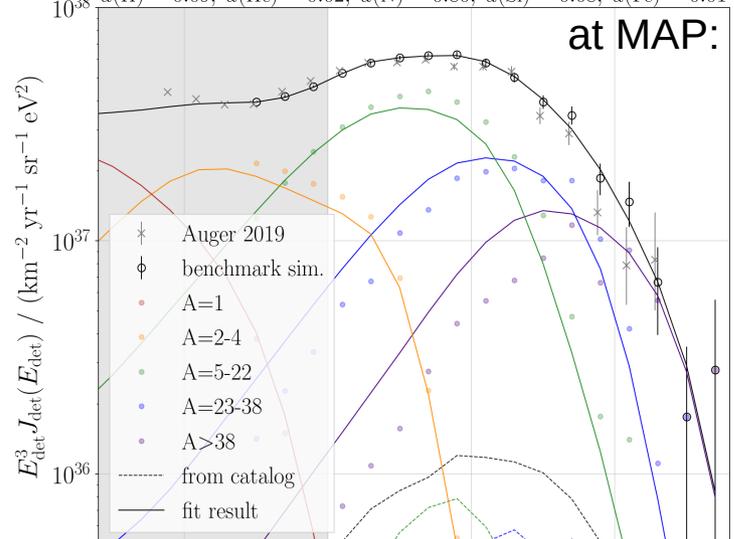
Fitted Source Parameters  
 $\gamma = -0.37$ ,  $\log_{10}(R_{\text{cut}}/V) = 18.30$ ,  $f_0 = 0.022$ ,  $\delta_0 = 15.37^\circ$ ,  $\nu_{X_{\text{max}}} = -2.33\sigma$   
 $a(\text{H}) = 0.05$ ,  $a(\text{He}) = 0.03$ ,  $a(\text{N}) = 0.86$ ,  $a(\text{Si}) = 0.06$ ,  $a(\text{Fe}) = 0.00$



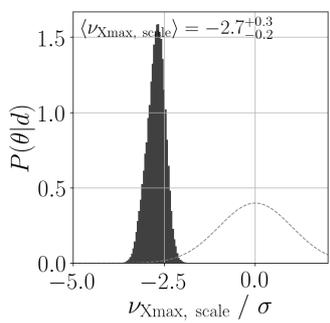
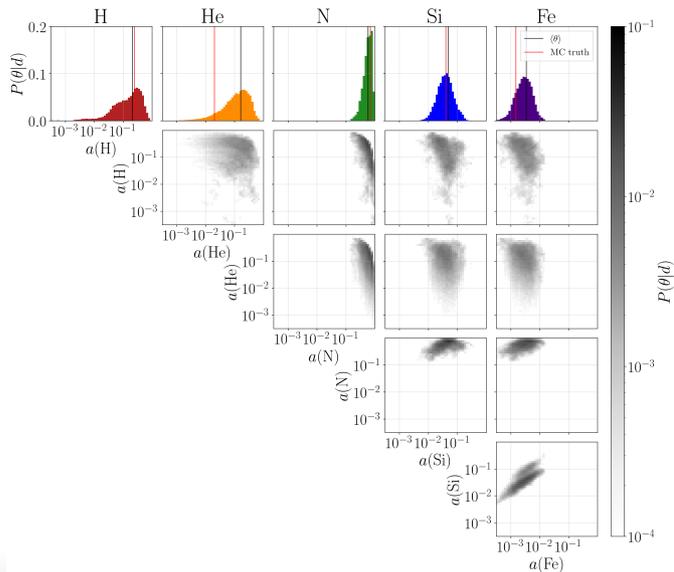
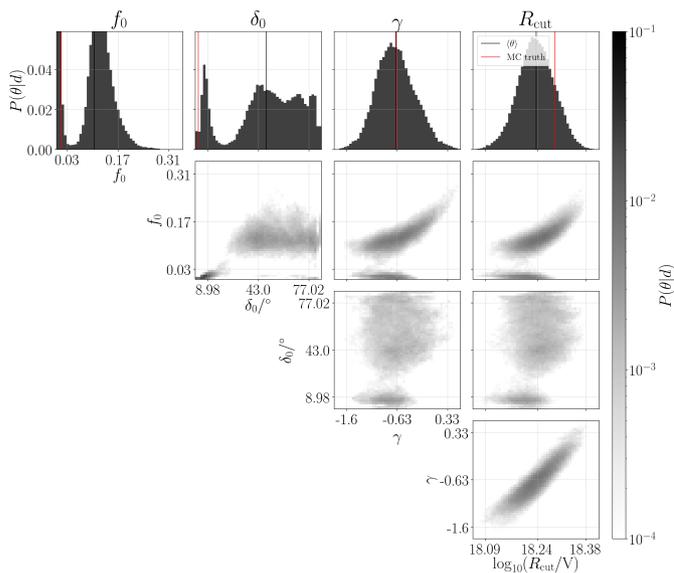
# Fit results: AGN model (m=3.4)



Fitted Source Parameters  
 $\gamma = -0.23$ ,  $\log_{10}(R_{\text{cut}}/V) = 18.34$ ,  $f_0 = 0.008$ ,  $\delta_0 = 4.76^\circ$ ,  $\nu_{X_{\text{max}}} = -2.61\sigma$   
 $a(\text{H}) = 0.09$ ,  $a(\text{He}) = 0.02$ ,  $a(\text{N}) = 0.80$ ,  $a(\text{Si}) = 0.08$ ,  $a(\text{Fe}) = 0.01$



# Fit results: AGN model (m=5.0)



Fitted Source Parameters  
 $\gamma = -0.91$ ,  $\log_{10}(R_{\text{cut}}/V) = 18.22$ ,  $f_0 = 0.110$ ,  $\delta_0 = 43.13^\circ$ ,  $\nu_{X_{\text{max}}} = -2.50\sigma$   
 $a(\text{H}) = 0.00$ ,  $a(\text{He}) = 0.20$ ,  $a(\text{N}) = 0.77$ ,  $a(\text{Si}) = 0.03$ ,  $a(\text{Fe}) = 0.00$

