

“Spider” Millisecond Pulsar Binaries as Potential TeV Emitters

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Fermi LAT Discoveries - Black Widows and Redbacks

- ~100 millisecond pulsars discovered in unidentified Fermi LAT sources
- ~20 black widows, ~9-10 redbacks (>60 known in other bands)

Table 1
Measured and Derived Parameters of BW Pulsars

Name	P_{ms}	\dot{P} (10^{-20})	L_{sd}^a (10^{34} erg s $^{-1}$)	B_8^b	d (kpc)	P_b (hr)	M_{comp} (M_{\odot})	a_{11}	E_{cut} (TeV)	References
J0023+0923 ^c	3.05	1.15	2.50	4.88	0.7	3.3	0.016	1.01	2.40	(1)
J0610-2100 ^c	3.86	0.34	0.36	2.96	3.5	6.9	0.025	1.65	3.04	(2)
J1124-3653 ^c	2.41	0.57	2.50	3.05	1.7	5.4	0.027	1.40	2.03	(1)
J1301+0833 ^c	1.84	0.95	9.36	3.44	0.7	6.5	0.024	1.59	1.37	(3)
J1311-3430 ^c	2.56	2.08	7.64	6.01	1.4	1.56	0.008	0.61	2.33	(4)
J1446-4701 ^c	2.19	1.01	5.93	3.88	1.5	6.7	0.019	1.62	1.52	(5)
J1544+4937 ^c	2.16	0.31	1.87	2.12	1.2	2.8	0.018	0.91	2.72	(6)
J1731-1847	2.34	2.47	11.9	6.26	2.5	7.5	0.04	1.75	1.23	(7)
J1745+1017 ^c	2.65	0.23	0.75	2.02	1.36	17.5	0.016	3.07	1.86	(8)
J1810+1744 ^c	1.66	0.45	6.08	2.26	2	3.6	0.044	1.07	1.86	(1)
J1959+2048 ^c	1.61	0.72	10.6	2.80	1.53	9.2	0.021	2.00	1.19	(9)
J2047+1053 ^c	4.29	2.00	1.56	7.63	2	3	0.035	0.95	2.78	(3)
J2051-0827 ^c	4.51	1.23	0.83	6.14	1	2.4	0.027	0.82	3.51	(2)
J2214+3000 ^c	3.12	1.46	2.96	5.57	1.32	10	0.014	2.11	1.59	(10), (11)
J2234+0944 ^c	3.63	1.94	2.50	6.91	1	10	0.015	2.11	1.66	(3), (5)
J2241-5236 ^c	2.19	0.67	3.90	3.15	0.5	3.4	0.012	1.03	2.12	(12)
J2256-1024 ^c	2.29	1.58	8.11	4.96	0.6	5.1	0.034	1.35	1.54	(1)

Table 2
Measured and Derived Parameters of RB Pulsars

Name	P_{ms}	\dot{P} (10^{-20})	L_{sd}^a (10^{34} erg s $^{-1}$)	B_8^b	d (kpc)	P_b (hr)	M_{comp} (M_{\odot})	a_{11}	E_{cut} (TeV)	References
J1023+0038	1.69	1.20	15.4	3.72	0.6	4.8	0.2	1.33	1.33	(1)
J1628-3205	3.21	1.13	2.11	4.96	1.2	5	0.16	1.36	2.15	(2)
J1723-2837	1.86	0.75	7.18	3.08	0.75	14.8	0.4	2.90	1.09	(3), (4)
J1816+4510 ^c	3.19	4.03	7.64	9.34	2.4	8.7	0.16	1.97	1.30	(5)
J2129-0429	7.61	43.54	6.08	47.4	0.9	15.2	0.37	2.94	1.12	(6)
J2215+5135 ^c	2.61	2.79	9.67	7.03	3	4.2	0.22	1.22	1.55	(6)
J2339-0533 ^c	2.88	1.39	3.59	5.21	0.4	4.6	0.26	1.30	1.93	(7), (8)

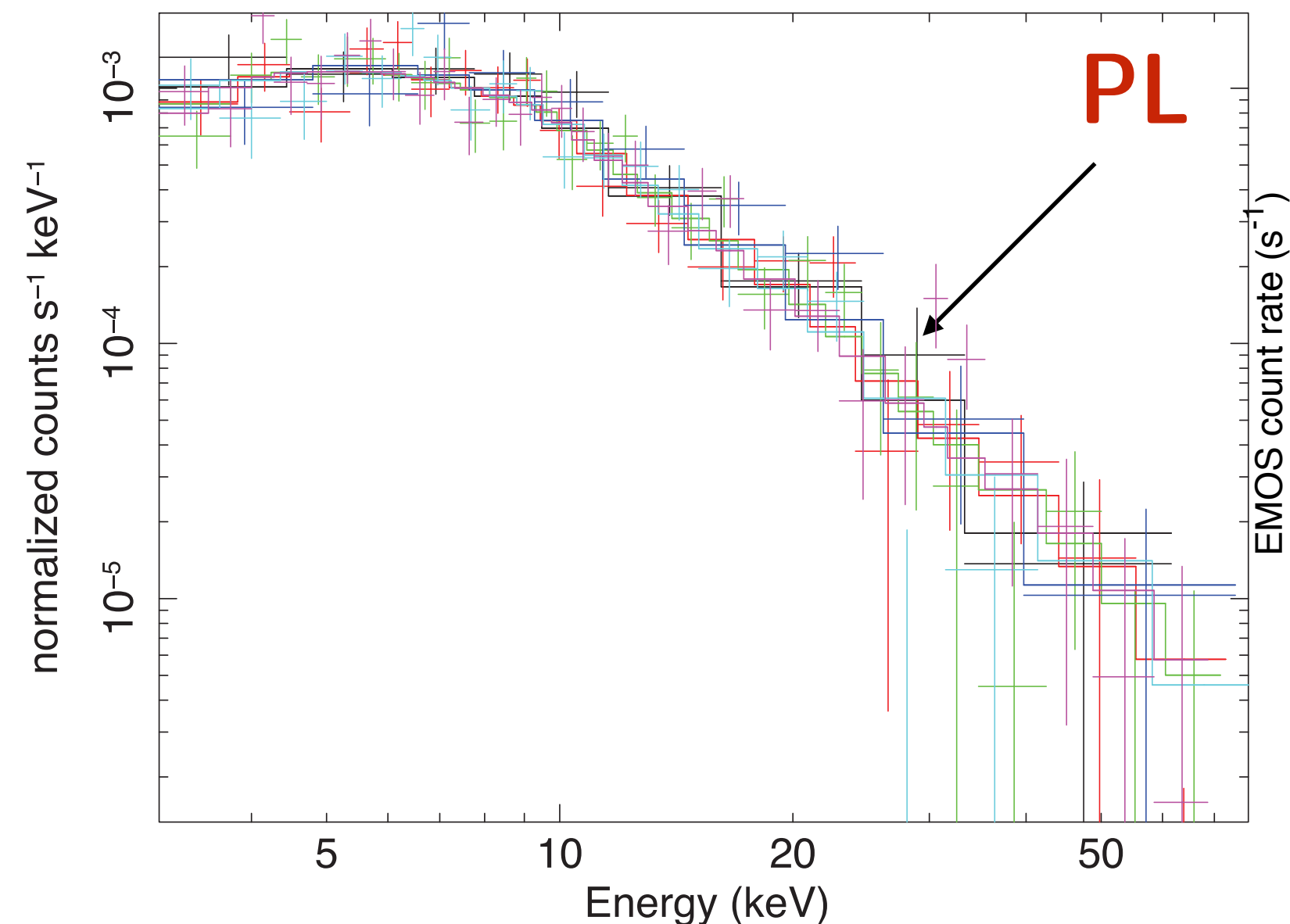
Why are “Spider” Binaries Interesting?

- We know pulsar winds are good accelerators and make TeV emission
- Clean systems: **circular orbits**, many orbits, pulsar well timed, companion radial velocities ==> inclination and component masses constrained
- Fermi gamma-ray pulsations — constrains pulsar magnetic obliquity and also binary inclination (if spin and orbital axes aligned)
- **Many** of them (~10 now with X-ray obs, ~60 in the radio) and growing
- Study shock acceleration and pulsar winds in **oblique shocks**
- **Doppler boosting along shock necessary to match X-ray LCs.** This constrains the character of the pulsar termination shock
- Target photons inverse Compton in the TeV
- Flares of the companion — $u \sim 1$ to $u \gg 1$ erg/cm³ — well suited flaring timescales for IACTs
- Double humped SED should peak in the MeV and TeV — some (all?) could be “gamma-ray binaries”
- Exciting for CTA and AMEGO (or any other sensitive MeV concepts)

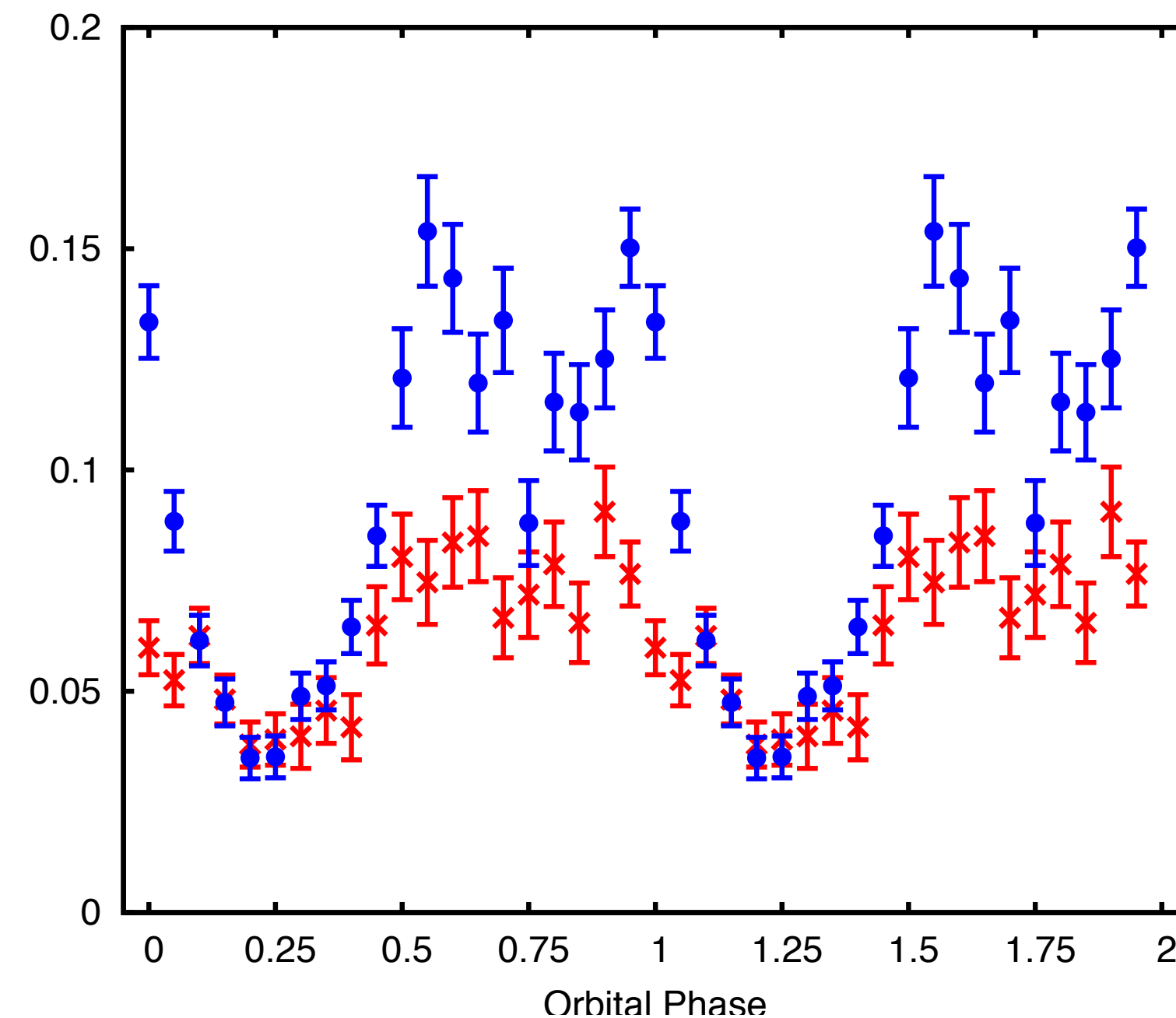
X-ray Observations

- Spectral photon indices are typically $\Gamma \approx 1-1.5$ implying very hard underlying electron power-law distributions and efficient acceleration
- Up to 80 keV NuSTAR PL implies downstream shocked $B \gtrsim 1$ G by containment (Hillas criterion) arguments

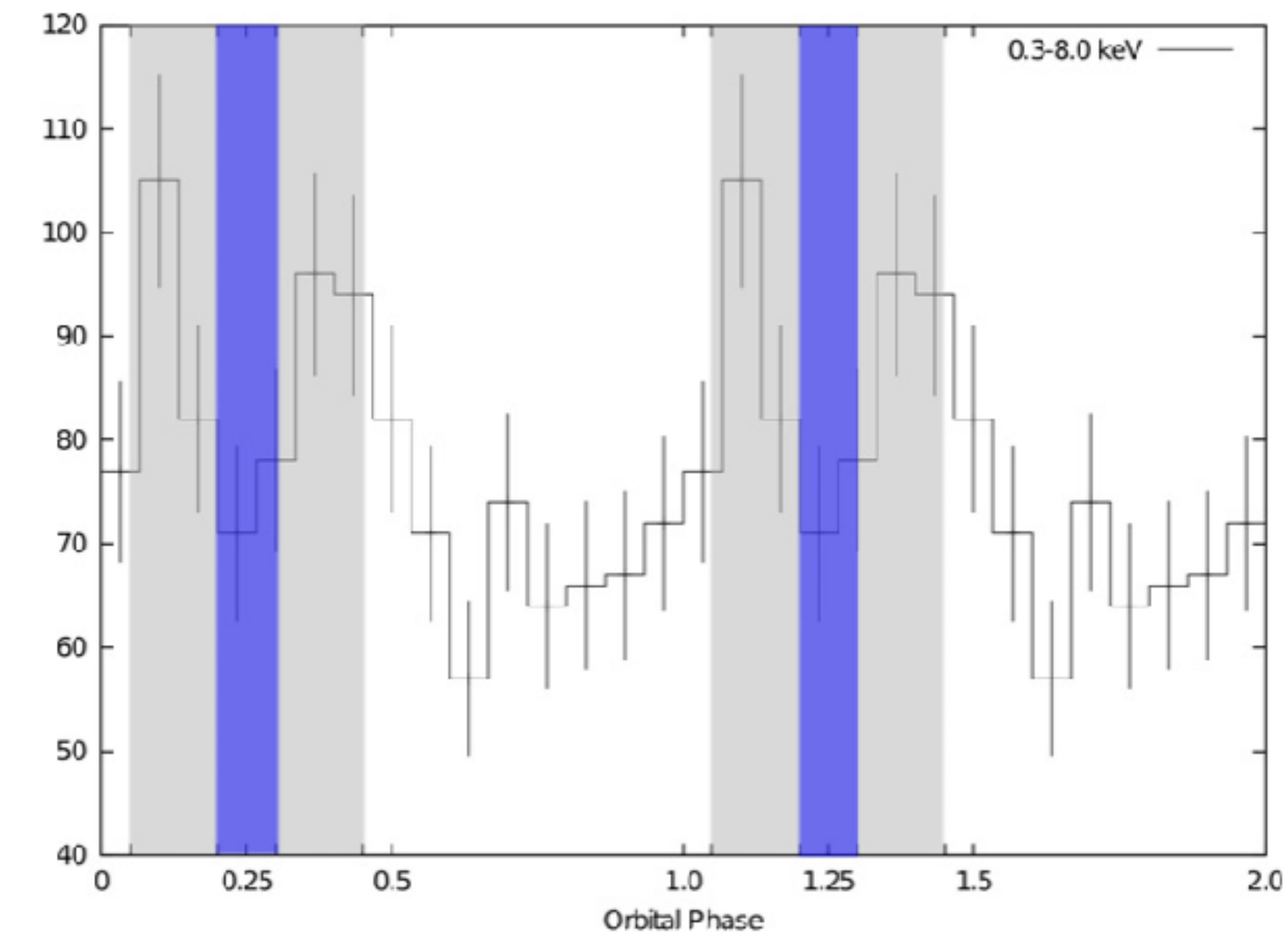
J1023+0038 (rotation-powered state)
Tendulkar et al. (2014)



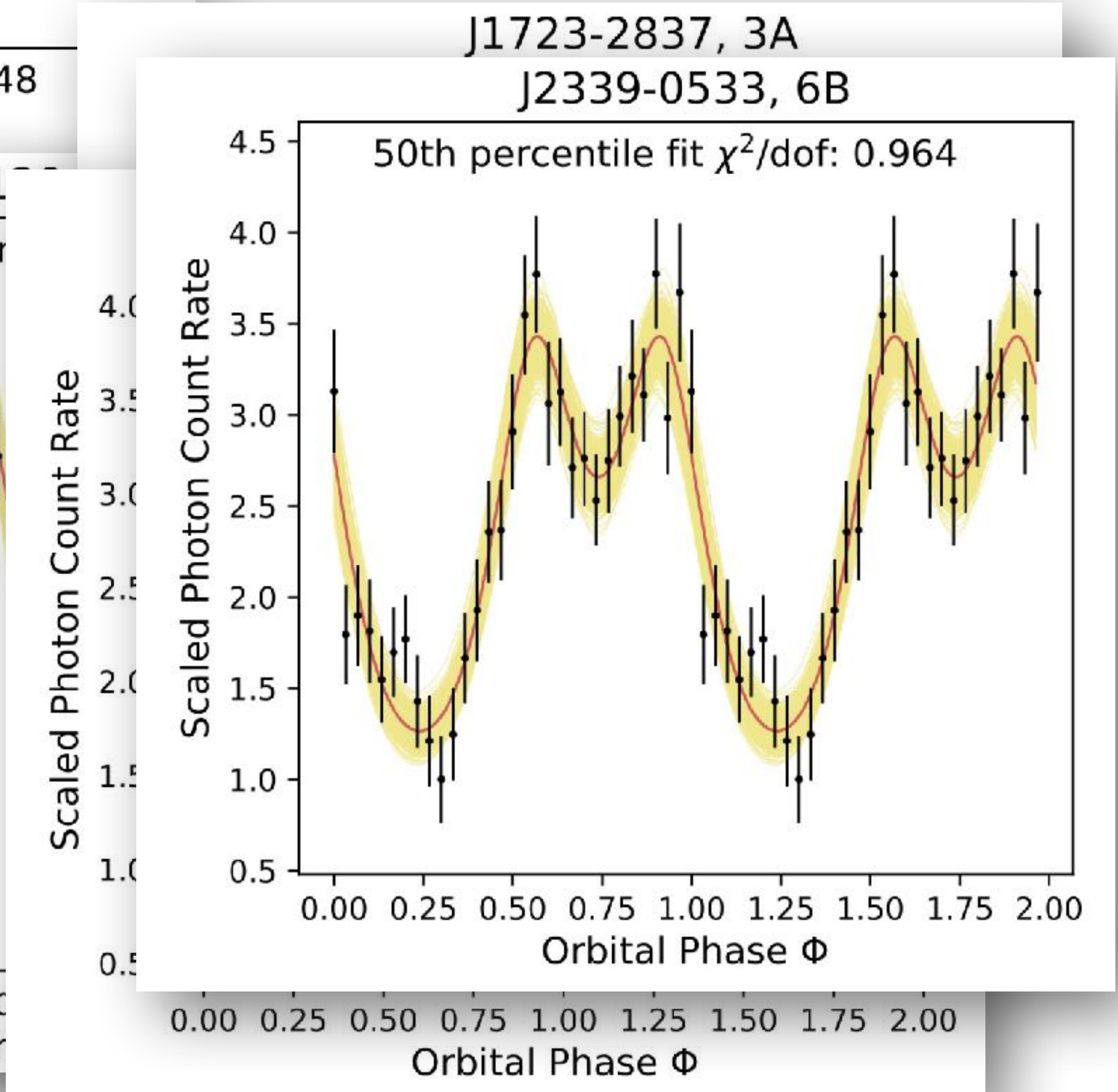
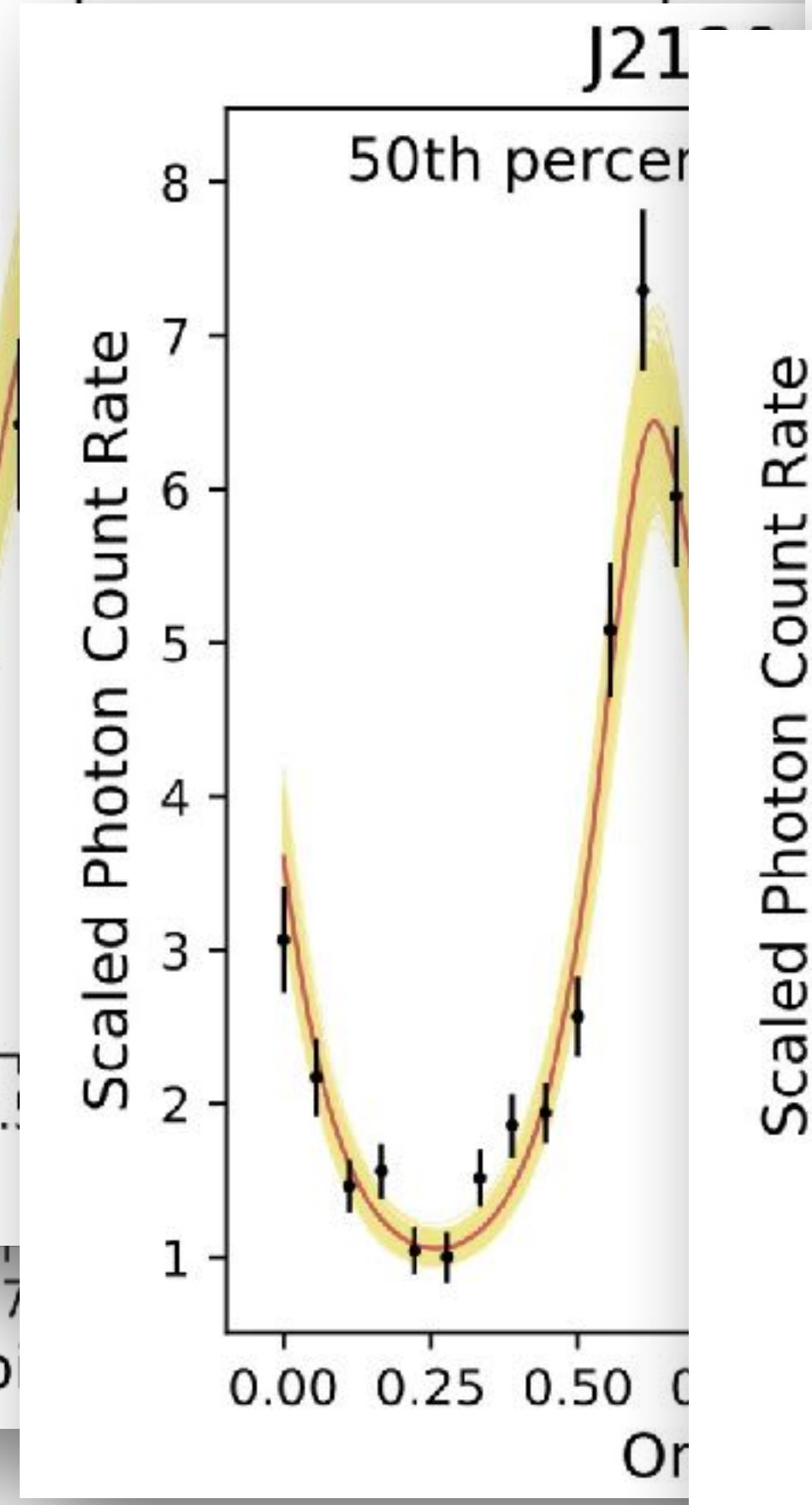
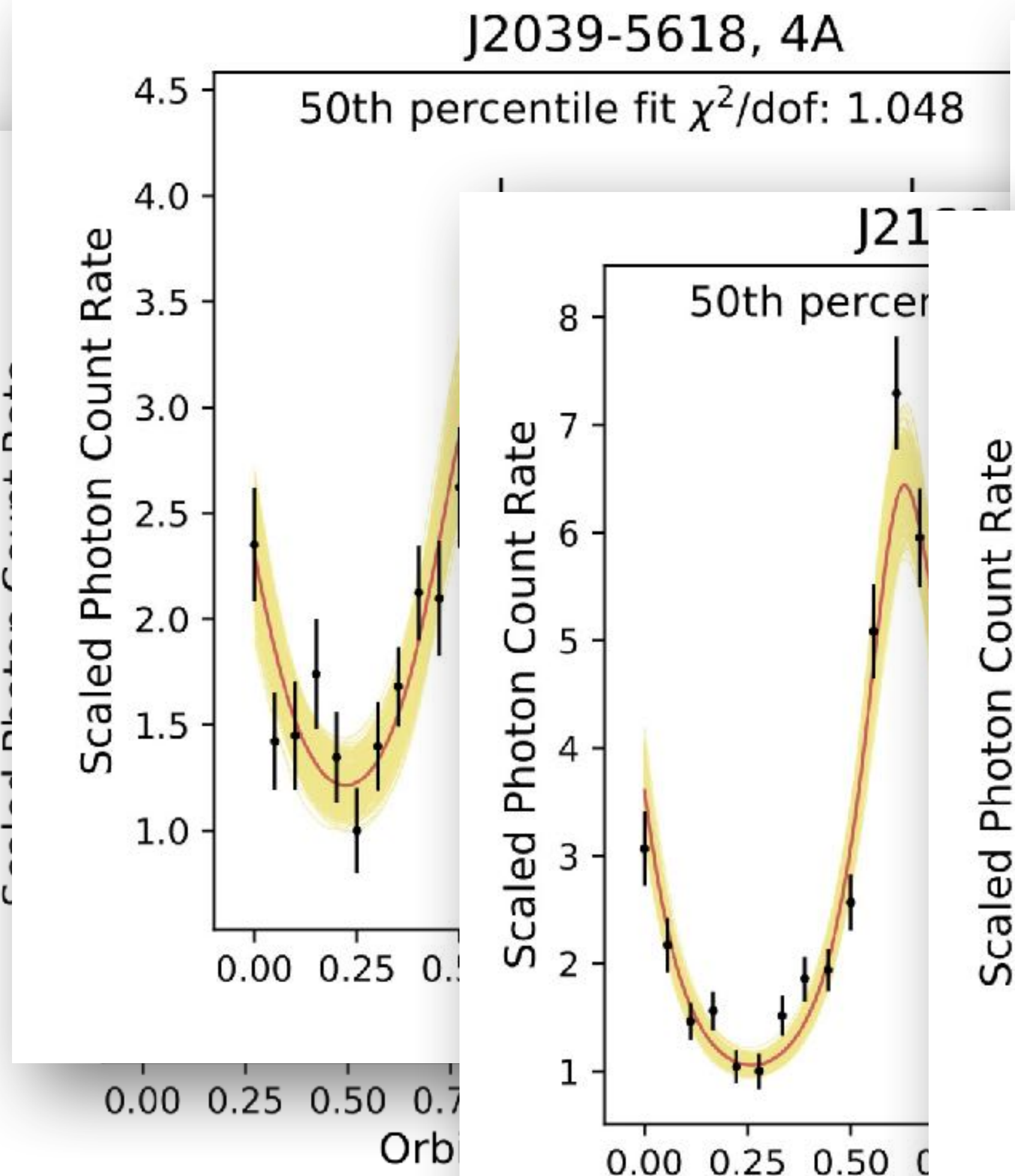
J1227-4853, de Martino et al. (2015)

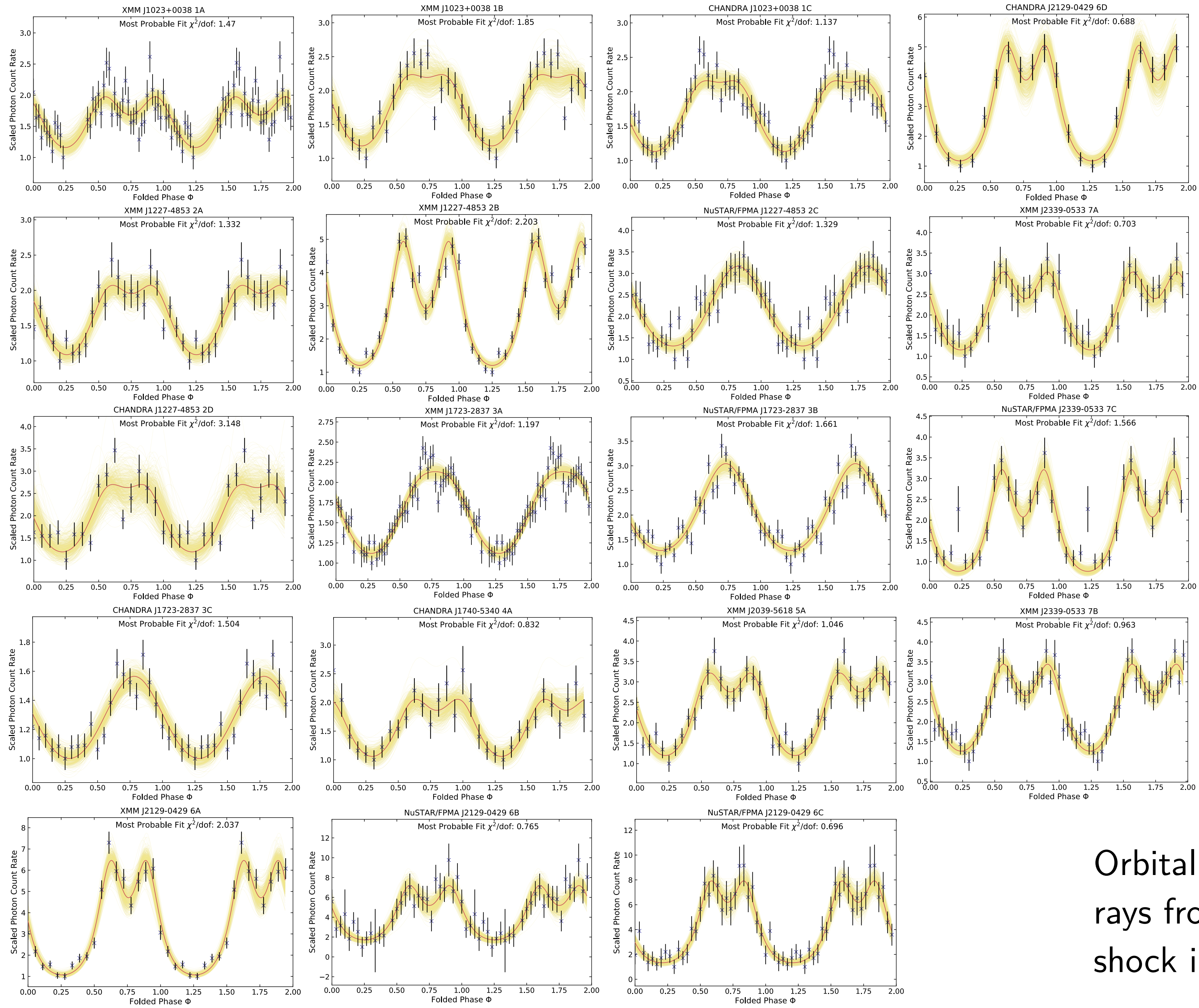


B1957+20, Huang et al. (2012)



Geometric X-ray LC Fitting

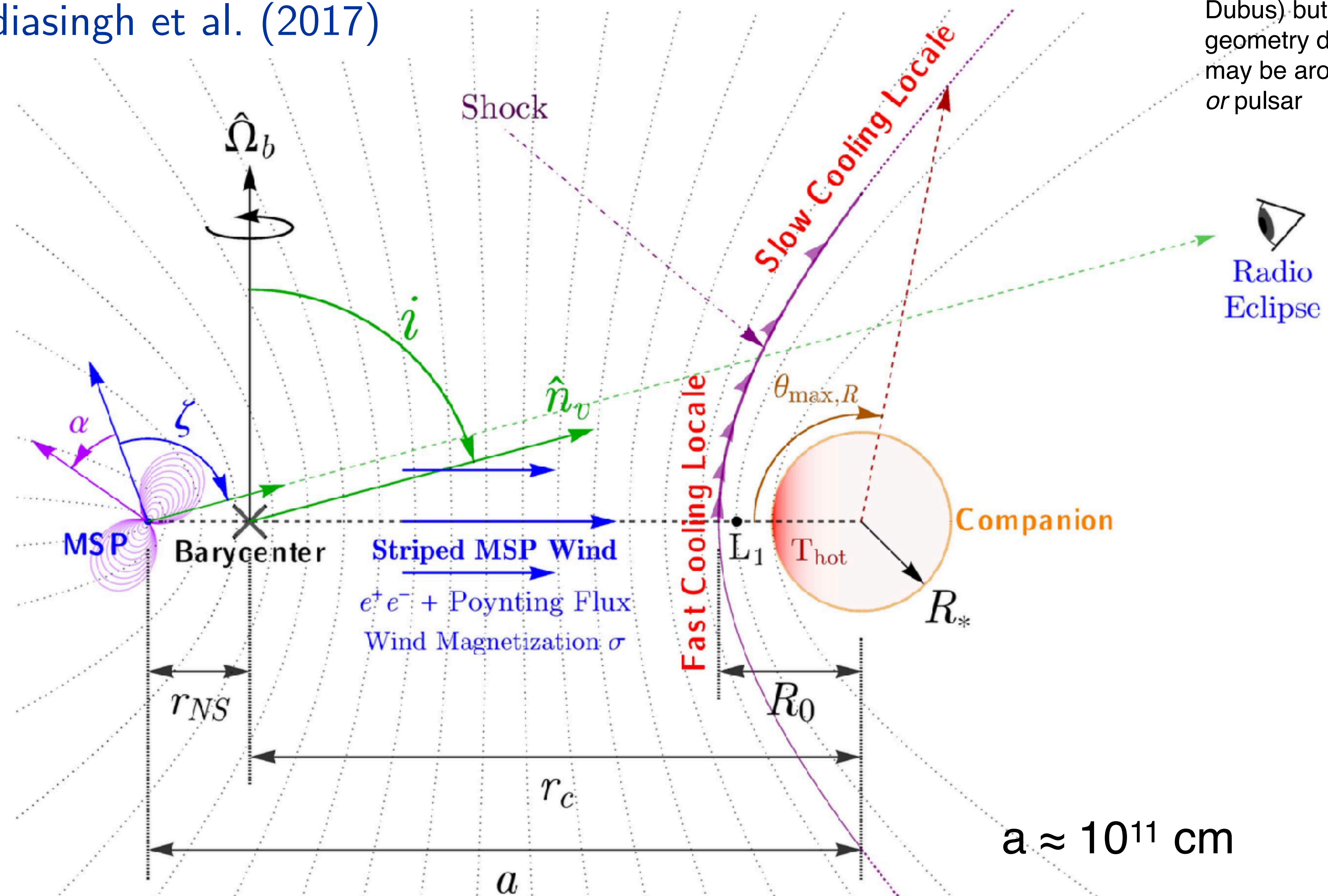




Orbital Modulation of X-rays from the intrabinary shock in redbbacks

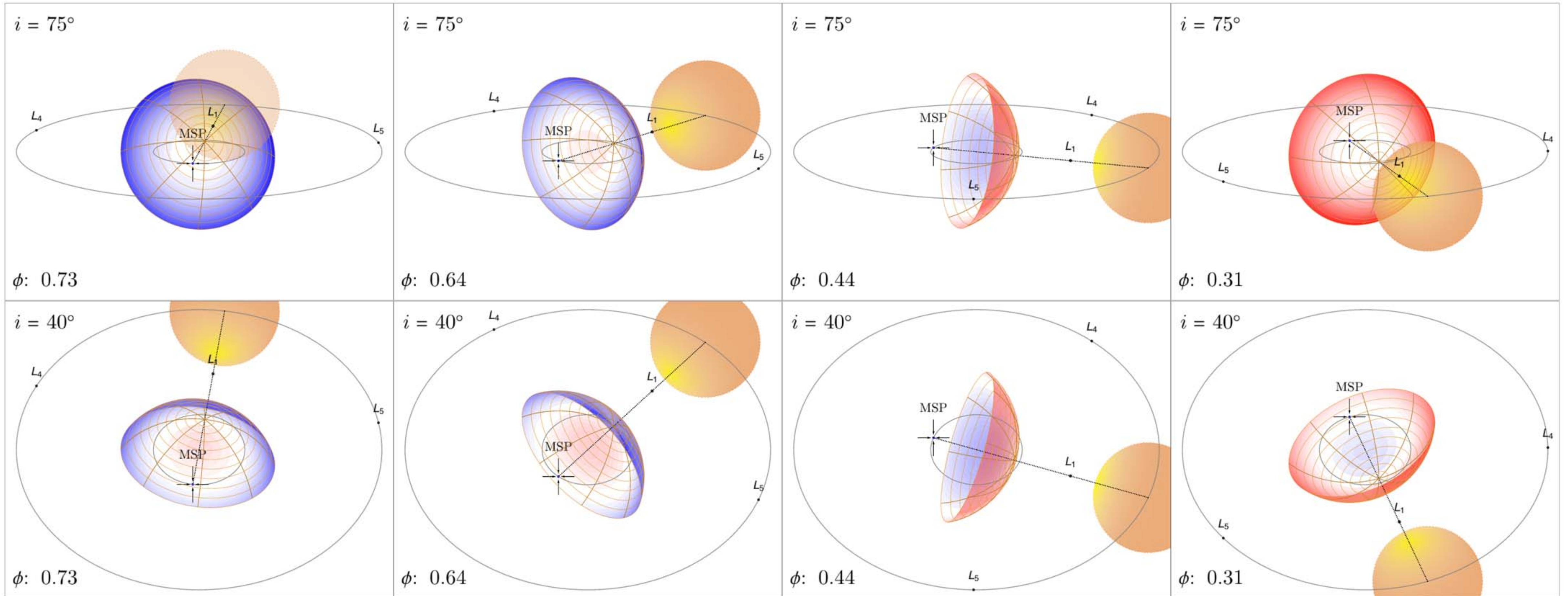
Schematic Geometry (Pulsar State)

Wadiasingh et al. (2017)



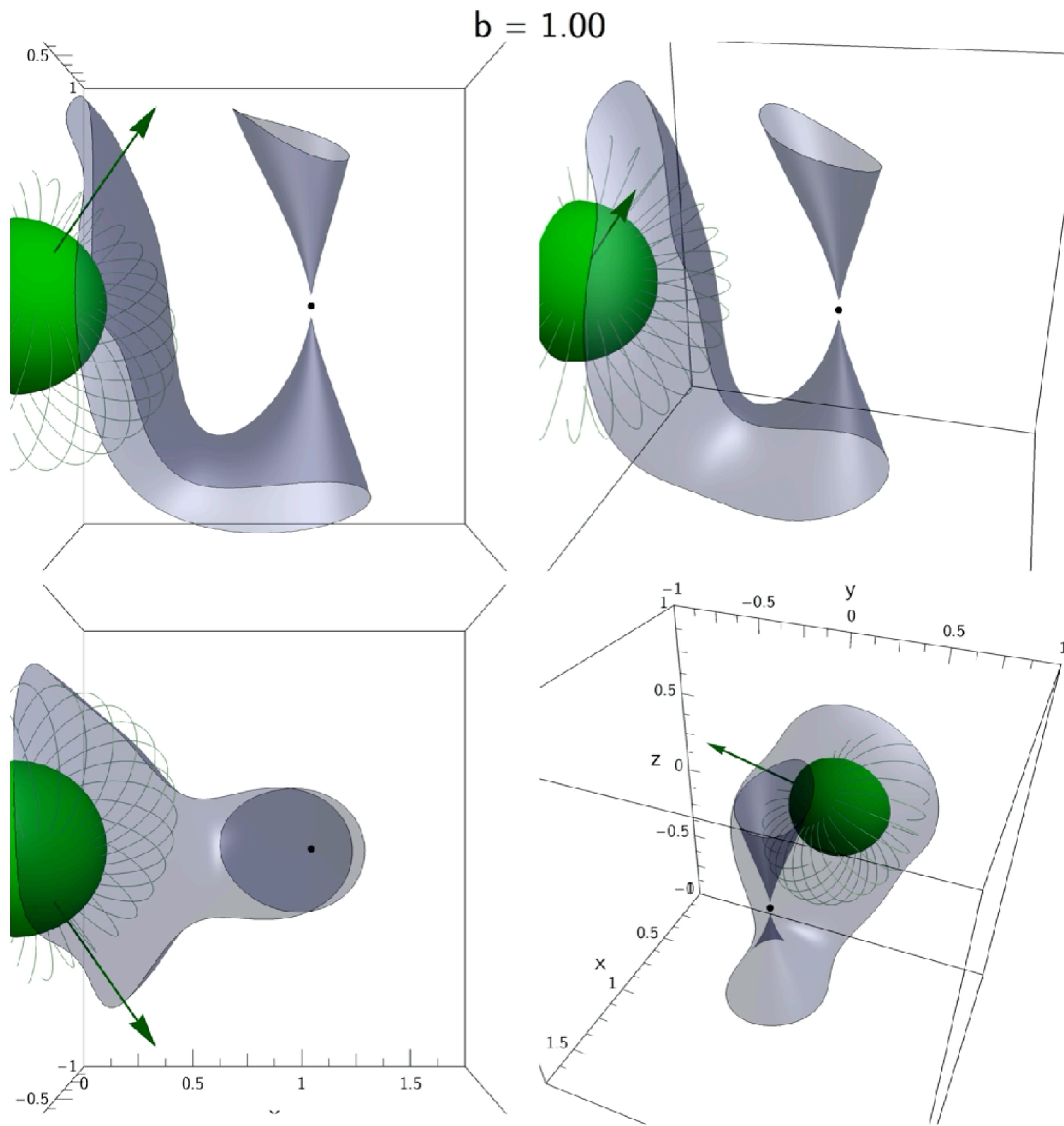
Physics somewhat similar to massive binaries (cf. Dubus) but scales and geometry differ — shock may be around companion or pulsar

Model Schematic – Doppler Boosting



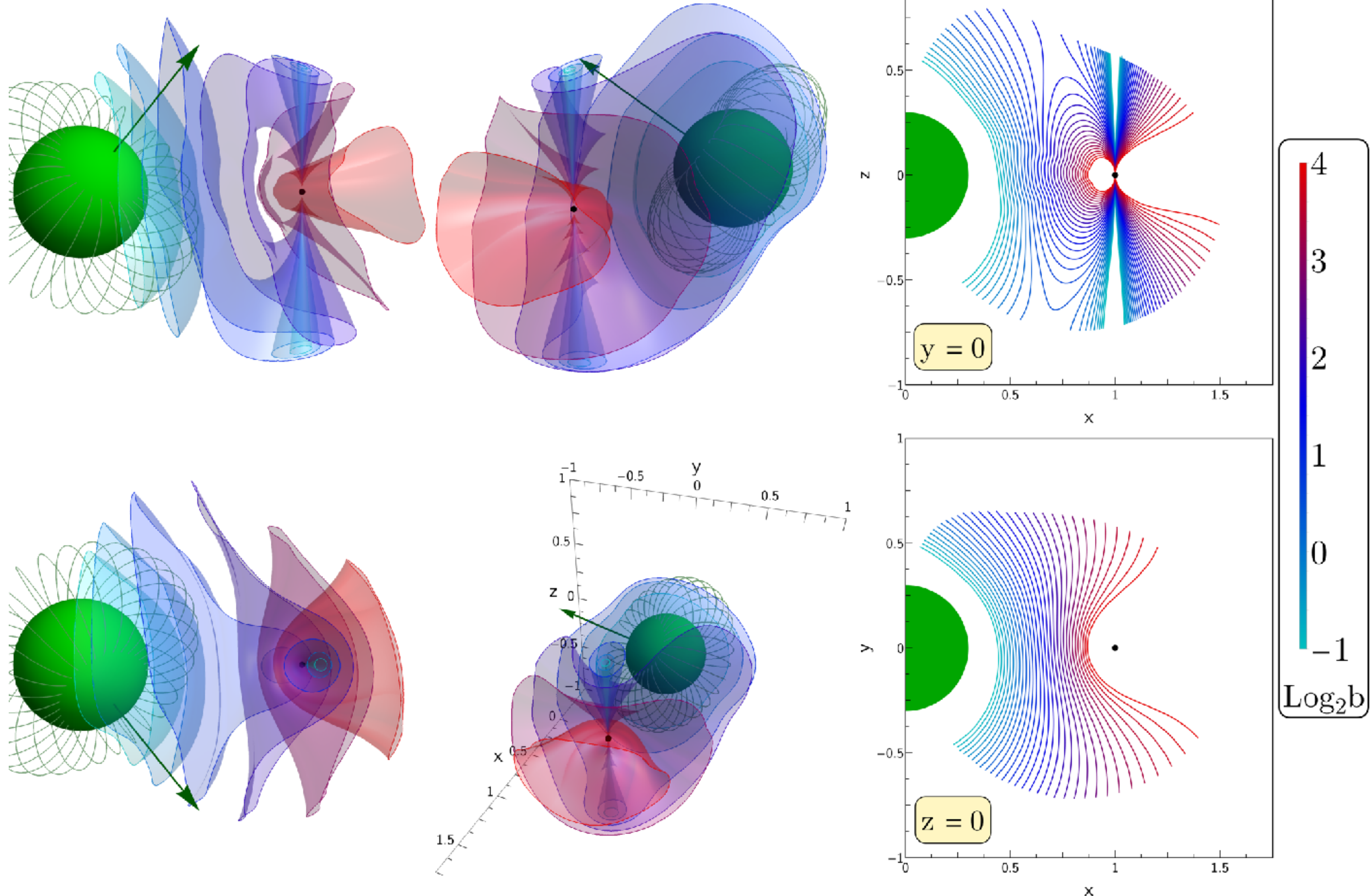
Van der Merwe, Wadiasingh, Venter, Harding & Baring;
ApJ 904:91, 2020

Pulsar Wind + companion B



Pulsar Wind + companion B

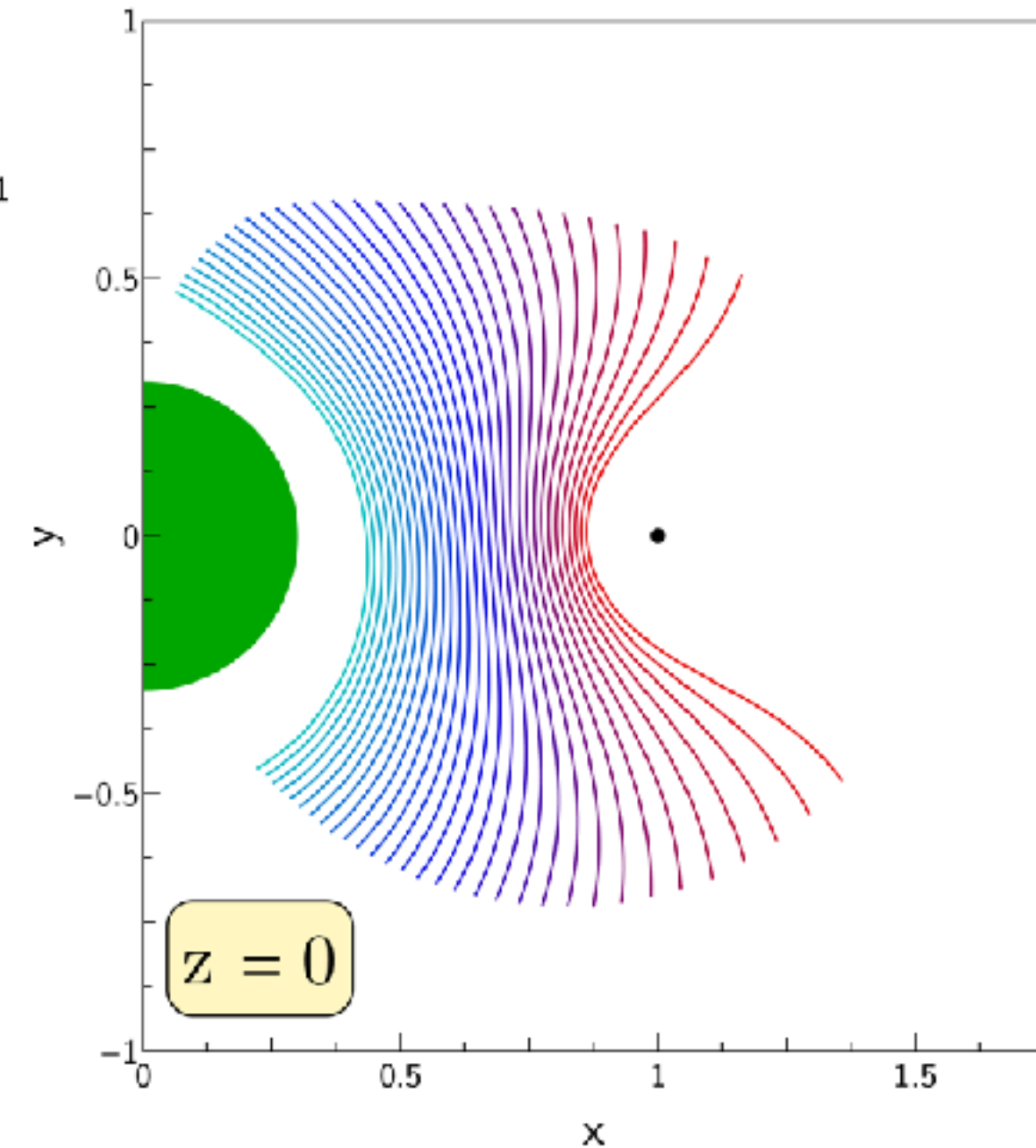
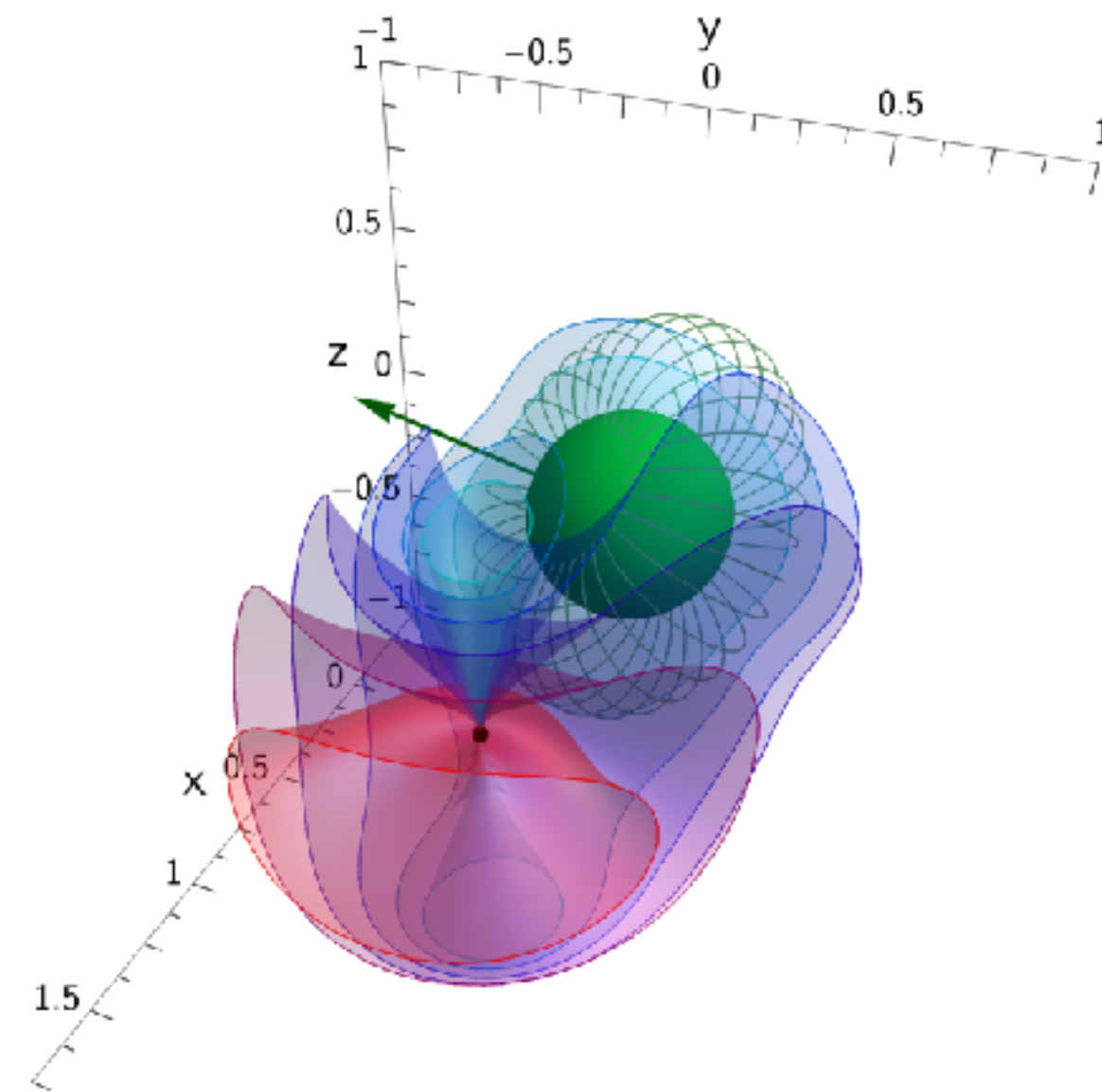
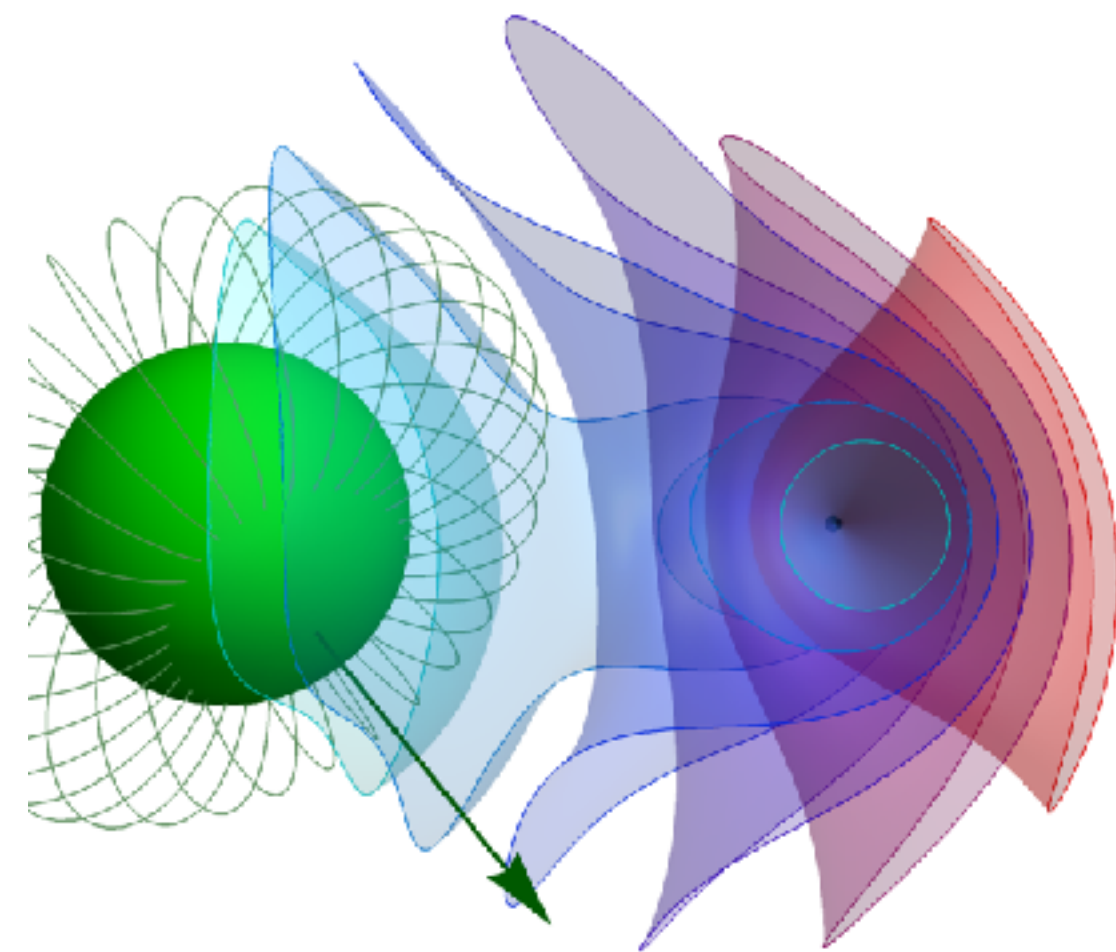
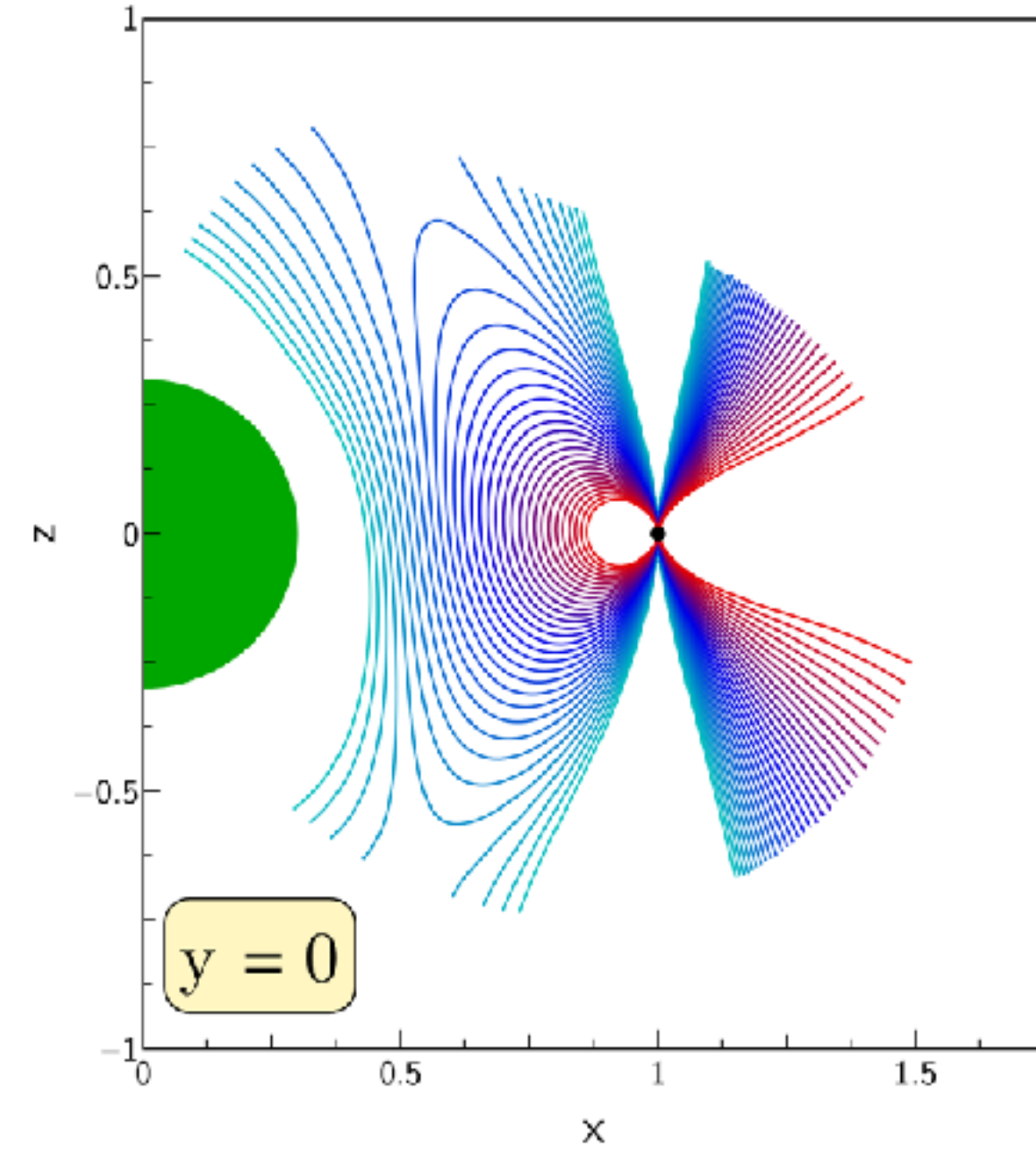
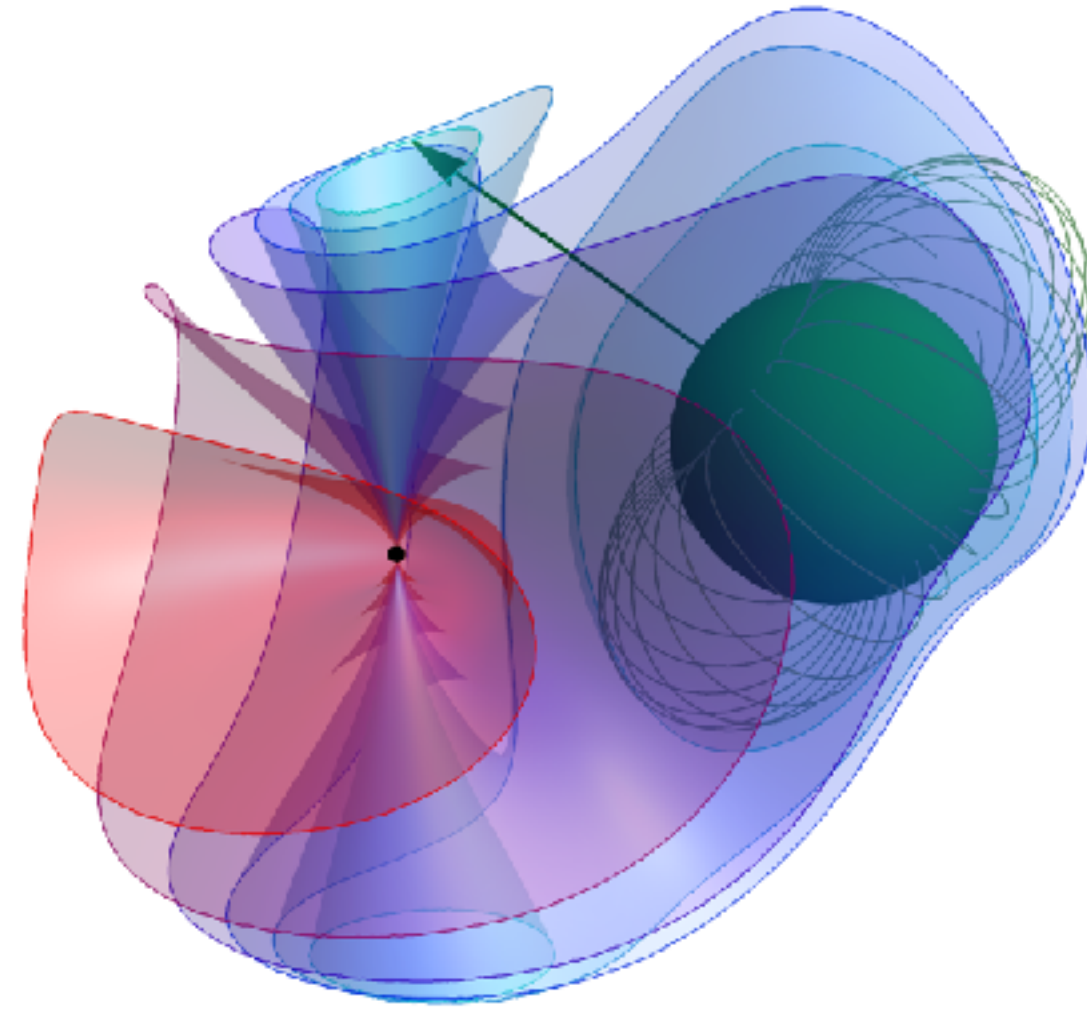
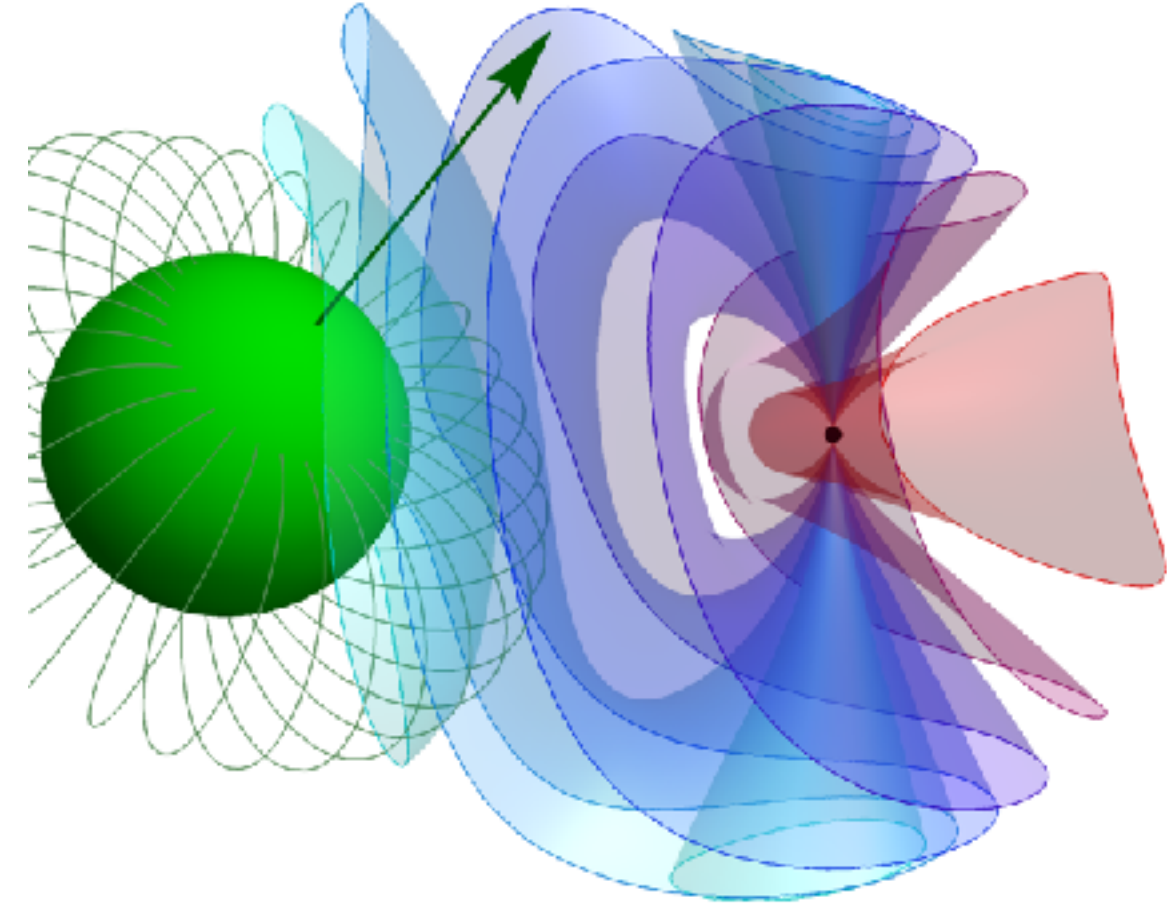
$\alpha = 15^\circ$



Wadiasingh et al. (2018)

Pulsar Wind + companion B

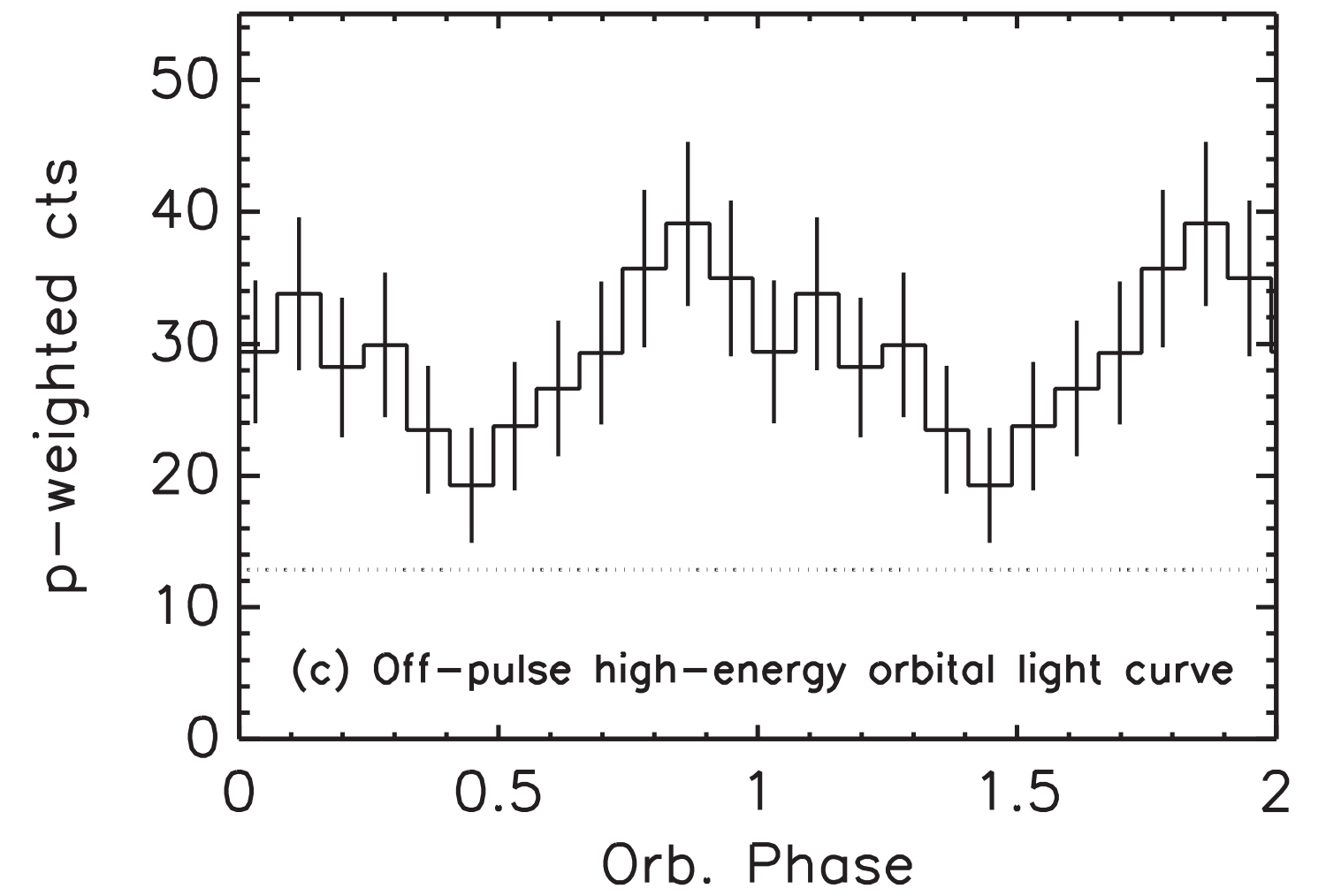
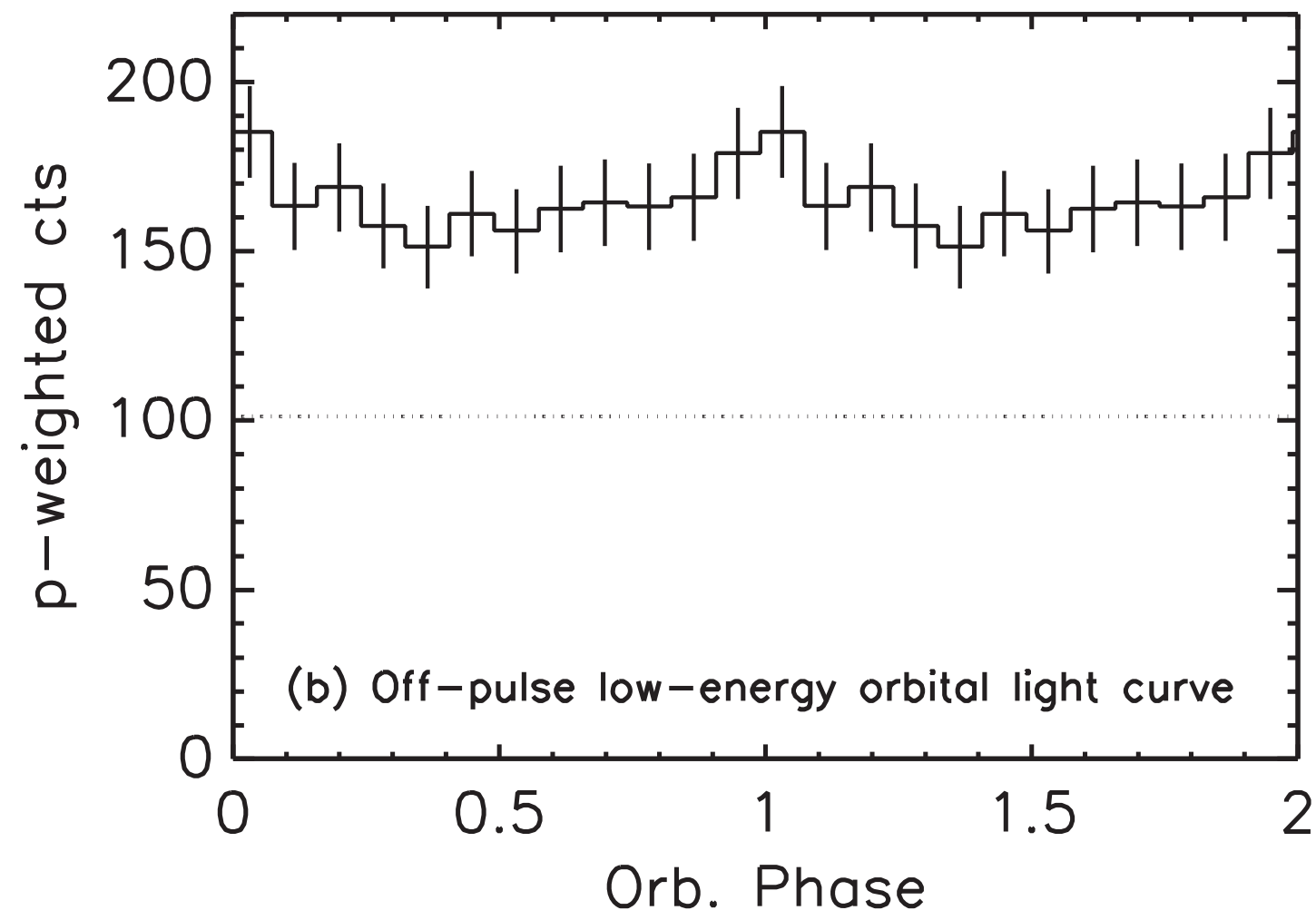
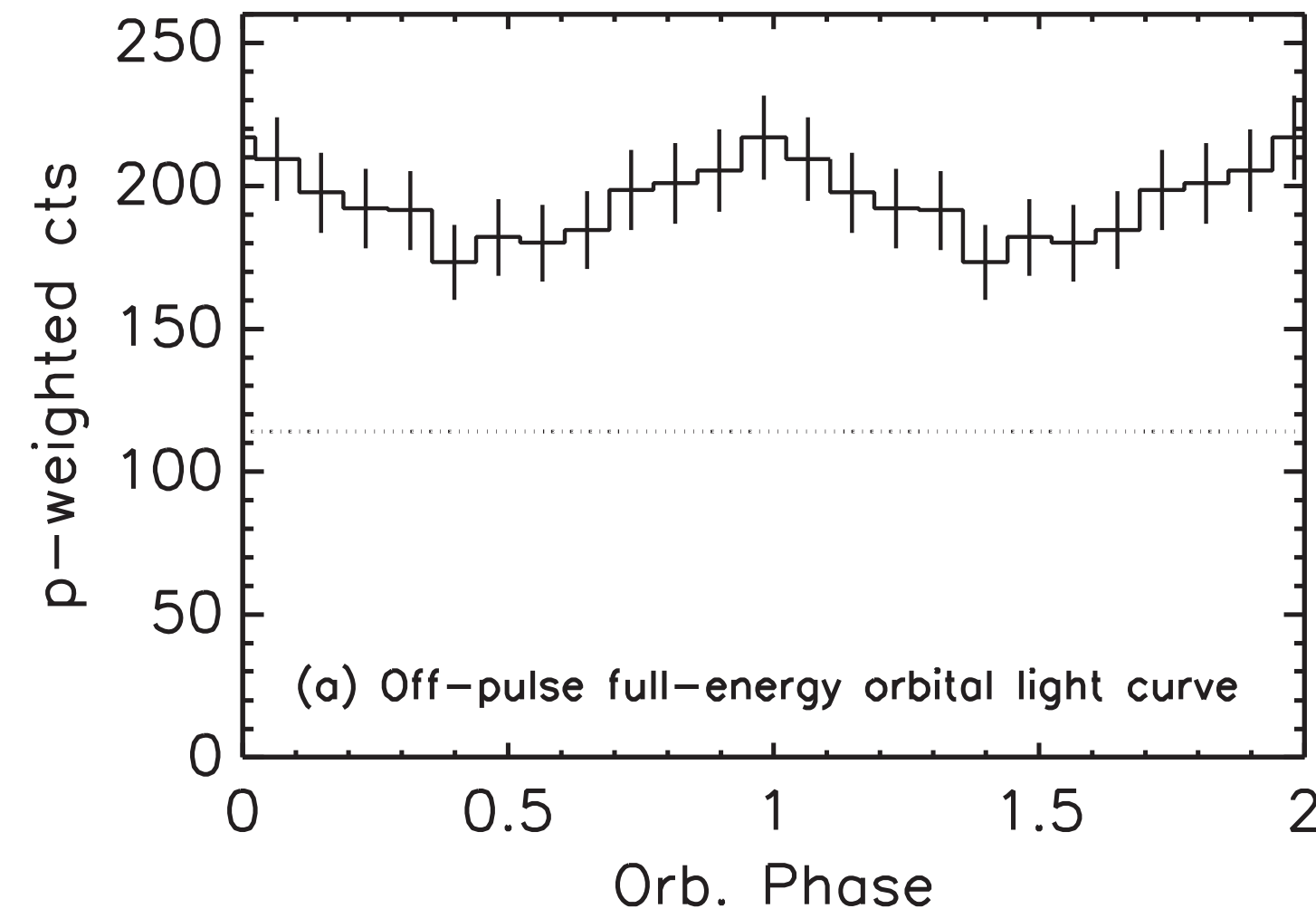
$\alpha = 90^\circ$



Wadiasingh et al. (2018)

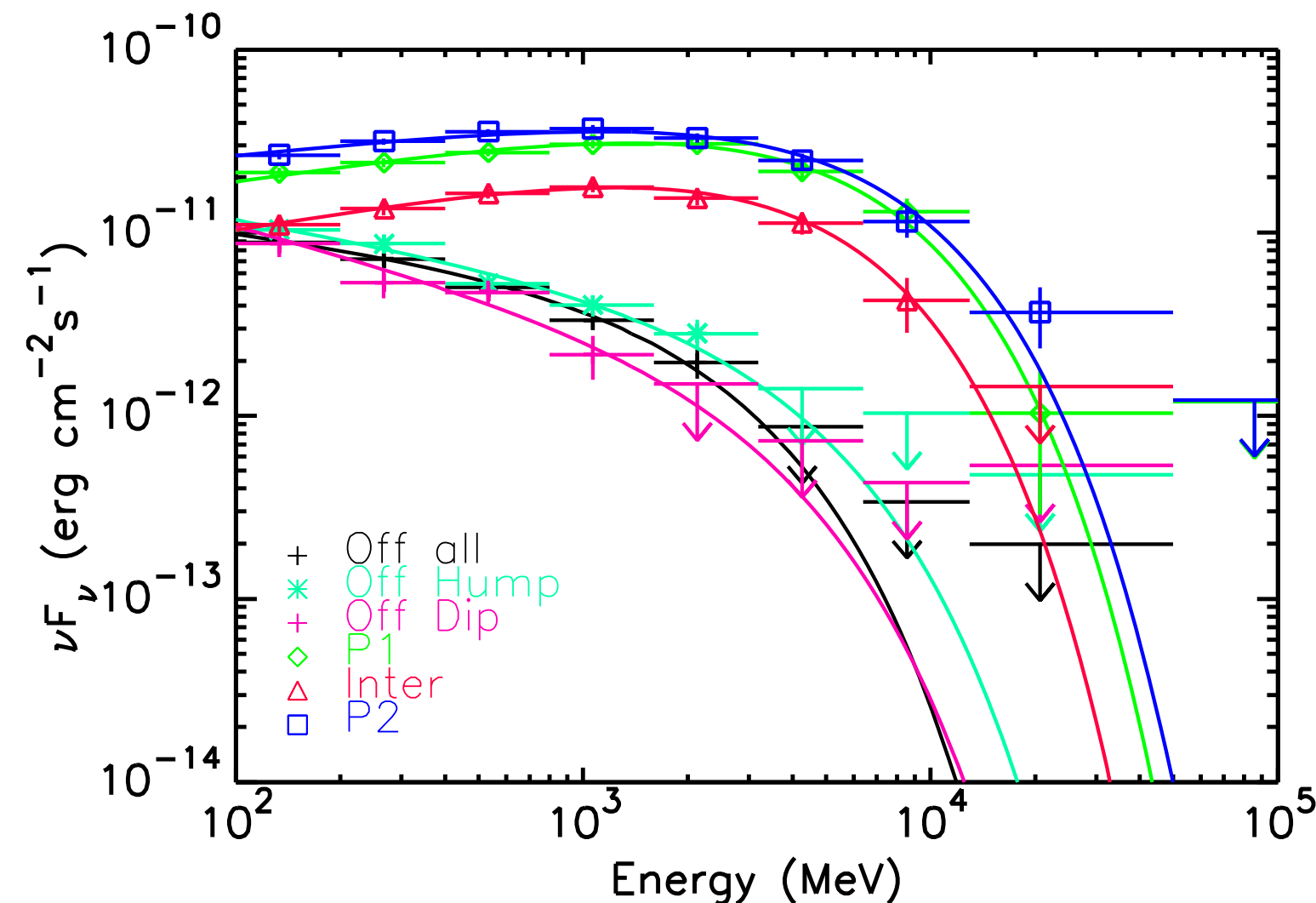
Fermi-LAT Orbital Modulation

Seen in a small subset of spiders



Black widow
J1311–3430

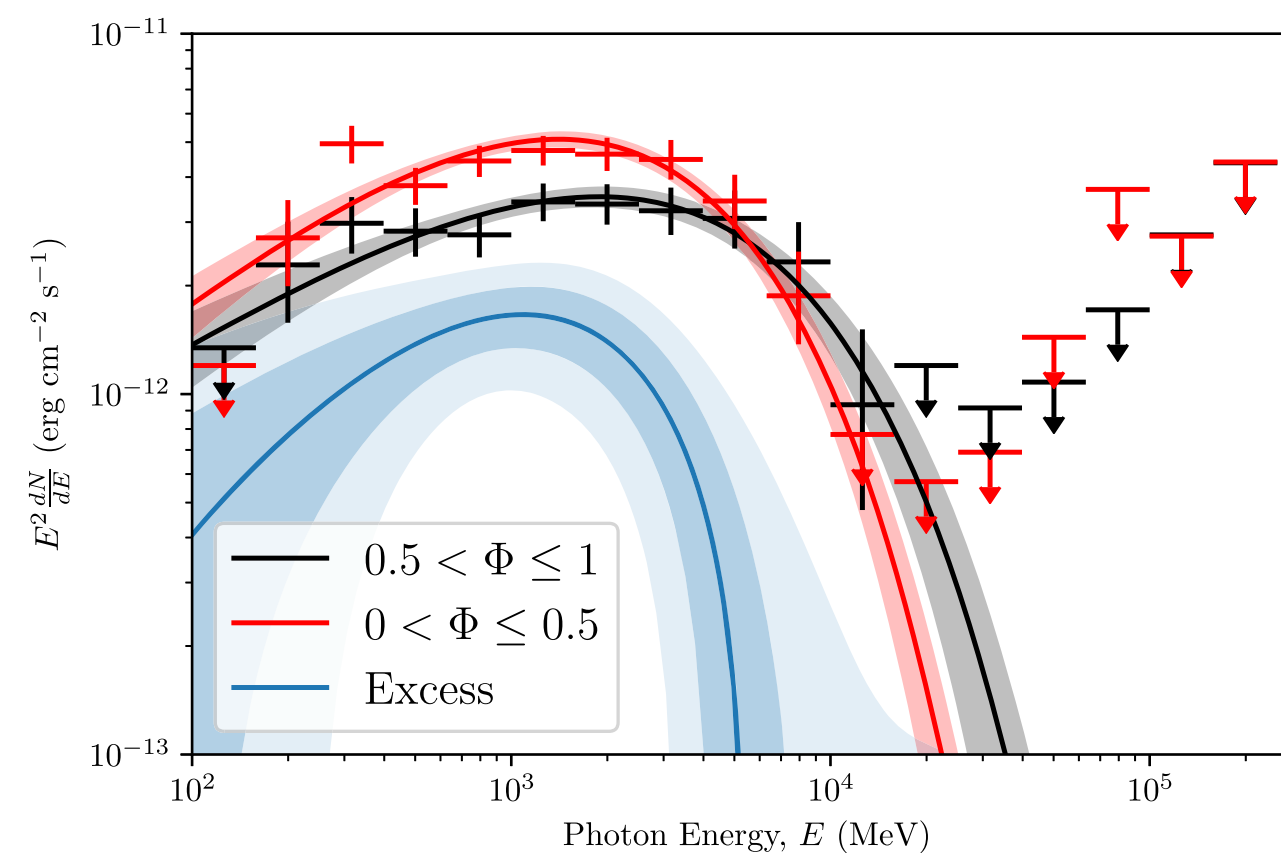
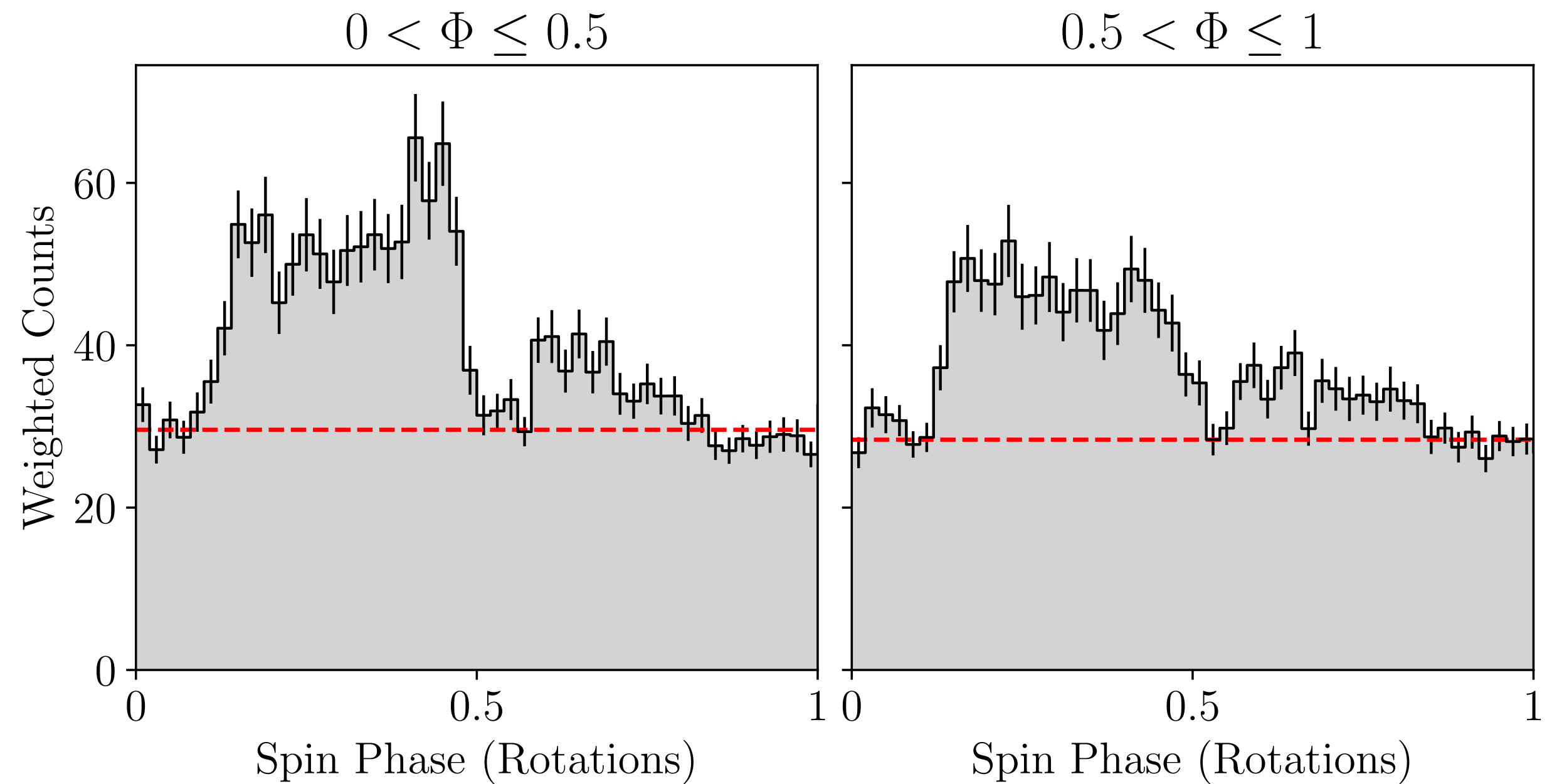
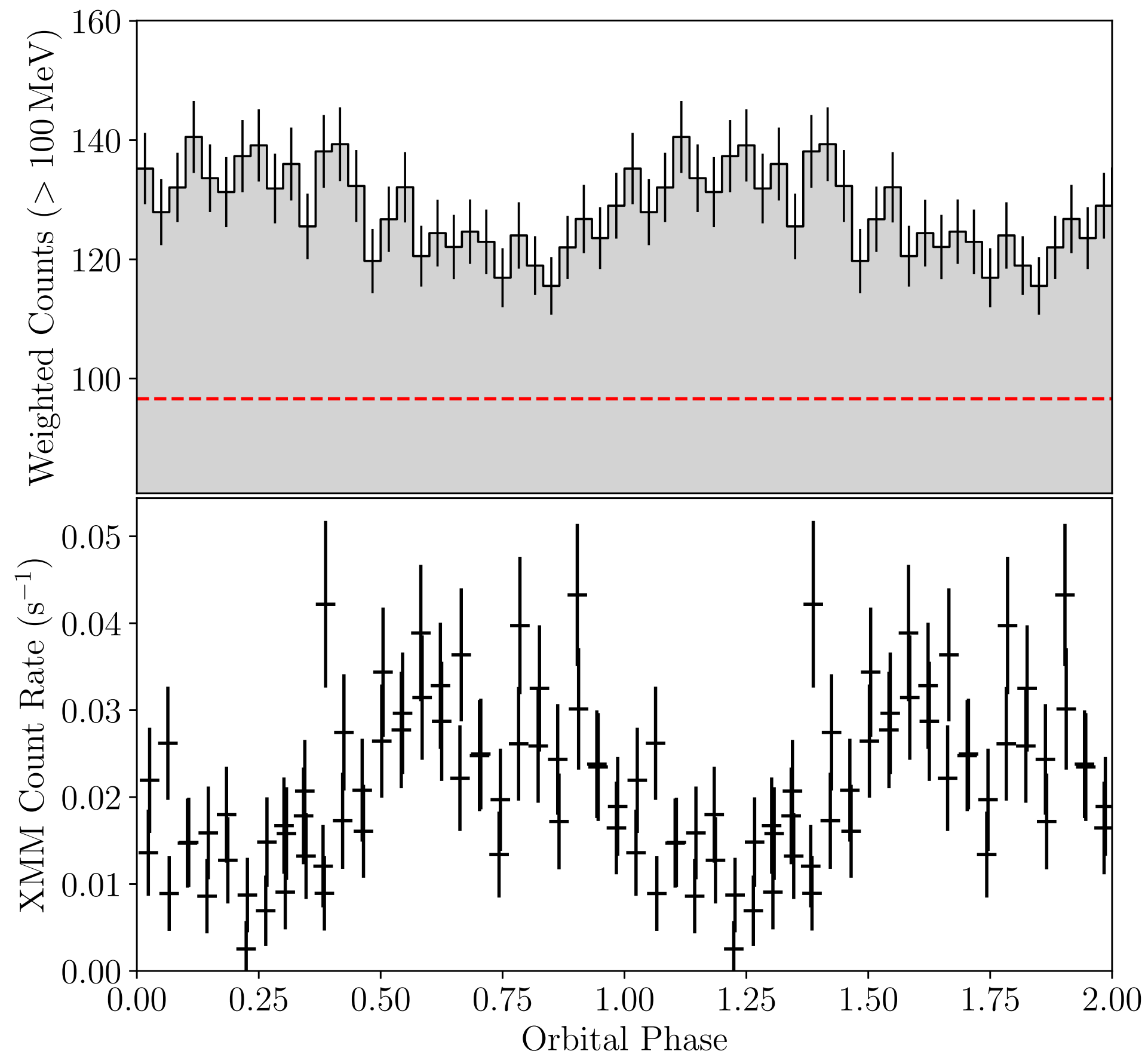
An et al. 2017



Peaks near
pulsar inferior
conjunction

Fermi-LAT Orbital Modulation — Pulse Enhancement

Redback J2039—5617



Pulsed enhancement
near pulsar superior
conjunction

Clark et al. (2021)

Multizone Modeling — Simultaneous spectra and light curves

**Van der Merwe, Wadiasingh, Venter, Harding and Baring;
ApJ 904:91, 2020**

Characteristic Scales

$$a \sim 10^{11} \text{ cm} \quad R_* \sim 0.3a \quad r_{\text{LC}} \sim 10^7 \text{ cm} \sim 10^{-4}a$$

$$T_{\text{comp}} \sim 5000 - 8000 \text{ K}$$

$$B_{\text{w}} \approx \left(\frac{3\dot{E}_{\text{SD}}}{2c} \right)^{1/2} \frac{1}{r_{\text{s}}} = 22 \left(\frac{\dot{E}_{\text{SD}}}{10^{35} \text{ erg s}^{-1}} \right)^{1/2} \left(\frac{10^{11} \text{ cm}}{r_{\text{s}}} \right) \text{ G} \quad B_{\text{s}} \gtrsim B_{\text{s,min}} \approx 4.4 \epsilon_{\text{X,max}}^{1/3} \left(\frac{10^9 \text{ cm}}{r_{\text{L}}} \right)^{2/3} \text{ G}$$

$$\sigma \sim 10^{-5} - 10^{-3} \quad \text{from SED fitting}$$

$$u_{\text{B}} \sim \mathcal{O}(0.1 - 10) \text{ erg cm}^{-3}$$

$$u_{\text{ph}} \sim \mathcal{O}(0.1 - 1) \text{ erg cm}^{-3}$$

$$E_{\text{cut}} \sim 0.1 - 10 \text{ erg} \rightarrow 0.1 - 10 \text{ TeV electrons}$$

Simultaneous Spectra and Orbital Light Curves: Particle Injection and Transport + Beaming and Emission Code in Multiple Zones

Model Assumptions — UMBRELA Code

1. **Hemispherical polar cap** shape for shock surrounding companion (to be relaxed soon).
2. Azimuthal symmetry about line joining pulsar and companion ($d/d\phi = 0$).
3. Steady-state ($d/dt = 0$).
4. Isotropic **black-body emission** at temperature T from companion. IC on companion photons dominates at TeV. SSC is negligible.
5. Approximate particle transport using **timescales (linearization)**.
6. Isotropic steady-state particle spectrum in comoving frame.
7. Bulk flow: linear profile for $\beta\Gamma(\theta)$ (bulk momentum linearly increasing).
8. $\tau_{\gamma\gamma}$ is quite small, even for flaring companions and is neglected for now.

Injection Spectrum

Cut-off Energy:

This is usually the minimum and sets E_{cut}

$$E_{\text{cut}} = \min\{E_{\text{SR RRLA}}, E_{\text{Hillas}}, E_{\text{MSP } \Phi}\}$$

Solid Angle & Diffusion:

$$Q_{\text{PSR}}(E_e) = Q_0 E_e^{-\Gamma} \exp\left(-\frac{E_e}{E_{\text{cut}}}\right)$$

$$Q_1 = \left(\frac{1}{4\pi} \int_0^{2\pi} \int_{\lambda_1}^{\lambda_2} \sin \lambda \, d\lambda \, d\phi\right) Q_{\text{PSR}} = \frac{1}{2} (\cos \lambda_1 - \cos \lambda_2) Q_{\text{PSR}}$$

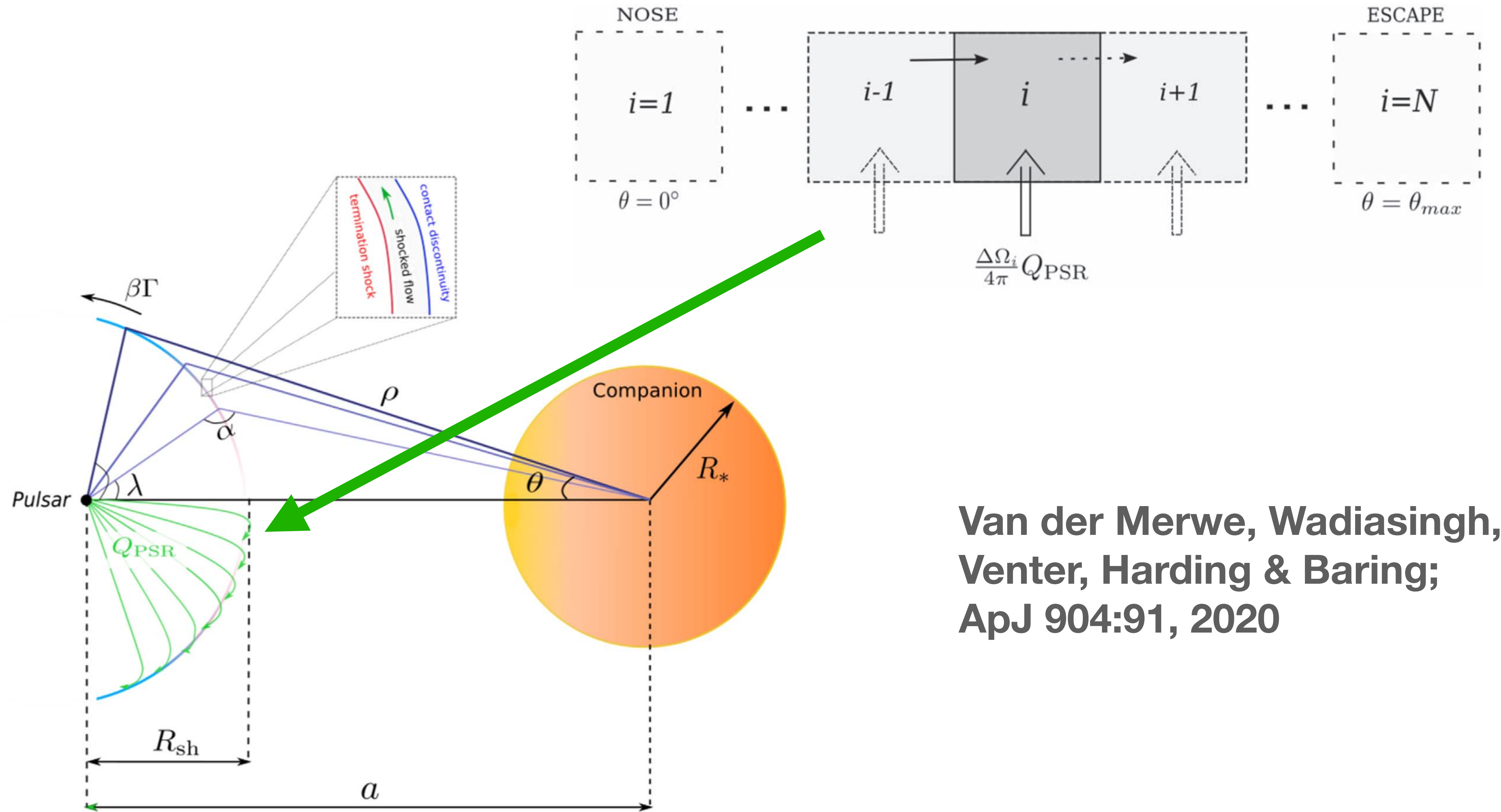
$$Q_i = \frac{1}{t_{\text{diff}}} \frac{dN_{e,i-1}}{dE_e} + \frac{1}{2} (\cos \lambda_i - \cos \lambda_{i+1}) Q_{\text{PSR}}, \quad i > 1$$

Normalization - Current and Energetics:

$$\dot{N}_{\text{GJ}} = \frac{B_{\text{PSR}} 4\pi^2 R_{\text{PSR}}^3}{2ceP^2} \quad \dot{N}_{\text{II}} = M_{\pm} \dot{N}_{\text{GJ}}$$

$$\int_{E_{\text{min}}}^{\infty} Q_{\text{PSR}} \, dE_e = (M_{\pm} + 1) \dot{N}_{\text{GJ}} \quad \int_{E_{\text{min}}}^{\infty} E_e Q_{\text{PSR}} \, dE_e = \eta_p \dot{E}_{\text{rot}}$$

Model Schematic



Van der Merwe, Wadiasingh,
Venter, Harding & Baring;
ApJ 904:91, 2020

Particle Transport (Boltzmann or Convection-Diffusion Equation)

$$\frac{\partial N_e}{\partial t} = -\vec{V} \cdot (\vec{\nabla} N_e) + \kappa(E_e) \nabla^2 N_e + \frac{\partial}{\partial E_e} (\dot{E}_{e,\text{tot}} N_e) - (\vec{\nabla} \cdot \vec{V}) N_e + Q$$

➔ $N_e = Q \tau_{\text{eff}} \quad \tau_{\text{eff}}^{-1} = \tau_{\text{ad}}^{-1} + \tau_{\text{diff}}^{-1} + \tau_1^{-1} + \tau_2^{-1} + \tau_{\text{rad}}^{-1}$

$$\tau_{\text{ad}} = \frac{3R_0}{c} \left[\frac{\partial \beta}{\partial \theta} + \beta \cot \theta \right]^{-1} \quad \tau_{\text{rad}} = \frac{E_e}{\dot{E}_{e,\text{rad}}}$$

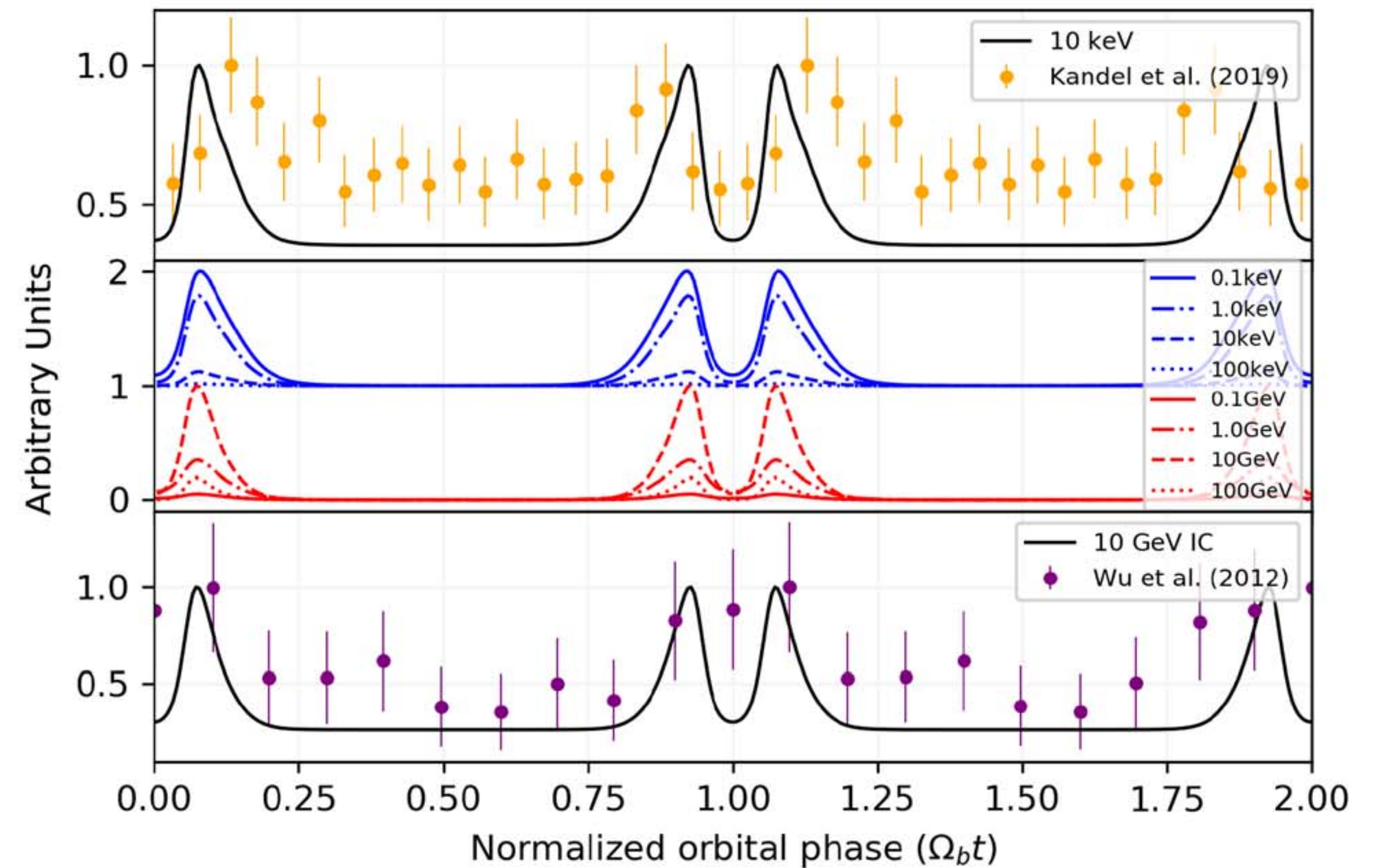
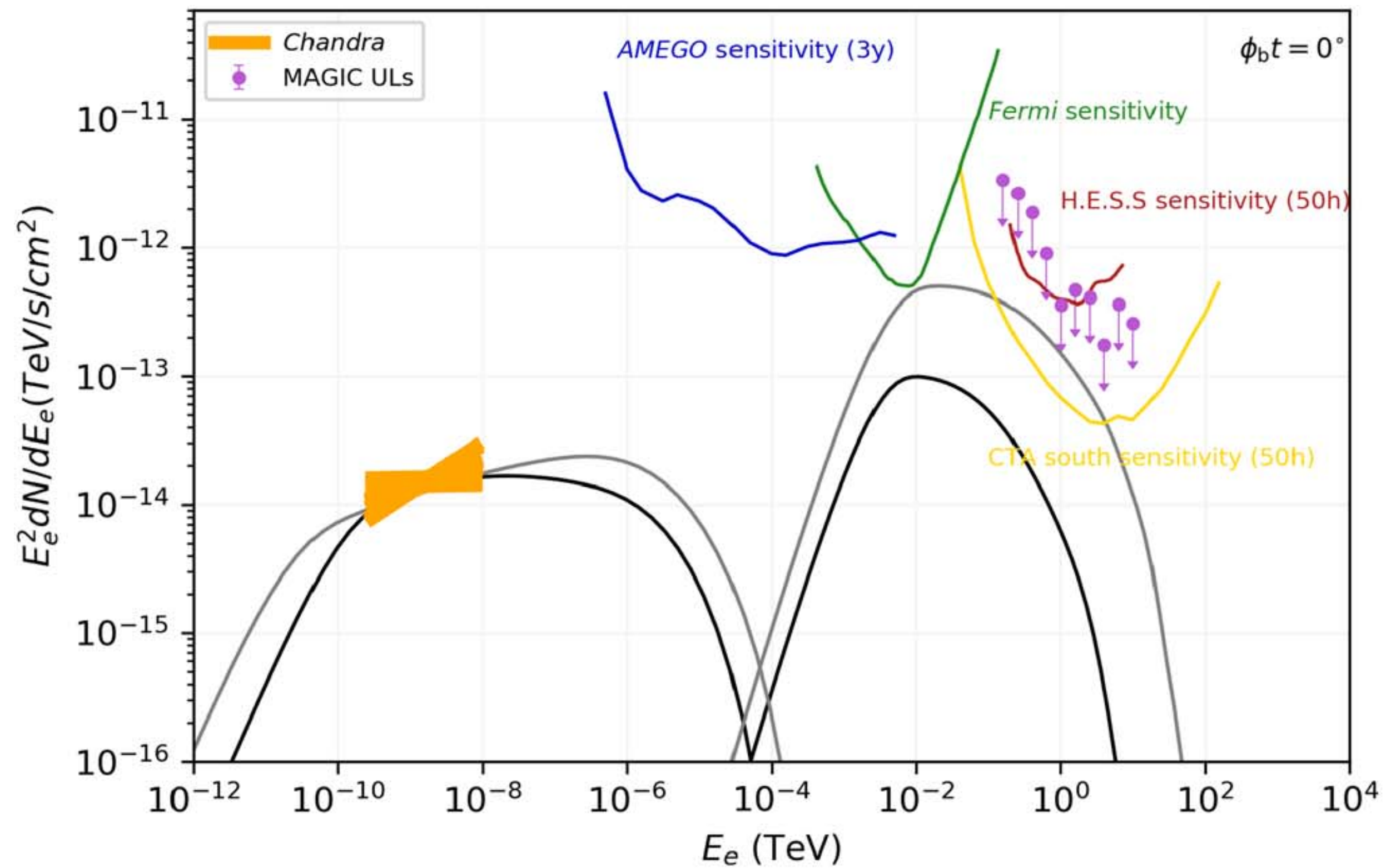
$$\tau_1 = \frac{R_0}{c \beta \tan \theta} \quad \tau_2 = \frac{\tau_{\text{ad}}}{3} \quad \tau_{\text{diff}} = \frac{R_0^2}{2\kappa}$$

Convection almost always dominates τ_{eff} but Doppler boosting compensates

Some Results

Models

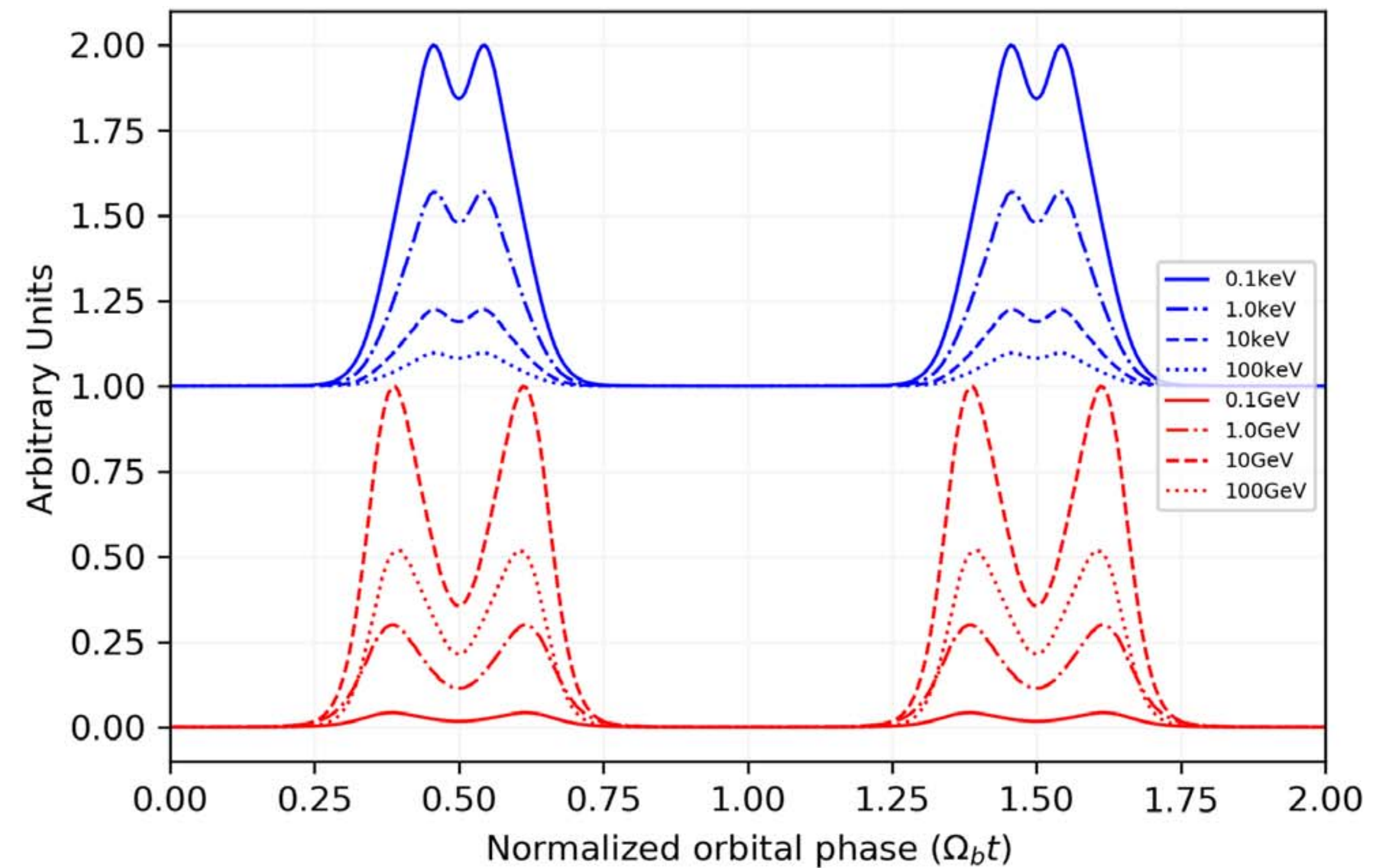
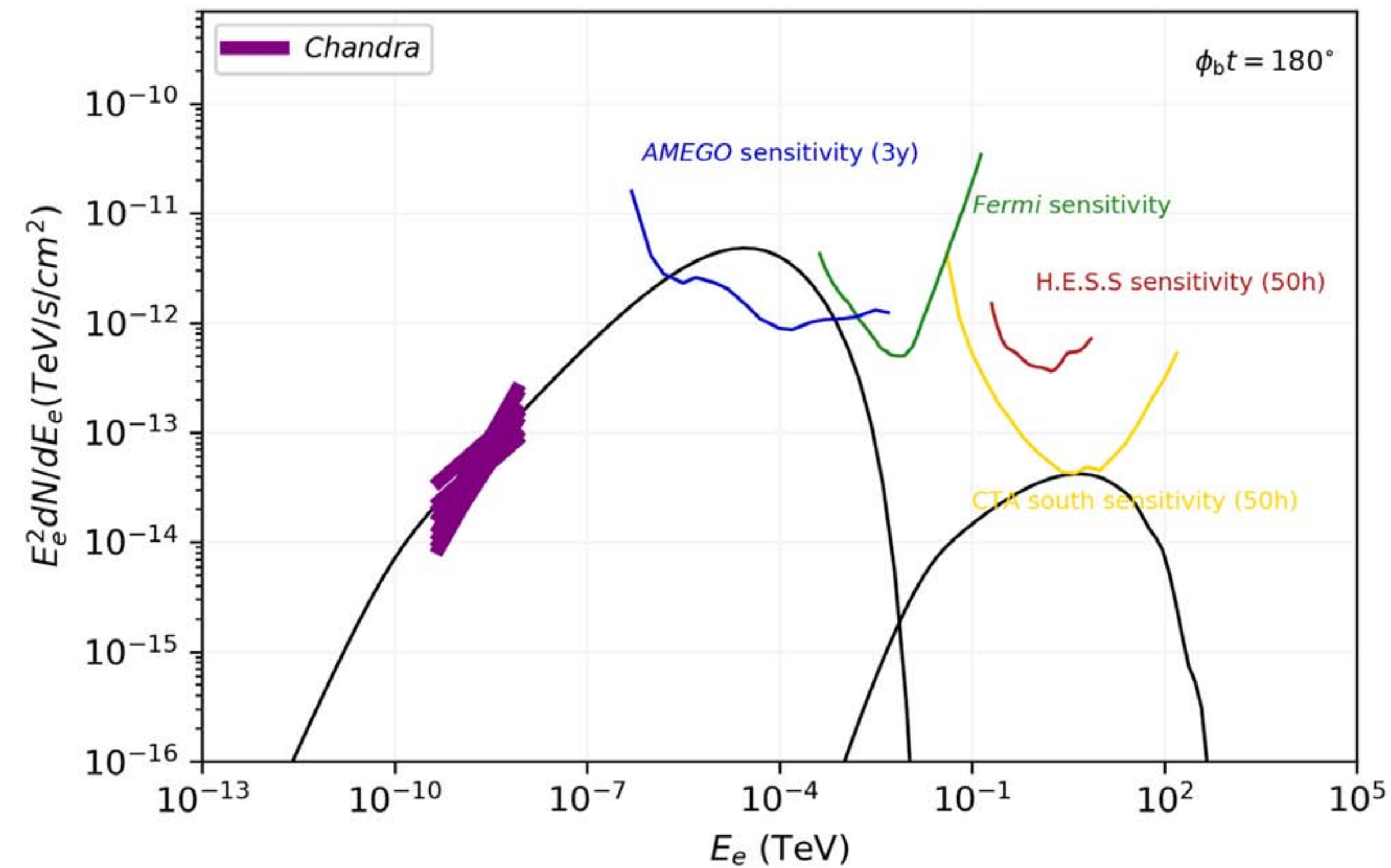
Case Study Black Widow B1957+20



Van der Merwe, Wadiasingh, Venter, Harding & Baring;
ApJ 904:91, 2020

Models

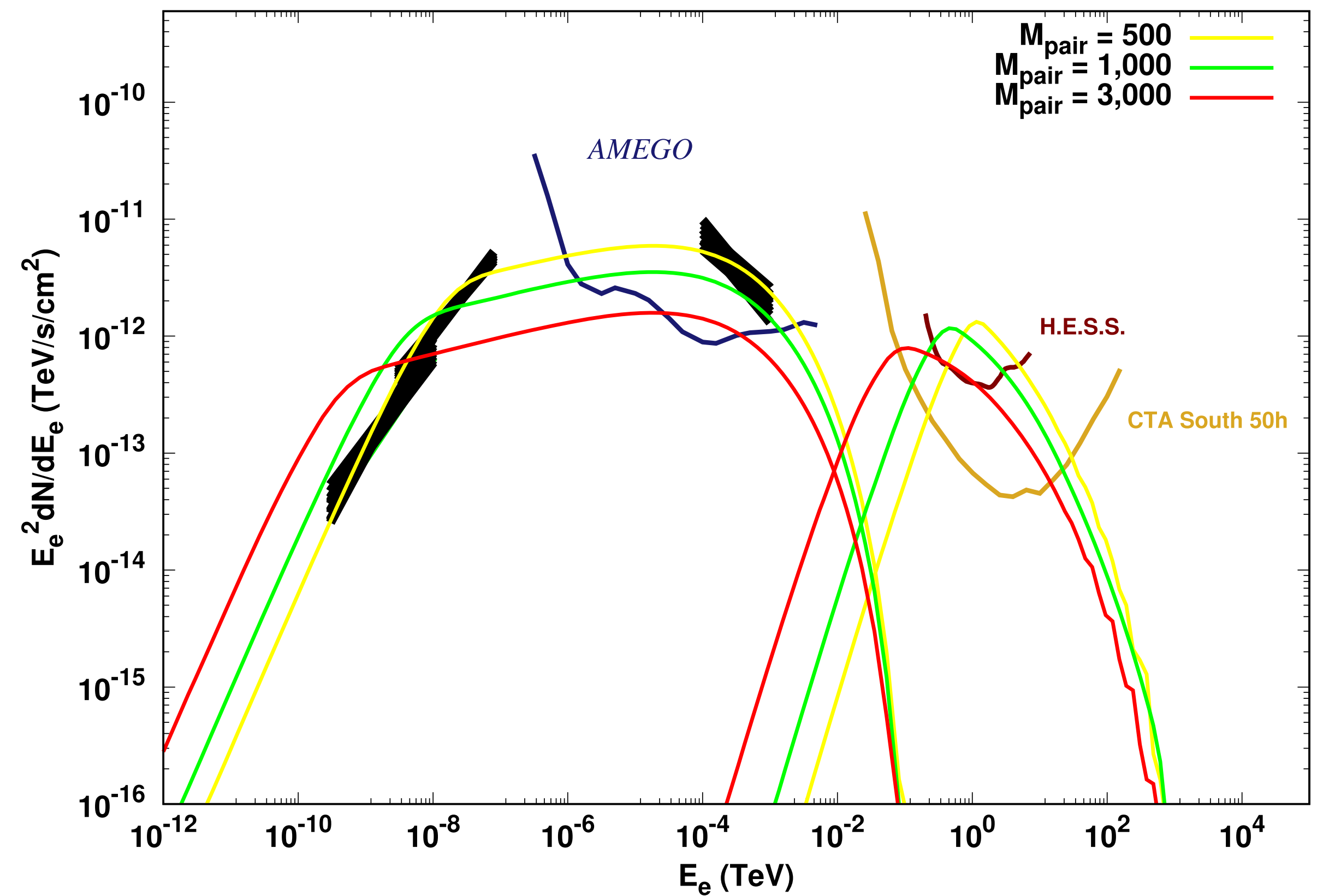
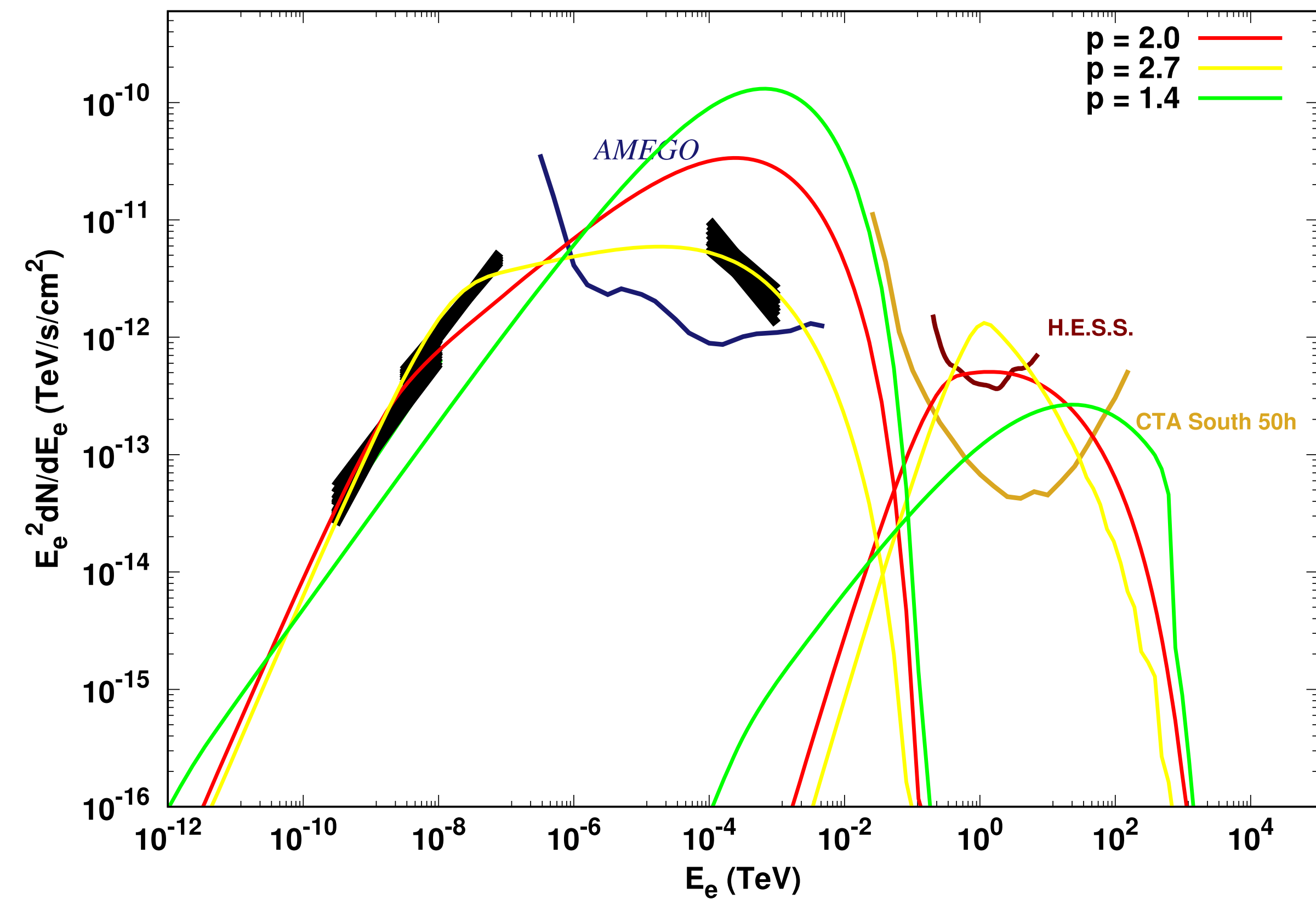
Case Study Redback J2339–0533



Van der Merwe, Wadiasingh, Venter, Harding & Baring;
ApJ 904:91, 2020

Model SEDs - varying injection

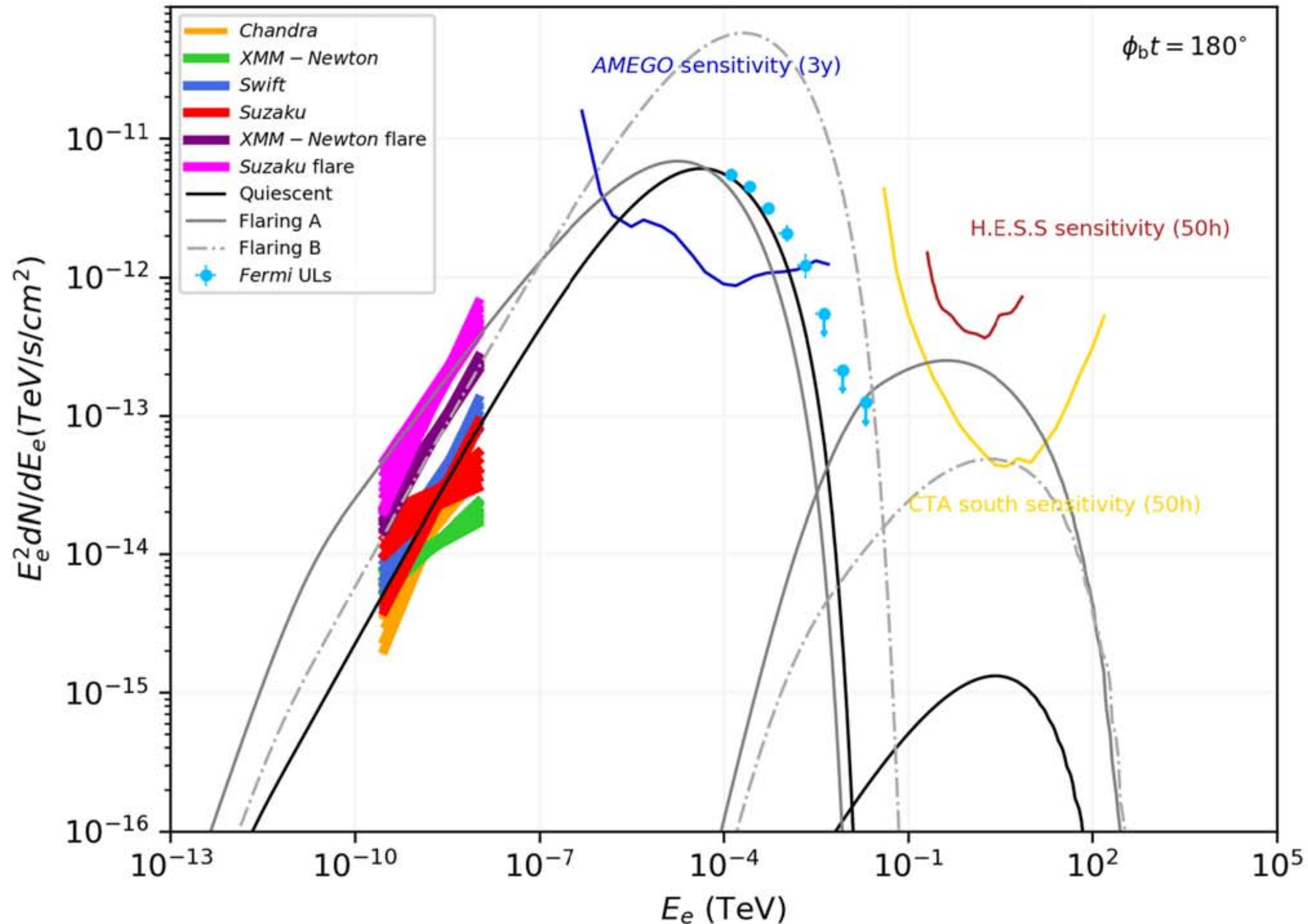
Case Study Redback J1723-2837



Van der Merwe, Wadiasingh, Venter, Harding & Baring;
ApJ 904:91, 2020

Model SEDs - Flaring States

Case Study Black Widow J1311-3430



Van der Merwe,
Wadiasingh, Venter,
Harding & Baring;
ApJ 904:91, 2020

Table 1
Model Parameters for Illustrative Cases

		B1957+20 (A)	B1957+20 (B)	J1723–2837 (Black)	J1723–2837 (Gray)	J2339–0533	J1311–3430 Quiescent (Flaring)
Parameters	Symbols	Values					
Orbital separation ^a	a ($\times 10^{11}$ cm)	1.95	1.95	2.90	2.90	1.25	0.597
Orbital period	P_b (hr)	9.17	9.17	14.8	14.8	4.6	1.56
Mass ratio	q	70	70	3.5	3.5	18.2	180
Pulsar mass	M_{psr} (M_{\odot})	1.7	1.7	1.7	1.7	1.7	1.7
Pulsar radius	R_{psr} ($\times 10^6$ cm)	1.0	1.0	1.0	1.0	1.0	1.0
Pulsar period	P (ms)	1.60	1.60	1.86	1.86	2.89	2.56
Pulsar period derivative	\dot{P} ($\times 10^{-20}$ s s ⁻¹)	1.7	1.7	0.75	0.75	1.4	2.1
Moment of inertia of pulsar	I ($\times 10^{45}$)	1.0	1.0	1.0	1.0	1.0	1.0
Inclination angle	i (deg)	65	85	40	40	54	60
Distance	d (kpc)	1.40	1.40	0.93	0.93	1.10	1.4
Companion temperature	T_{comp} (K)	8500	8500	6000	6000	6000	12,000 (45,000)
Shock radius	R_{sh}/a	0.4	0.2	0.4	0.4	0.3	0.4
Magnetic field at shock	B_{sh} (G)	1.2	7.0	0.8	0.8	0.8	1.0 (1.2)
Pair multiplicity	M_{pair}	9000	9000	400	2000	500	600 (3000)
Maximum particle conversion efficiency	η_p	0.6	0.8	0.9	0.8	0.8	0.8 (0.9)
Acceleration efficiency	$\epsilon_{\text{acc}} = r_g/\lambda$	0.001	0.001	0.08	0.001	0.01	0.1 (0.01)
Index of injected spectrum	p	2.5	2.4	2.5	1.4	1.8	1.4 (1.8)
Bulk flow momentum	$(\beta\Gamma)_{\text{max}}$	4.0	5.0	6.0	7.0	7.0	5.0 (8.0)
Maximum shock angle	θ_{max}	61	68	60	50	55	65 (60)

Note.

^a This is a derived value using $a = (GM_{\text{NS}}M_{\text{comp}}P_b^2(1 + q)/4\pi^2q)^{1/3}$.

Conclusion

- Millisecond pulsar binaries are a growing in number and are “clean” systems for understanding pulsars and pulsar winds
- We have a new multizone code which can predict SR and IC fluxes, or energy-dependent orbital modulation
- This constrains pulsar injection and particle acceleration parameters by anchoring on the X-ray
- SEDs should peak in the MeV and TeV — some (all?) of spiders could be “gamma-ray binaries”
- Exciting for CTA and AMEGO (or any other sensitive MeV telescopes)
- IACTs particularly suited for time inverse Compton variability associated with flaring companions