



The study of the longitude development of muons in air shower

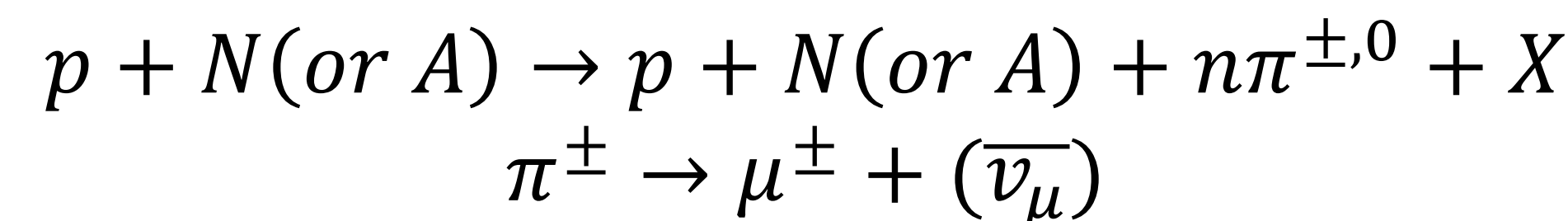
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Introduction

Muon introduction

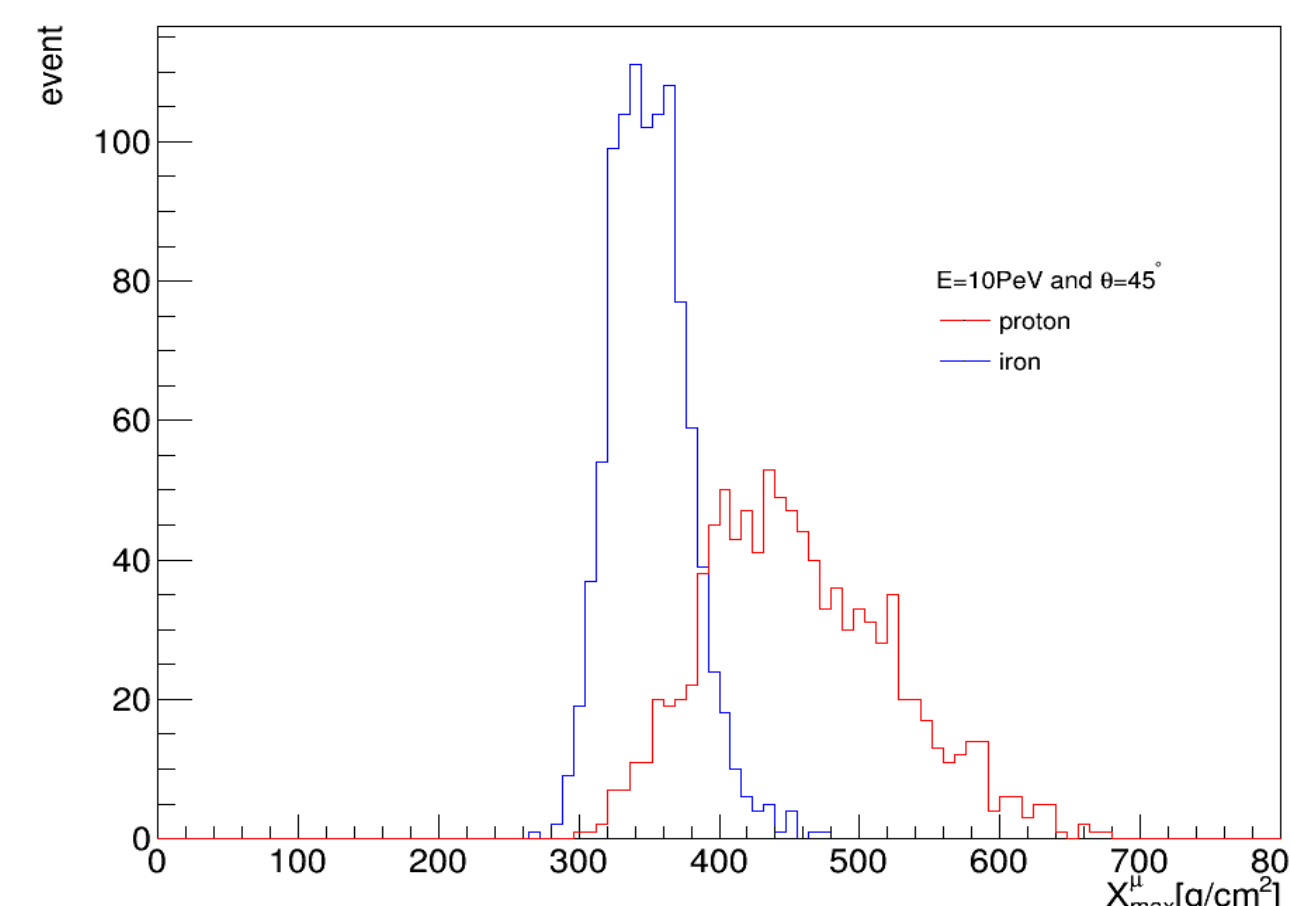
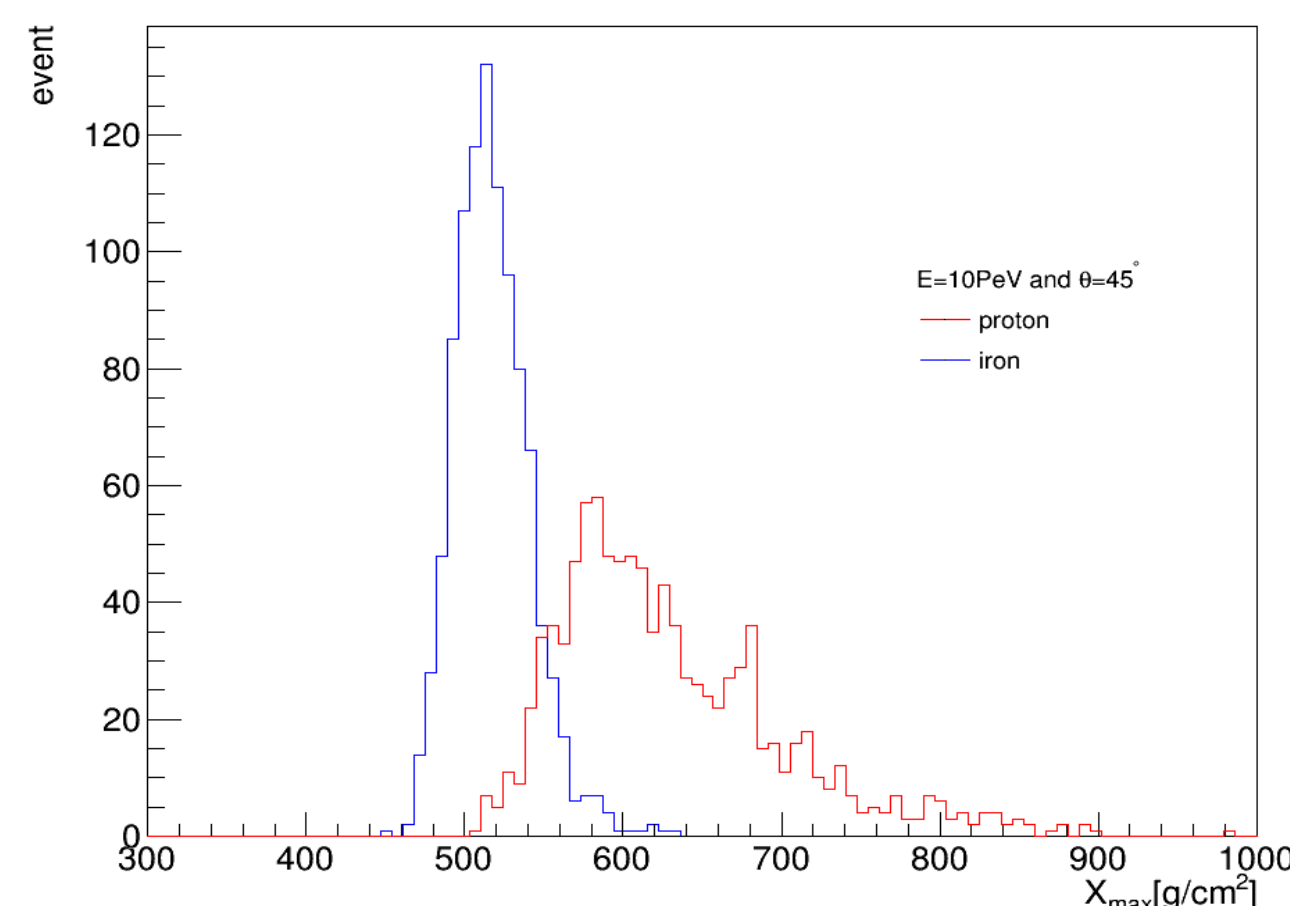
1. The main contributors to the muon component in air showers are charged pions (π^+ , π^-) and kaons (K^+ , K^- , K_L^0), but also charmed particles, such as $D^\pm$, D^0 , J/ψ and others



2. Longitude development of muons preserves the information of primary particles and plays an important role in the study of composition identification with energy 10^{15} eV- 10^{16} eV.

Purpose to study Muon

- Measure the cosmic ray energy spectrum and mass composition around knee region
- Helps to study the hadronic interaction model
- Provide insight on whether new physics phenomena take place



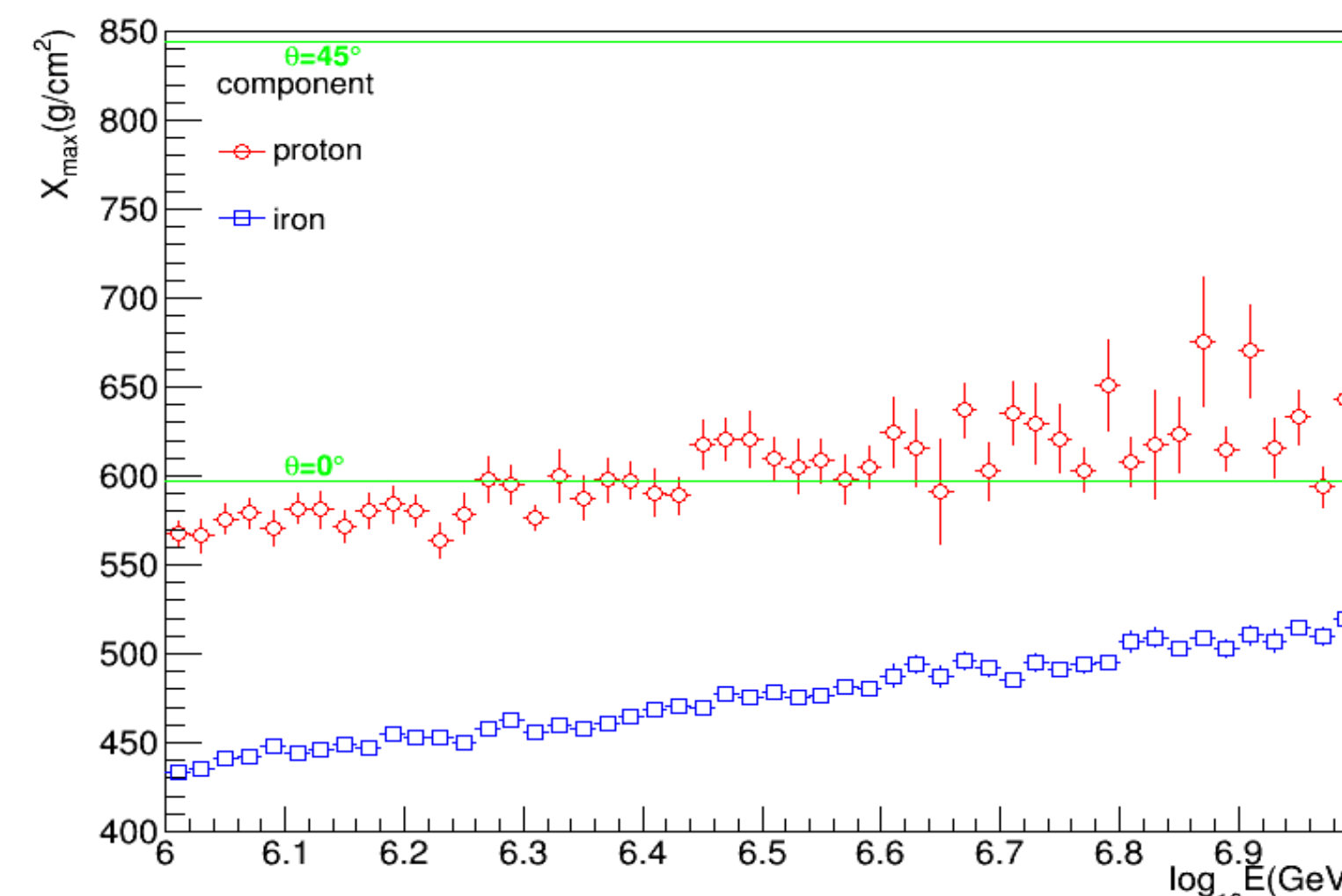
X_{max} : the air depth of the shower maximum development

X_{max}^{μ} : the maximum of the longitudinal profile of the muon production rate

X_{max}^{μ} can be used to identify mass compositions of cosmic rays.

Air shower simulation

- Simulation with CORSIKA (v76400)
- EPOS-LHC, QGSJETII-04
- Zenith angle(θ): fixed 45°
- Altitude: 4410m ($X = 600 g/cm^2$)
- Energy: 10PeV; 5PeV; 1PeV



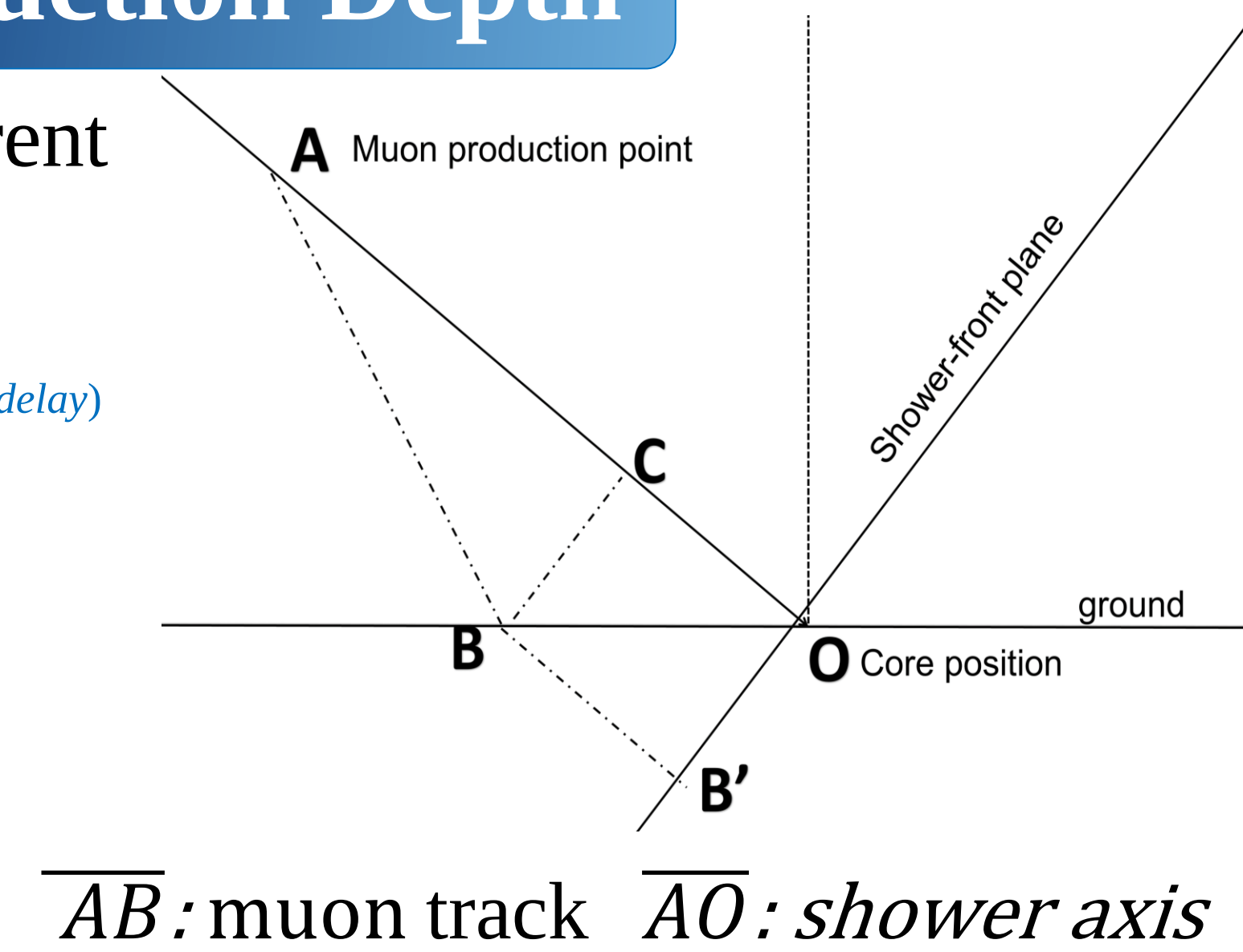
Y axis shows X_{max} , X axis shows $\log_{10}(E)$; green lines are air depth on ground with $\theta=0^\circ$ and $\theta=45^\circ$

In order to ensure the shower full development, the zenith angle is selected as 45°

Reconstruction of Muon Production Depth

- Correction by the path traveled by the parent mesons: $t_{\pi} \sim 3ns$
- Considering geometric delay as: $t_g^{(geometric\ delay)}$
- $\overline{AB} = \sqrt{\overline{BC}^2 + (\overline{AO} - \overline{BB'})^2}$
- $\overline{AB} = \overline{AC} + c \times t_g$

$$\overline{AO} = \frac{1}{2} \left(\frac{\overline{BC}^2}{c \times (t_g)} - c \times (t_g) \right) - c \times t_{\pi}$$



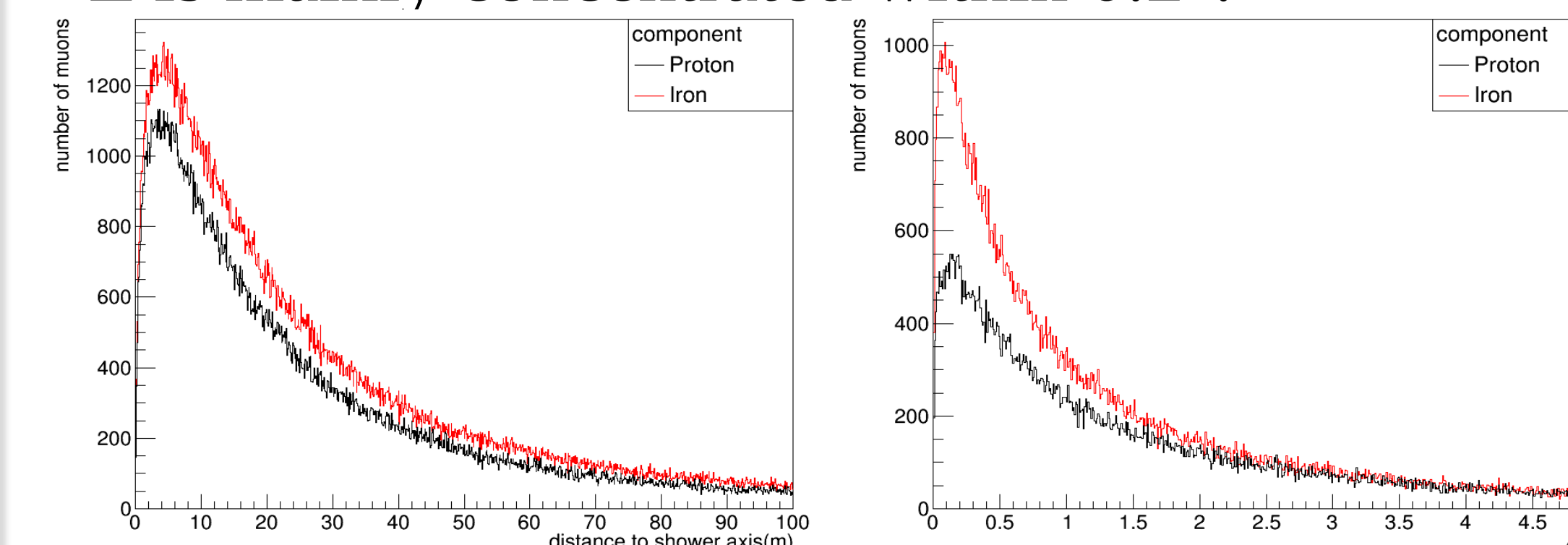
$\overline{AB}$: muon track $\overline{AO}$: shower axis

Muon propagation

- **Approximation I: The muons are produced on the shower axis**

* production point of most muons is confined to a cylinder with a radius of 10m

* Δ is mainly concentrated within 0.2° .



(Left) distributions of the perpendicular distance from the production point of muons to the shower axis
(Right): the difference of the direction of the muon between the production and incidence at the ground.

- **Approximation II: Muons travel in straight lines at the speed of light c**

* $t_B + t_{Rem} < t_{total} \times 10\%$ when $r > 400m$

* t_g is the dominated when $r > 400m$

r : distance from muon position on ground to core on SFP

t_{total} : total time delay

t_g : geometric delay

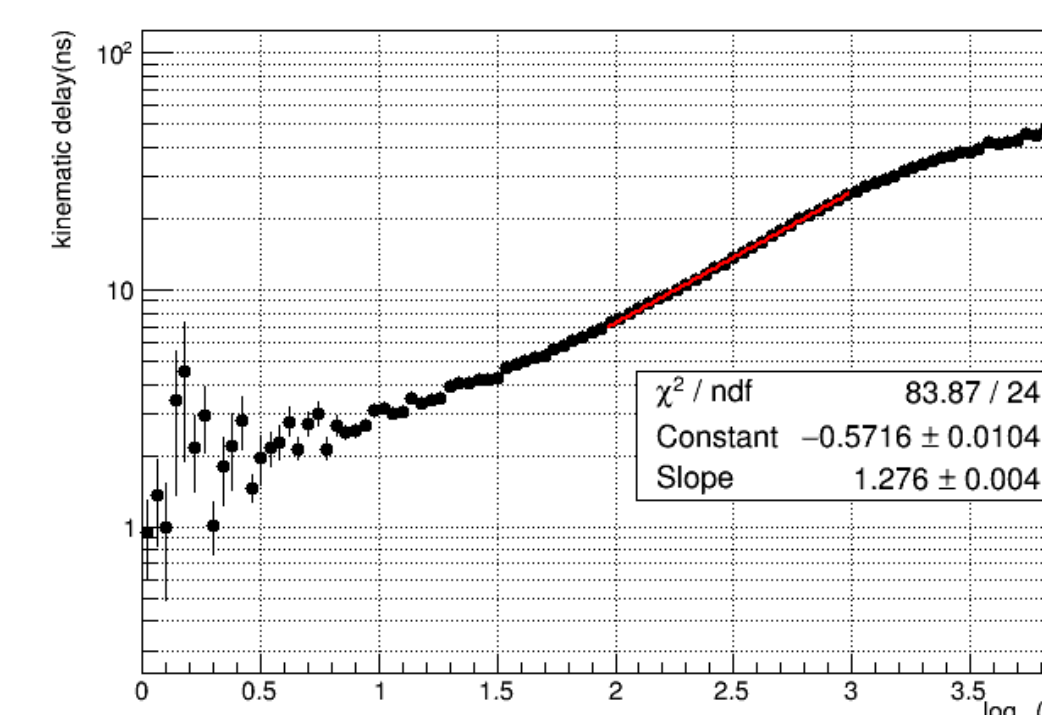
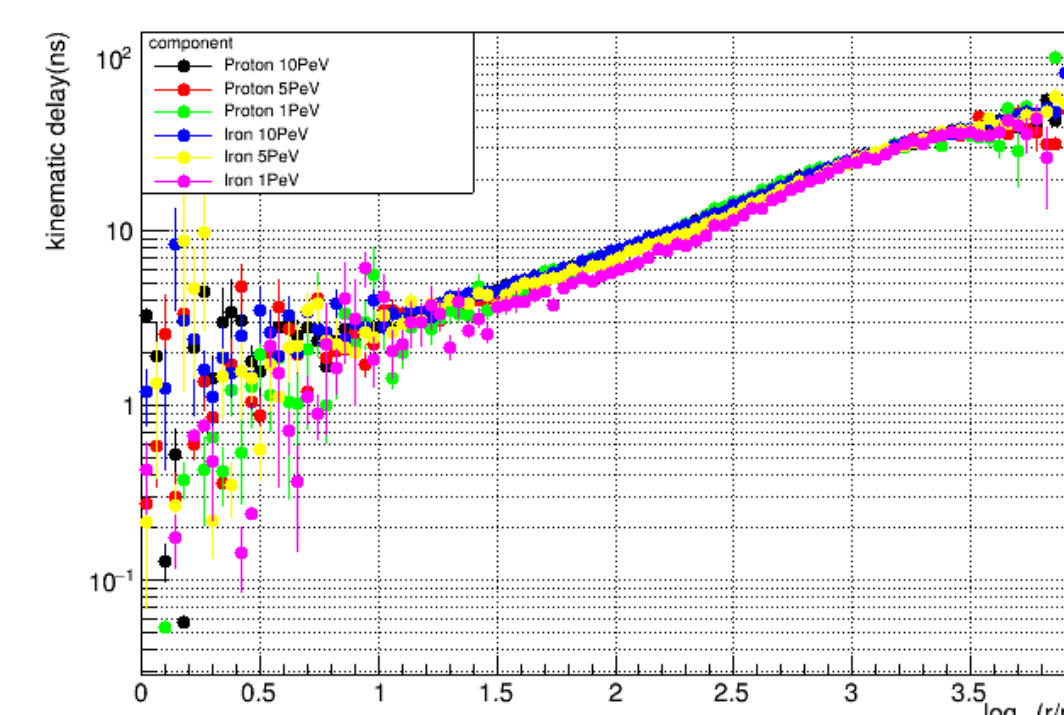
t_{ϵ} : kinematic delay

t_B : geomagnetic delay

t_{Rem} : multiple scattering

- **Approximation III: $t_g = t_{total} - t_{\epsilon}$**

Average time delay for different contribution to the total delay



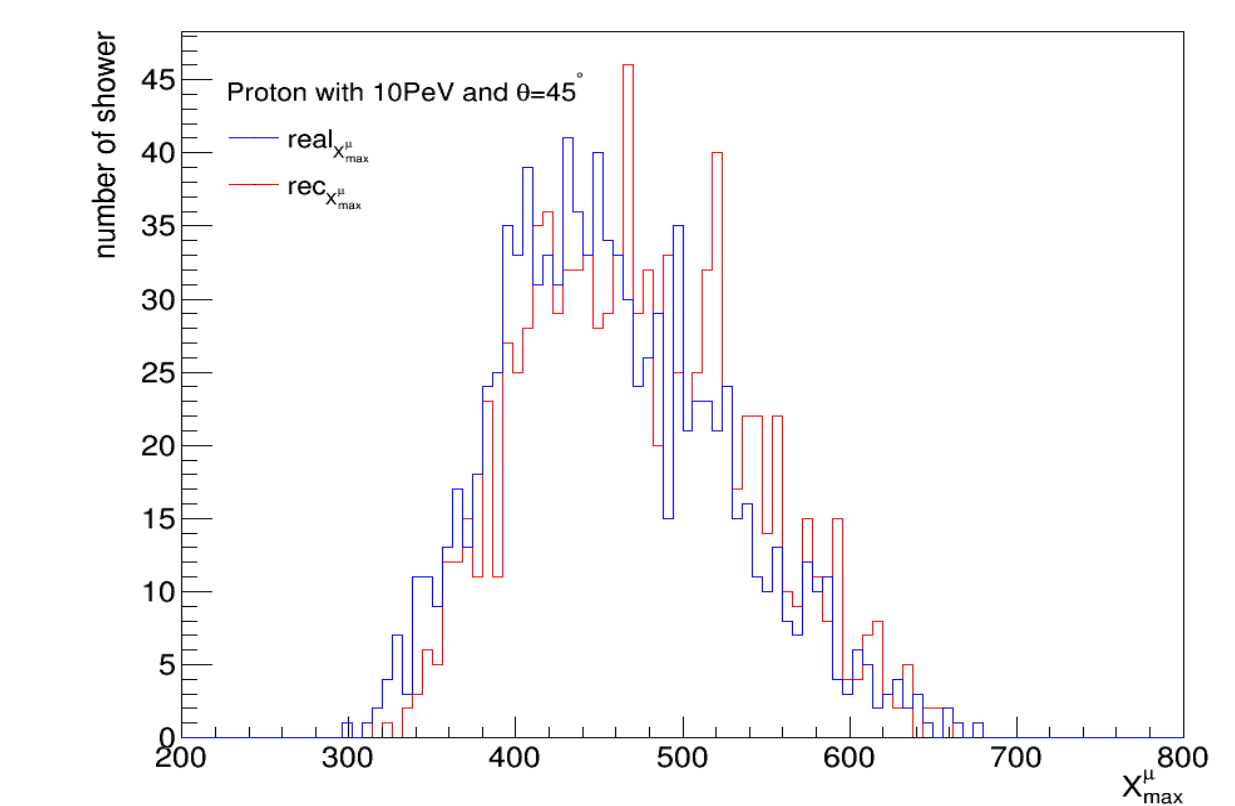
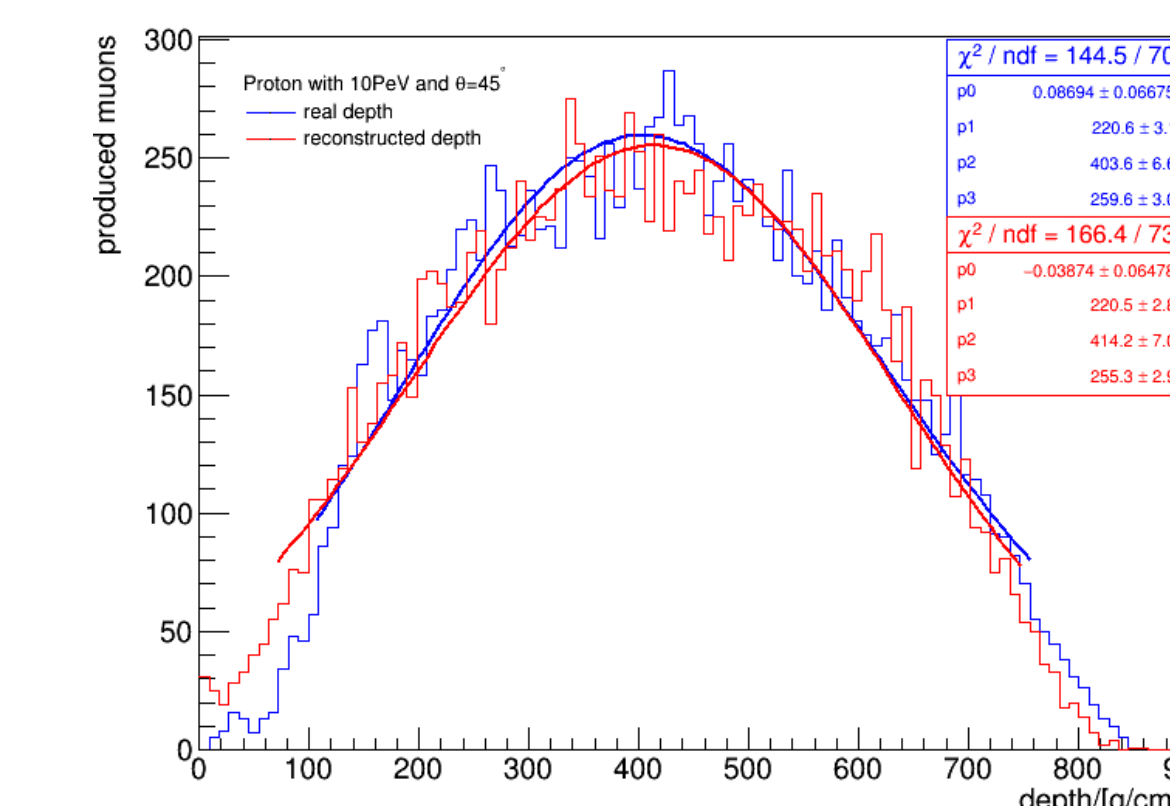
kinematic time delay distributions for showers with different compositions and energies can be fitted with an exponential function:

$$t_{\epsilon} = \exp(-0.57 + 1.276 \times \log_{10}(r))$$

Features of the muon profiles

Fit the longitudinal profile of the muon

Profile meet: ① 10 ns time resolution is considered ② $400m < r < 1000m$ ③ Muon energy $> 1GeV$



(Left): distributions of muon real production depth(blue) and muon reconstructed production depth(red) of a shower initiated by a proton with $E=10^{16}eV$ and $\theta=45^\circ$

(Right): distributions of real X_{max}^{μ} and reconstructed X_{max}^{μ} for 1000 showers initiated by protons with $E=10^{16}$ eV and $\theta=45^\circ$

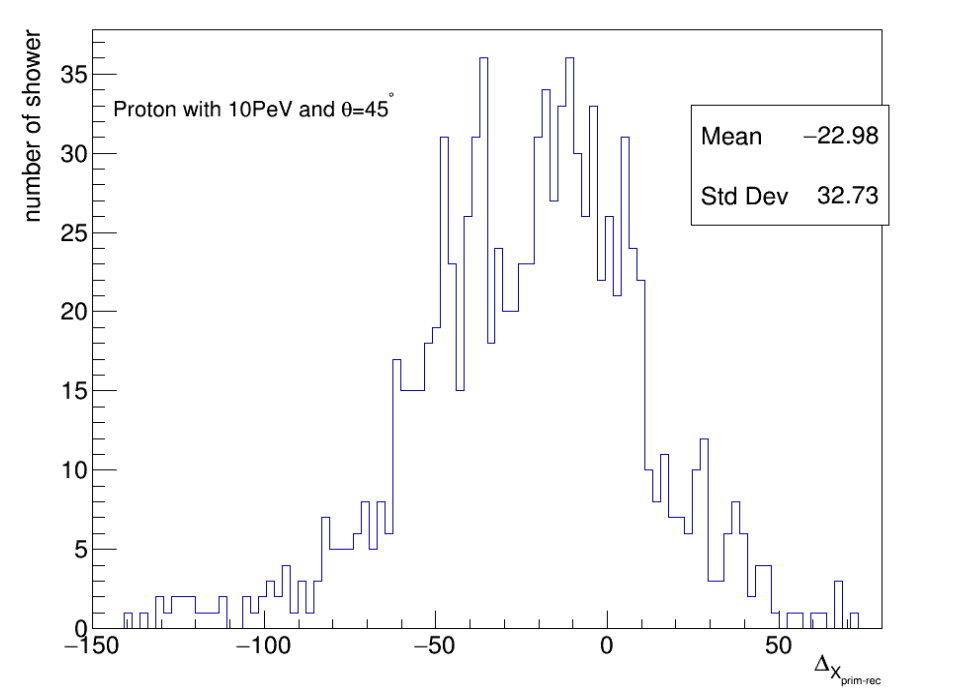
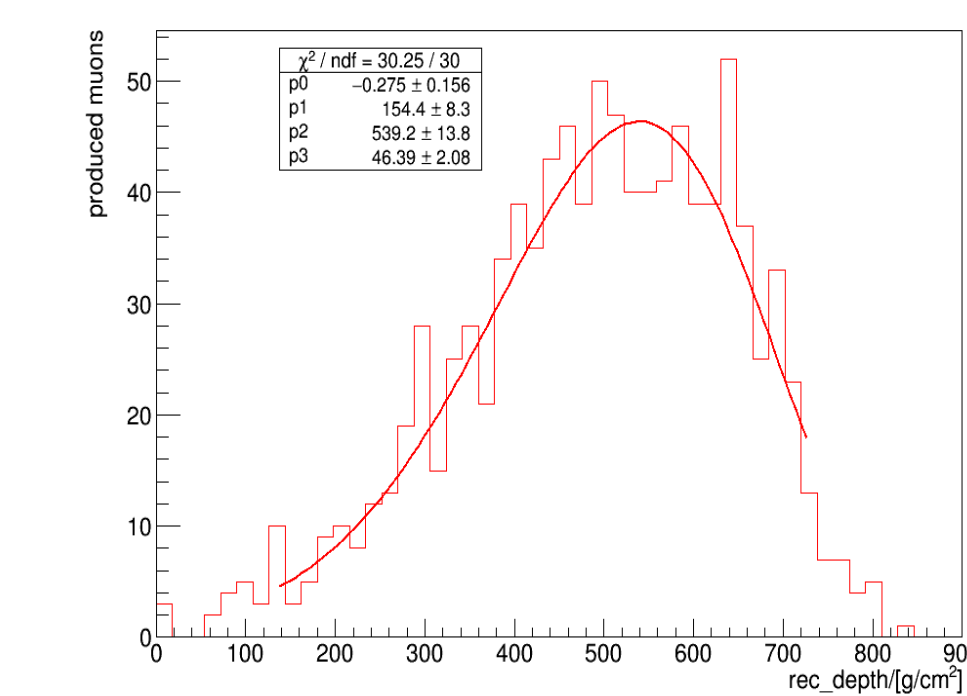
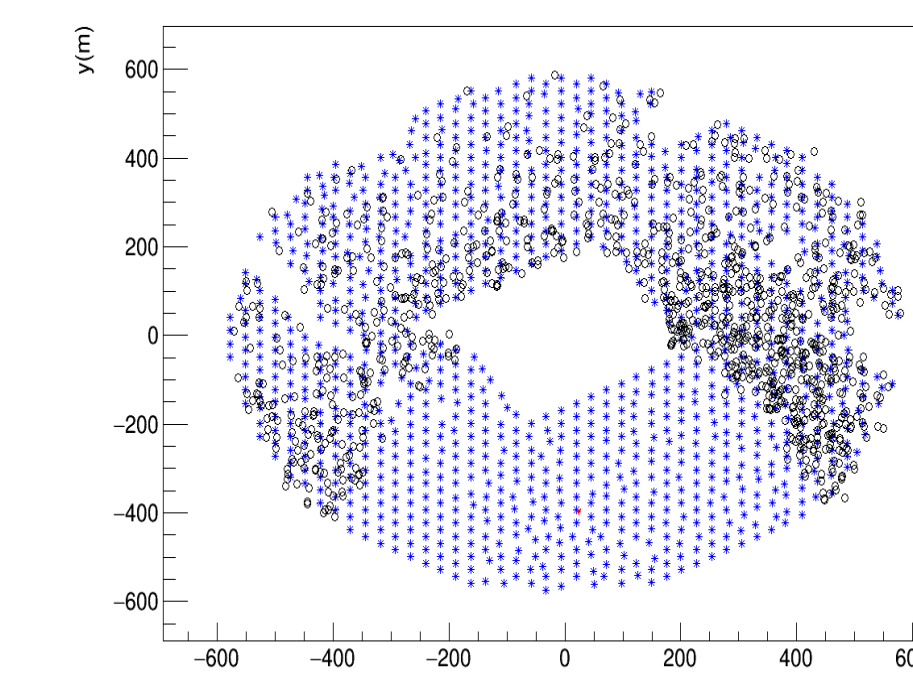
$$\text{Fit formula: } \frac{dN}{dX} = (1 + \frac{R}{L}(X - X_{max}^{\mu}))^{R-2} \exp\left(-\frac{X - X_{max}^{\mu}}{LR}\right)$$

✓ The reconstructed X_{max}^{μ} is close to the real X_{max}^{μ}

Consider the sampling of MD

* The configuration of muon detectors of LHAASO used [3]

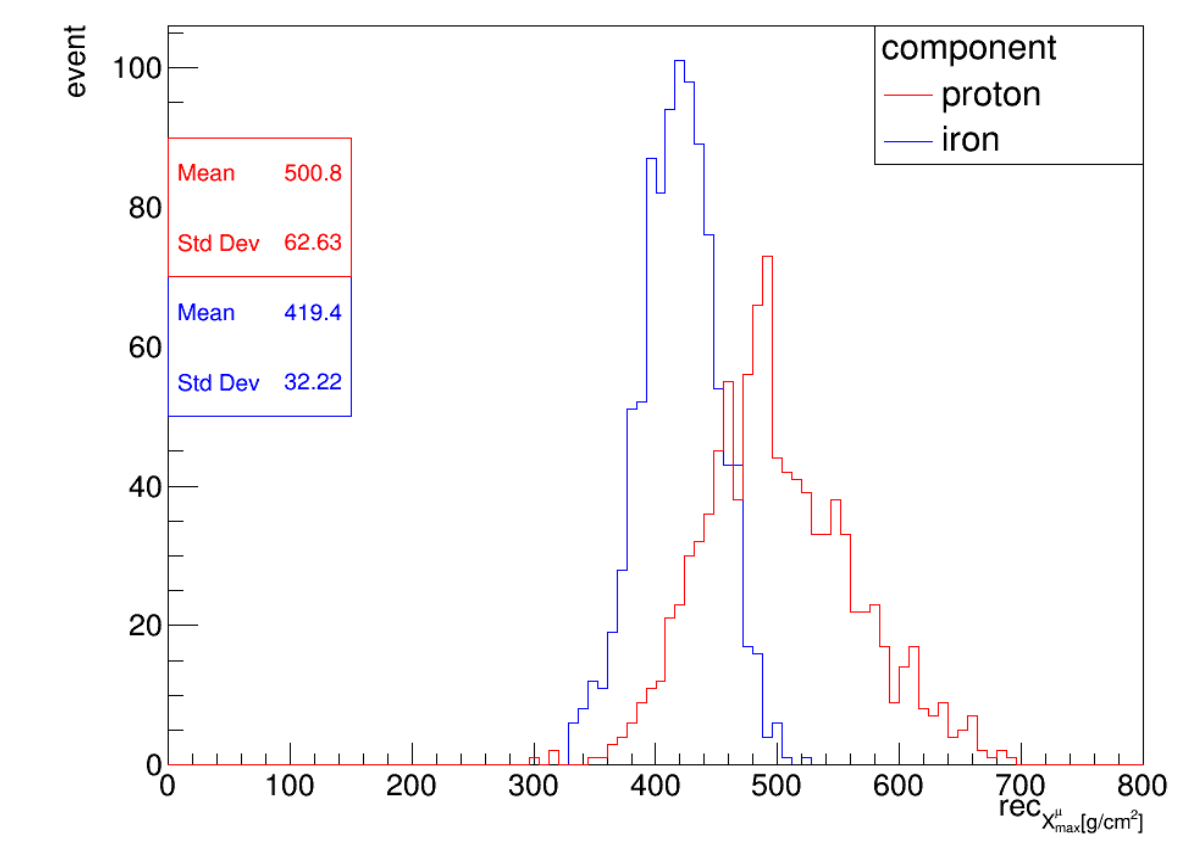
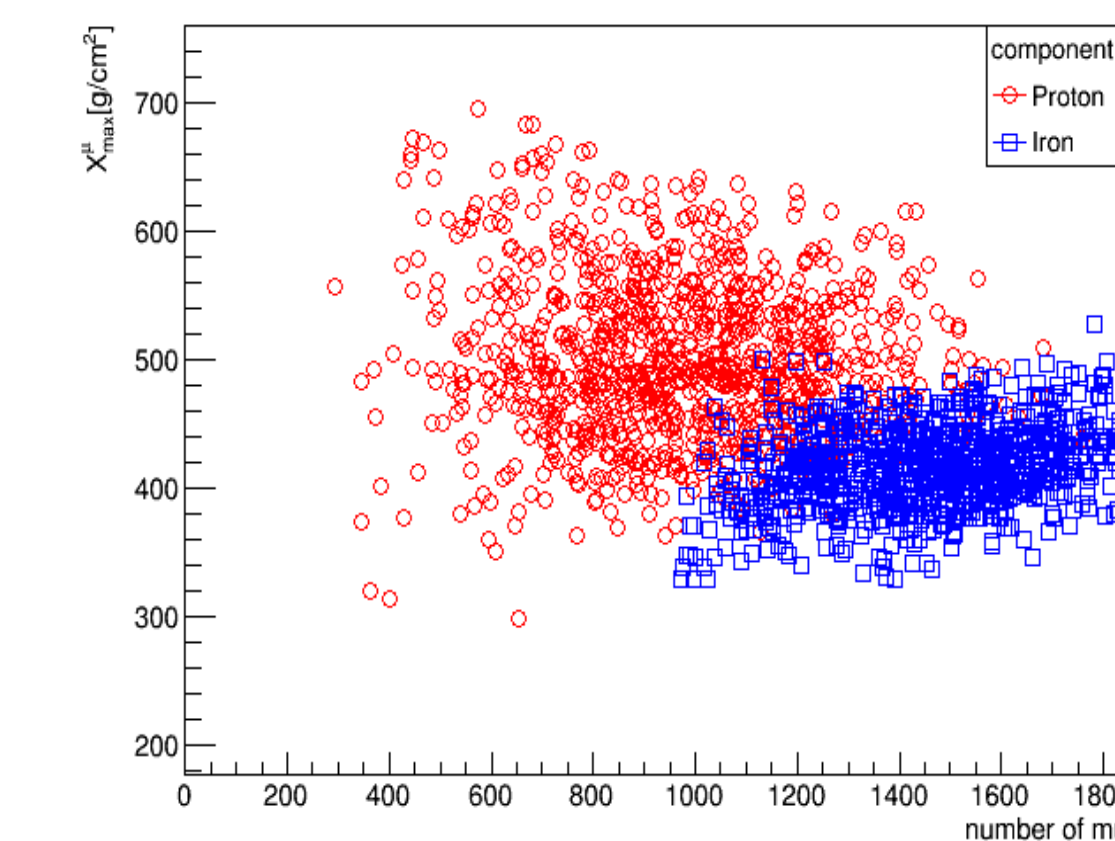
Sampling criteria: ① 10 ns time resolution ② $r > 400m$ ③ Muon energy $> 1GeV$ ④ MD array



(Left) Distribution of muons on muon detectors(black); muon detectors distribution(blue); core position(red)

(Center) Distribution of muon reconstructed production depth of a shower initiated by proton with $E=10^{16}$ eV and $\theta=45^\circ$

(Right): Distribution of real X_{max}^{μ} - reconstructed X_{max}^{μ} for 1000 showers initiated by protons with $E=10^{16}$ eV and $\theta=45^\circ$



(Left): Y axis: $rec_{X_{max}^{\mu}}$; X axis: number of muons; showers initiated by protons and irons with $E=10^{16}$ eV and $\theta=45^\circ$

(Right): Distributions of $rec_{X_{max}^{\mu}}$ of showers initiated by protons and irons with $E=10^{16}$ eV and $\theta=45^\circ$

- ✓ X_{max}^{μ} can be reconstructed with resolution $32g/cm^2$ by muon detectors (like LHAASO)
- ✓ X_{max}^{μ} can be used to identify mass compositions of cosmic rays
- ✓ Correlation between numbers of muon and X_{max}^{μ} is weak

Summary