



# The Theory of Efficient Particle Acceleration at Shocks

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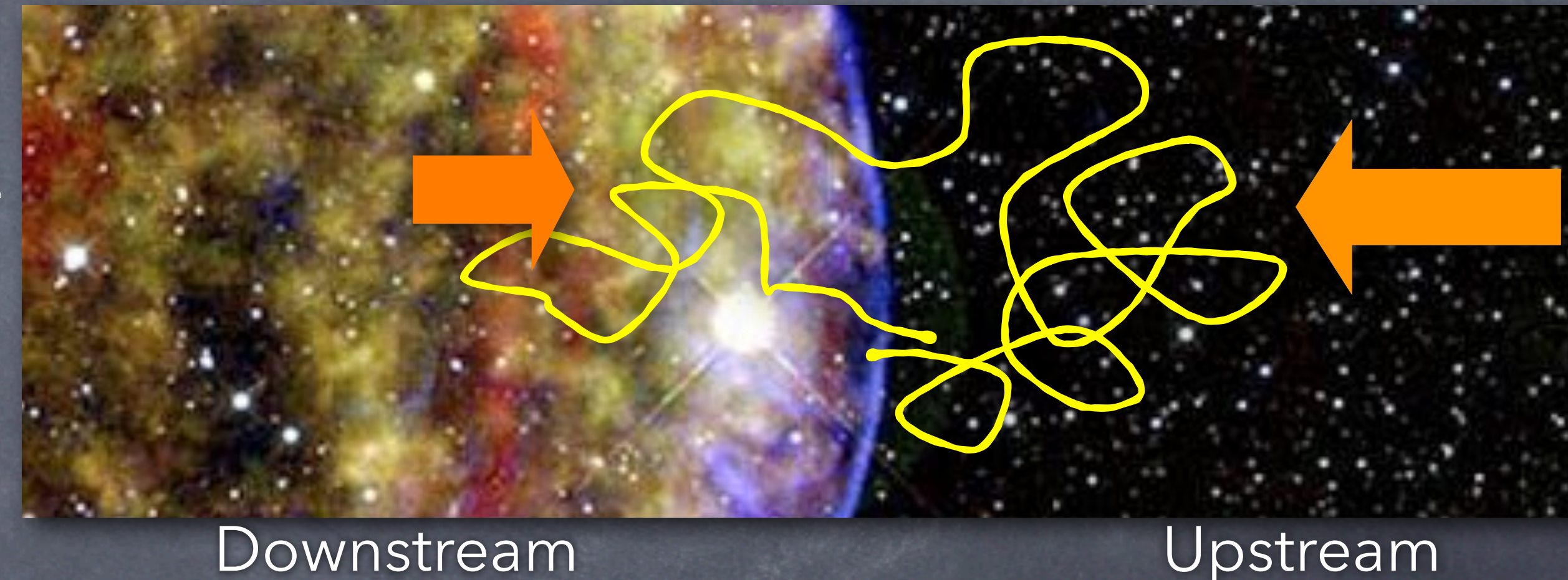
# The SNR paradigm for the origin of CRs

• **Energetics:** ~10% of SN kinetic energy can account for Galactic CRs (Baade-Zwicky34)



SN in NGC4526

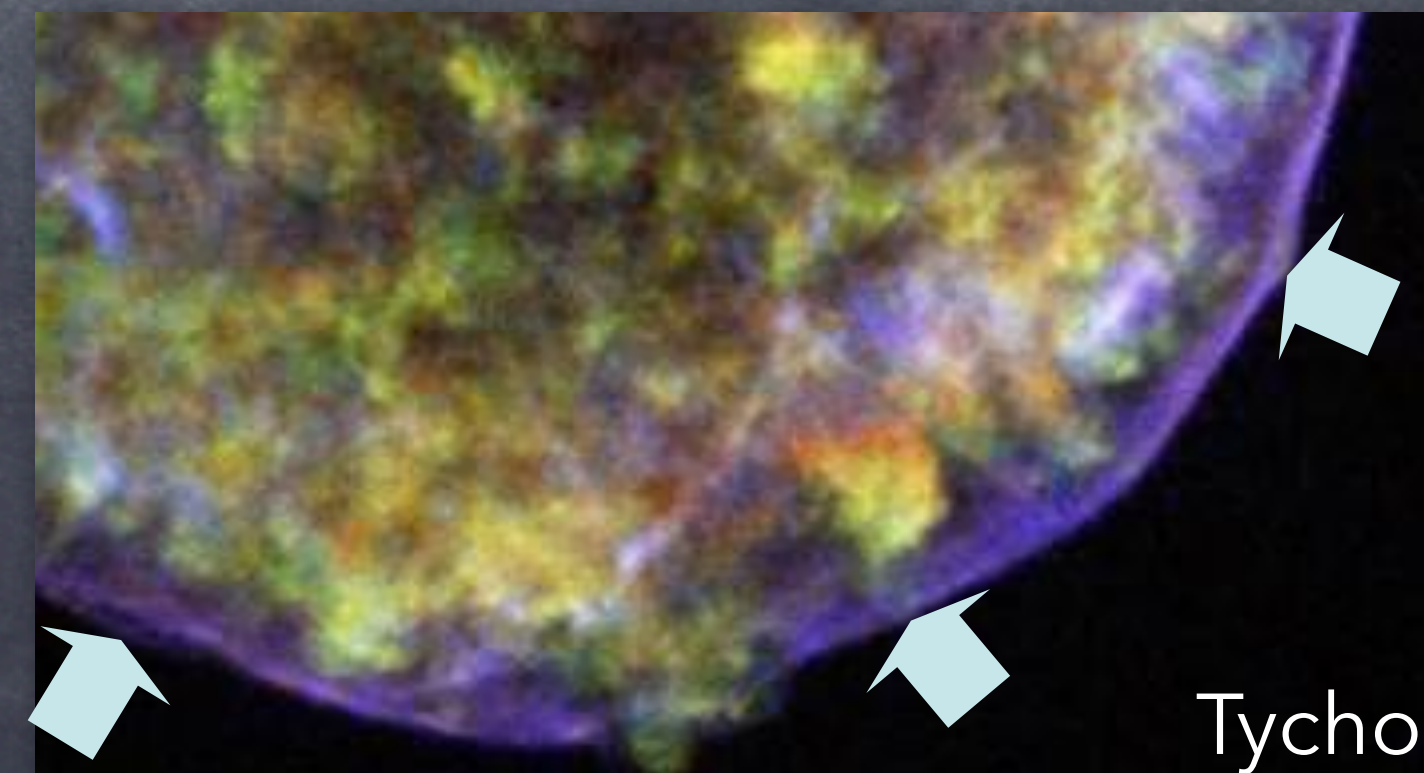
• **Mechanism:** Fermi acceleration at SNR shocks is *first-order* and produces power-laws. **Diffusive Shock Acceleration (DSA)** (Krimskii77, Axford+78, Bell78, Blandford-Ostriker78)



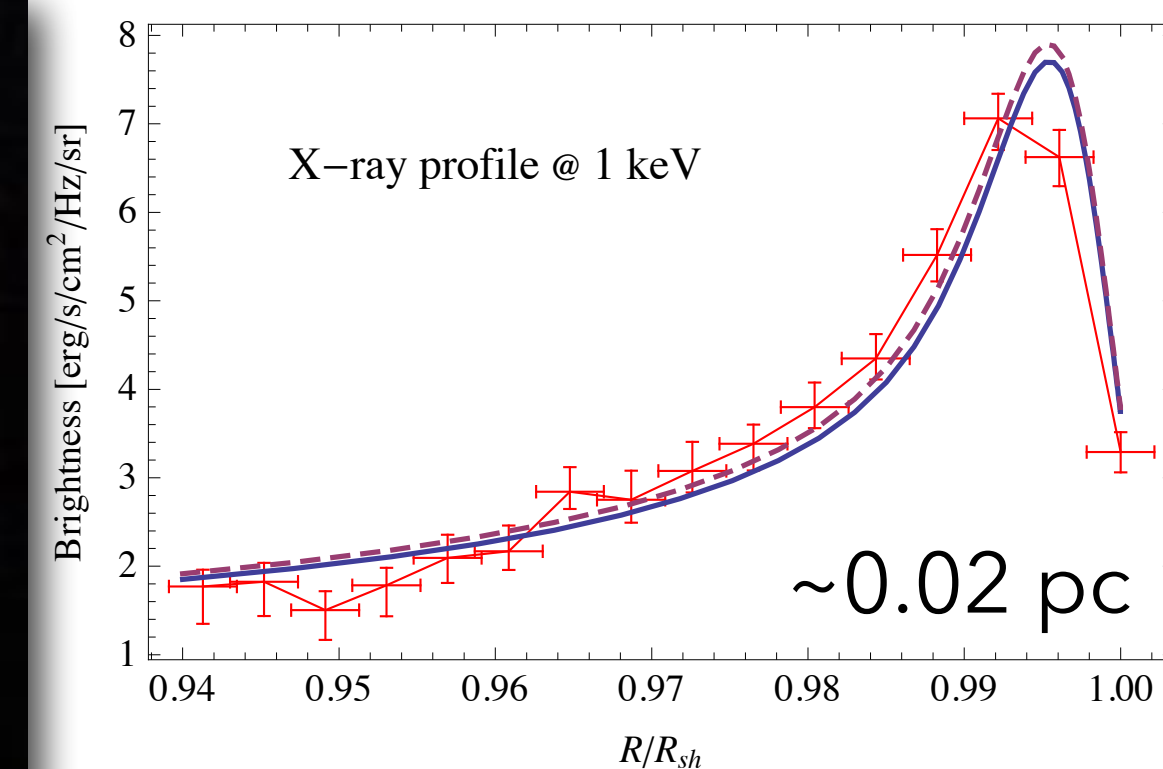
Downstream

Upstream

• Evidence of **B field amplification:** self-generated scattering enhances the energization rate (e.g., Bamba+05, Völk+05, Parizot+06, Morlino+12, Ressler+14, etc)



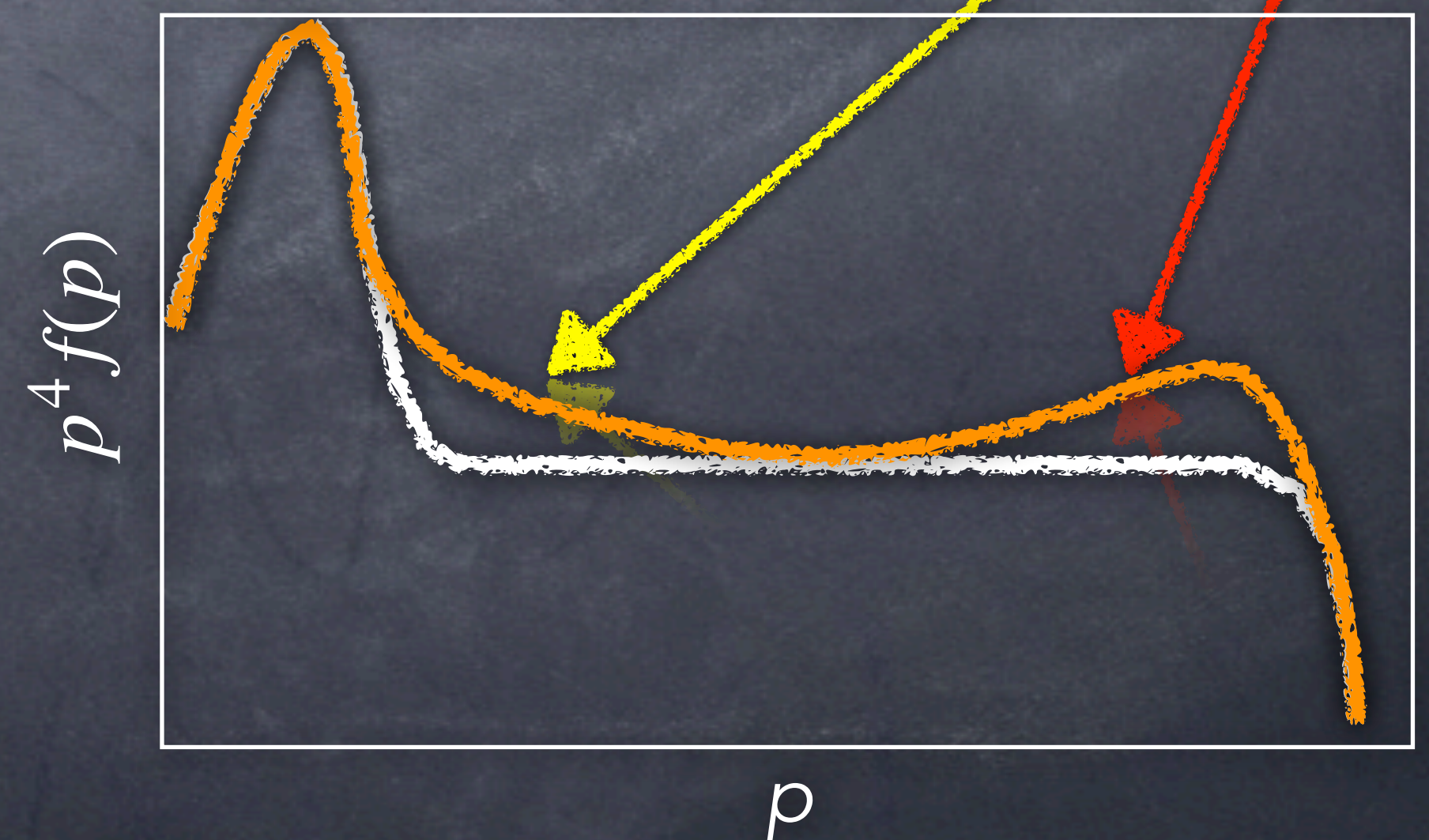
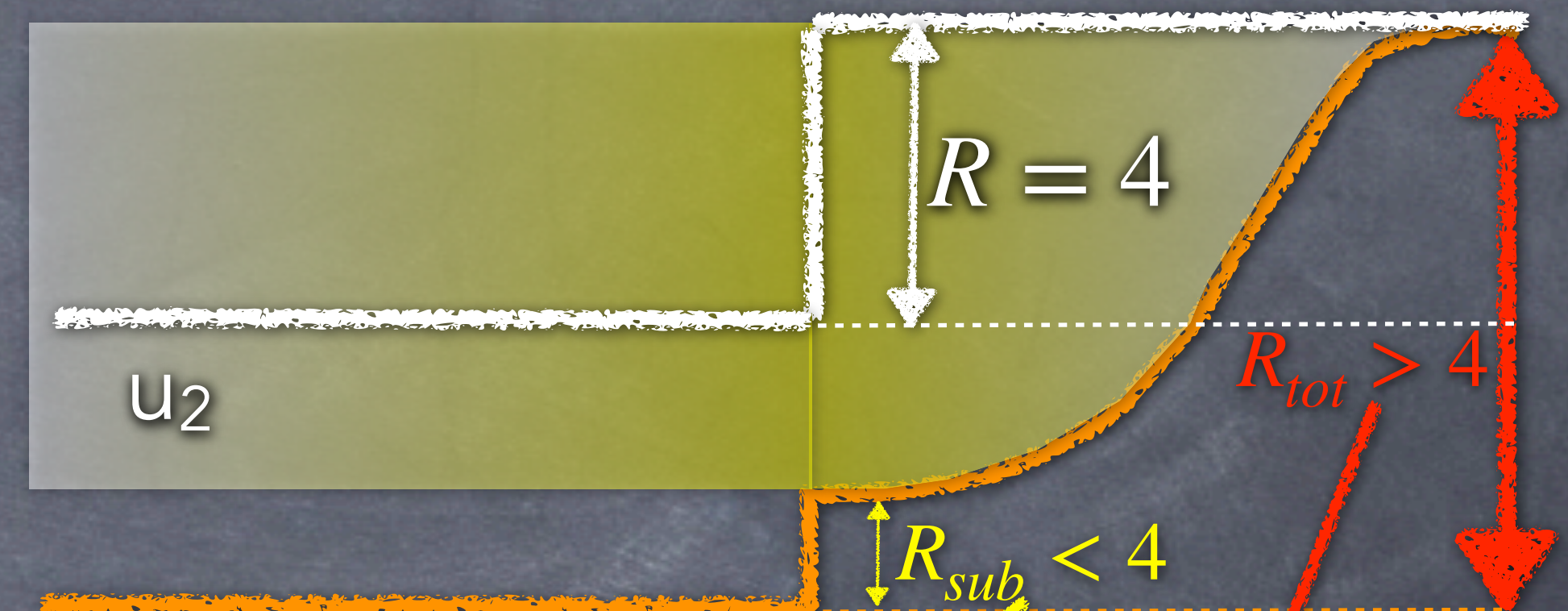
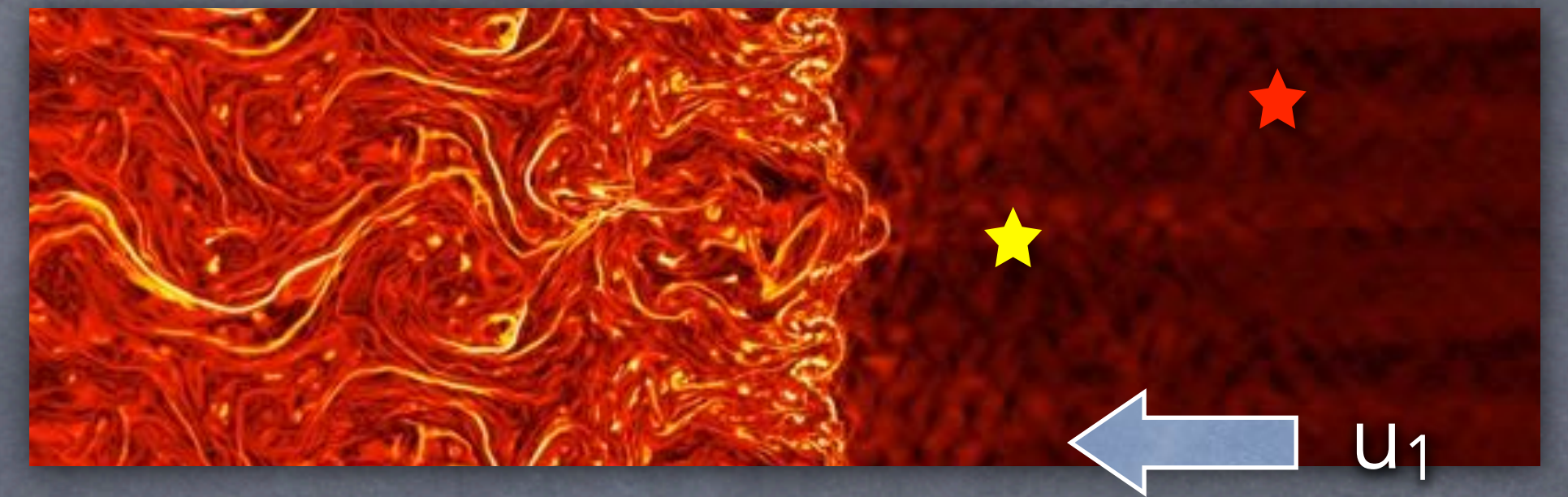
Tycho



# Non-Linear Diffusive Shock Acceleration

- DSA yields *momentum* power laws  $f(p) \propto 4\pi p^2 p^{-q}$
- The **slope**  $q$  depends only on the shock **compression**  

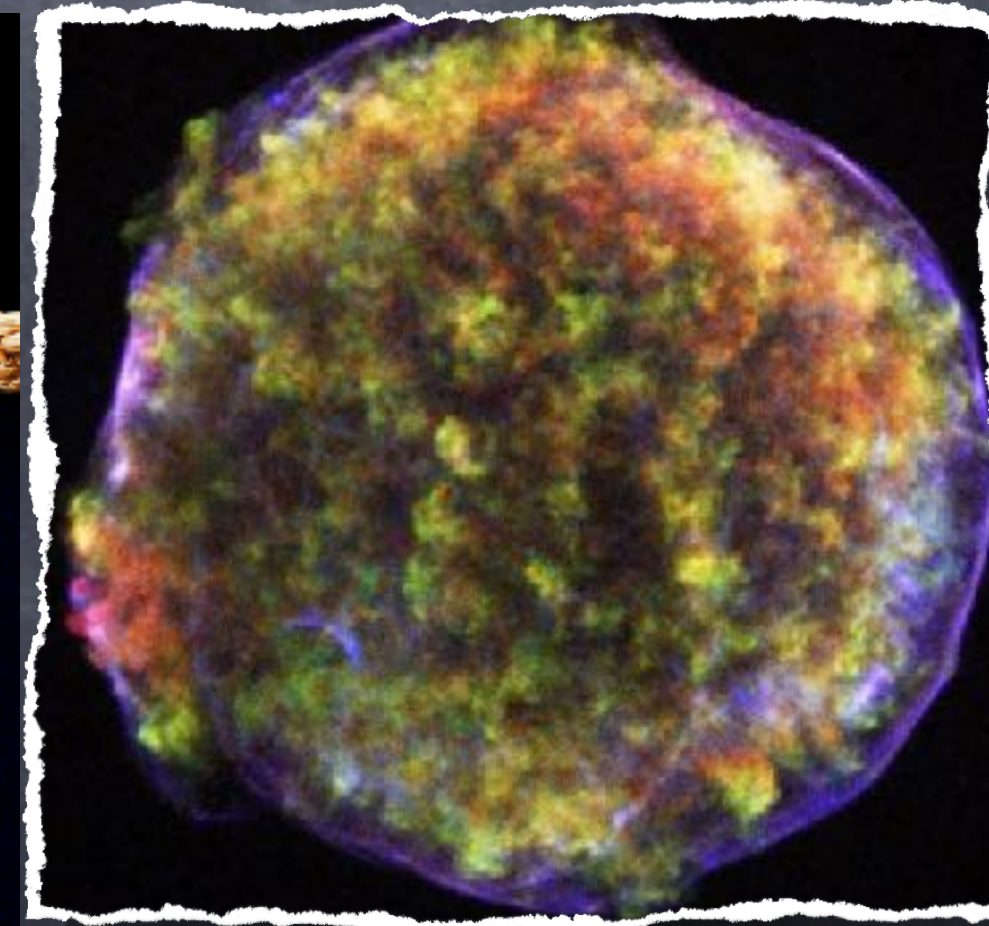
$$q = \frac{3R}{R-1}; \quad R = \frac{\gamma+1}{\gamma-1} \simeq 4; \rightarrow q = 4 \text{ for strong shocks}$$
- The CR pressure makes the **adiabatic index**  $\gamma$  smaller and induces a shock **precursor**
- Particles "feel" different compression ratios: spectra should become **concave**
- If **acceleration is efficient**, high-energy particles feel  $R_{tot} > 4$  and their spectra must be flat, i.e.,  $q < 4$



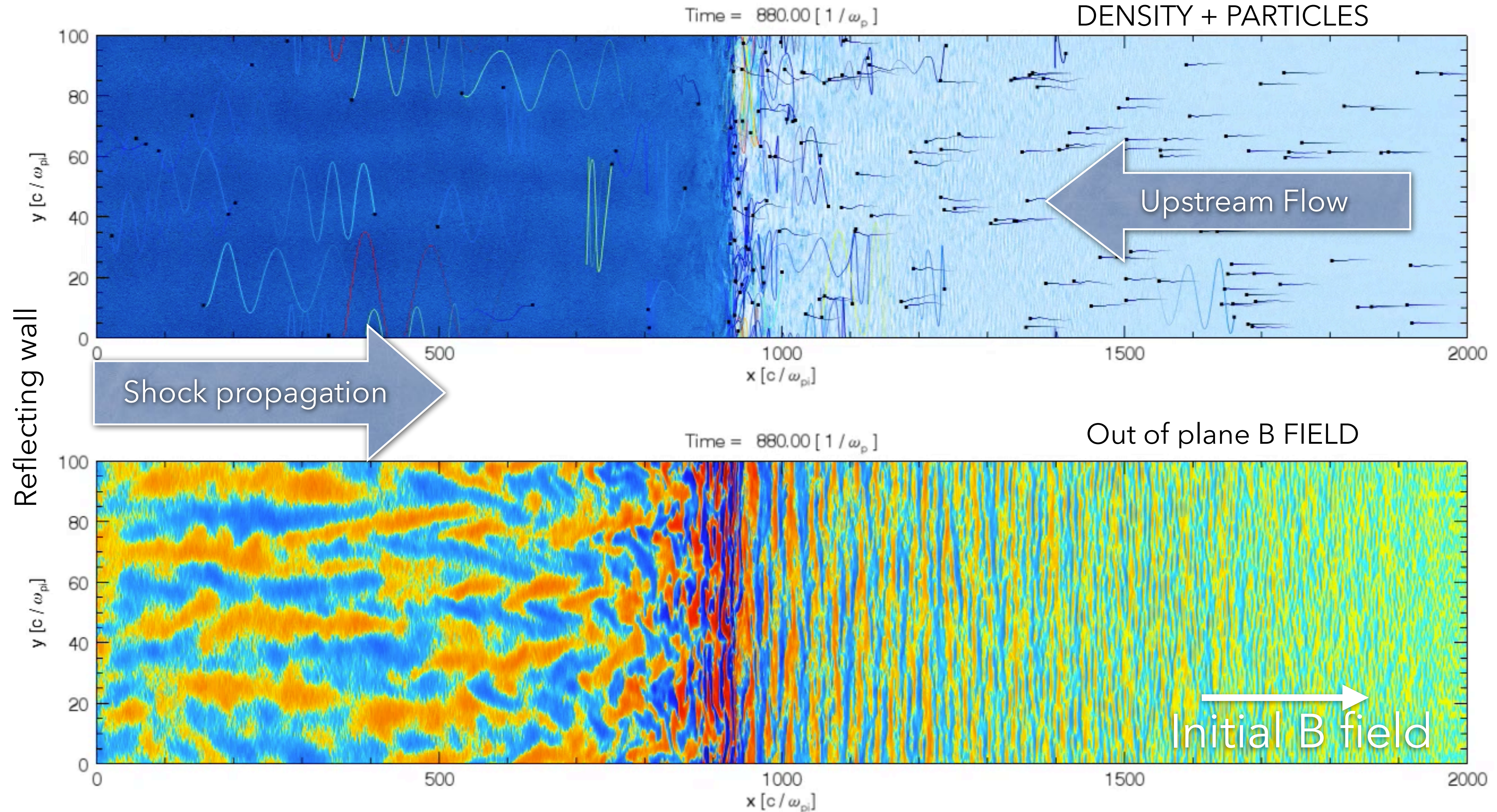
(e.g., Jones-Ellison91, Malkov-Drury01 for reviews)

# Theory vs Observations

- **Efficient DSA** should return:
  - Compression ratios  $R > 4$ ;
  - CR spectra flatter than  $p^{-4}$  (flatter than  $E^{-2}$  for relativistic particles)
- **Observations**, instead, point to significantly steeper spectra:
  - Hadronic  $\gamma$ -rays from historical and middle-age SNRs:  $q \sim 4.3 - 4.7$  (e.g., Caprioli11,12; Aharonian+19);
  - Synchrotron emission from radio SNe:  $q \sim 5$  (e.g., Chevalier-Fransson06, Bell+11);
  - Propagation of Galactic CRs suggests source spectra with  $q \sim 4.3 - 4.4$  (e.g., Blasi-Amato11a,b; Evoli+19).

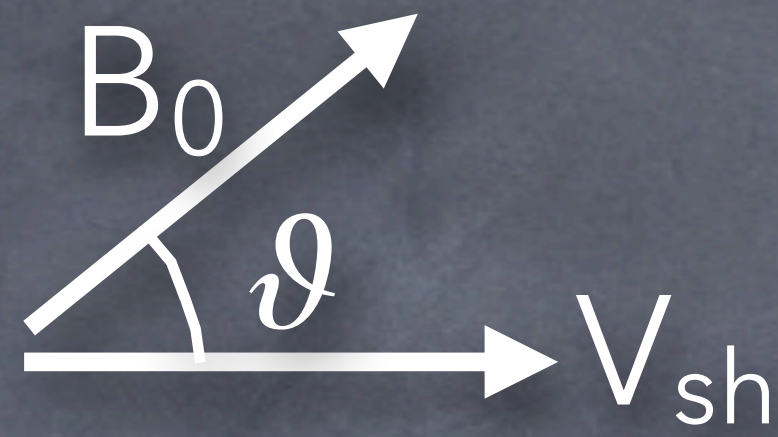


# Hybrid Simulations of Collisionless Shocks

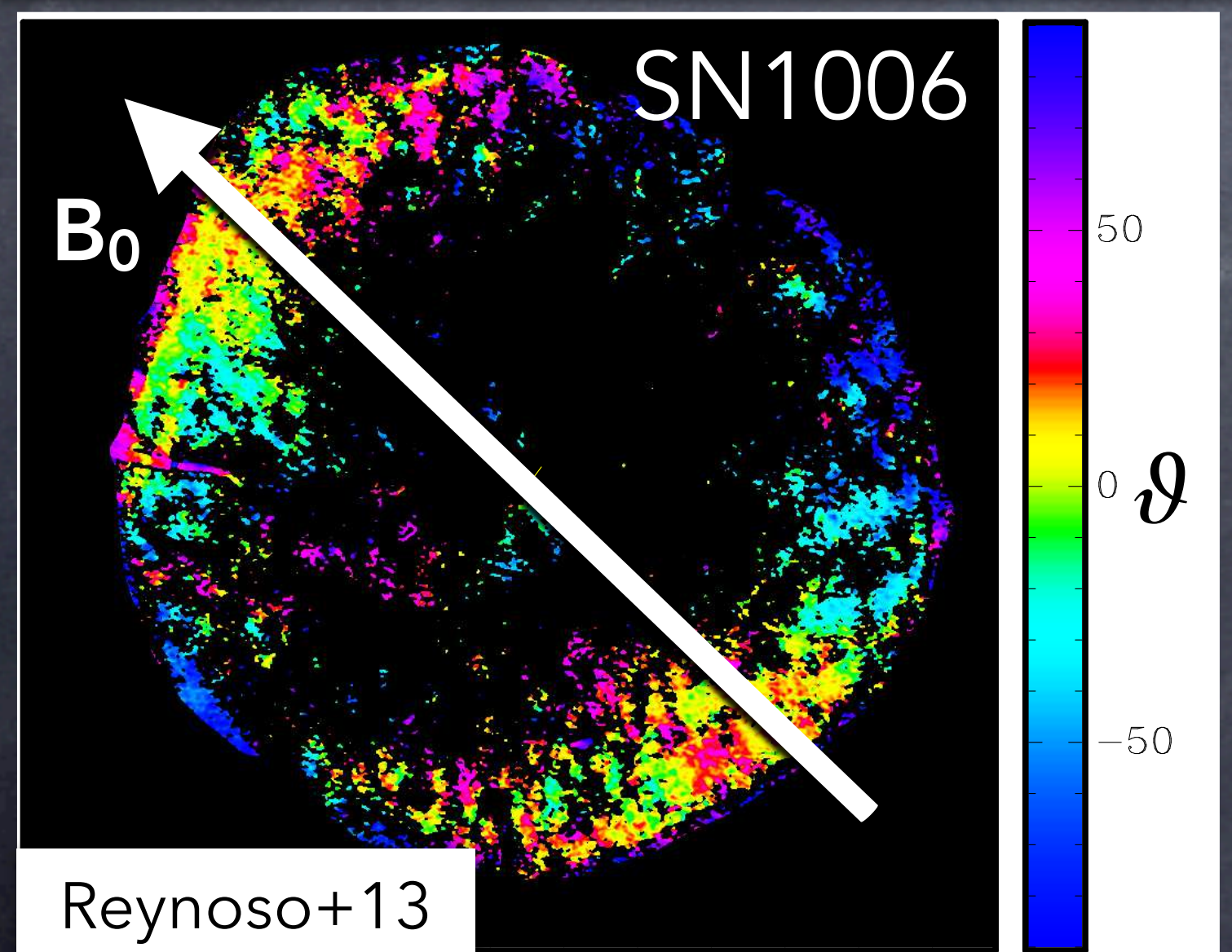
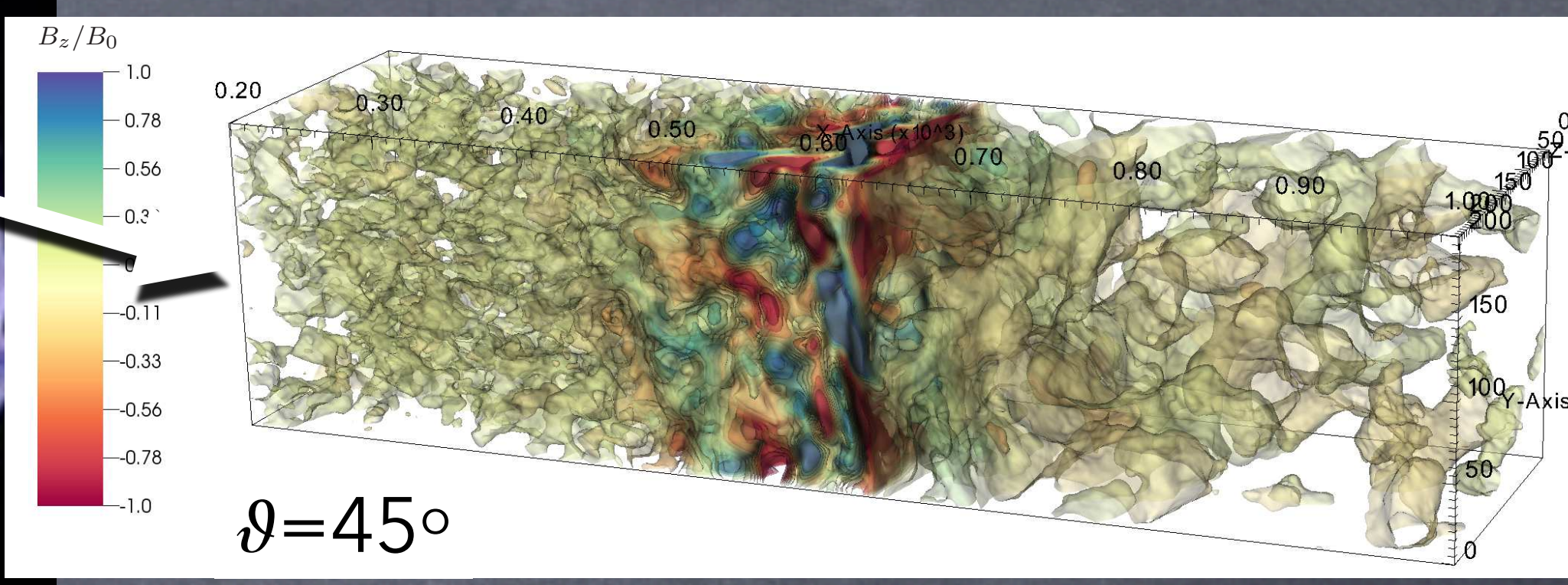
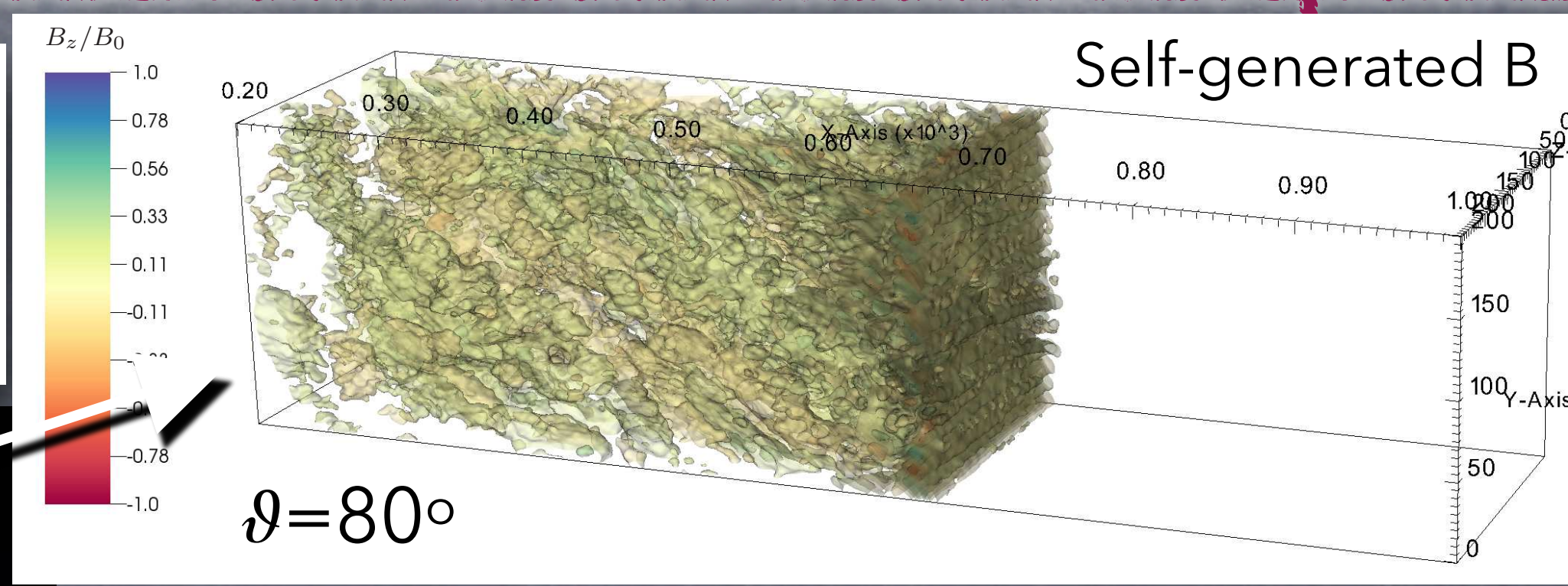
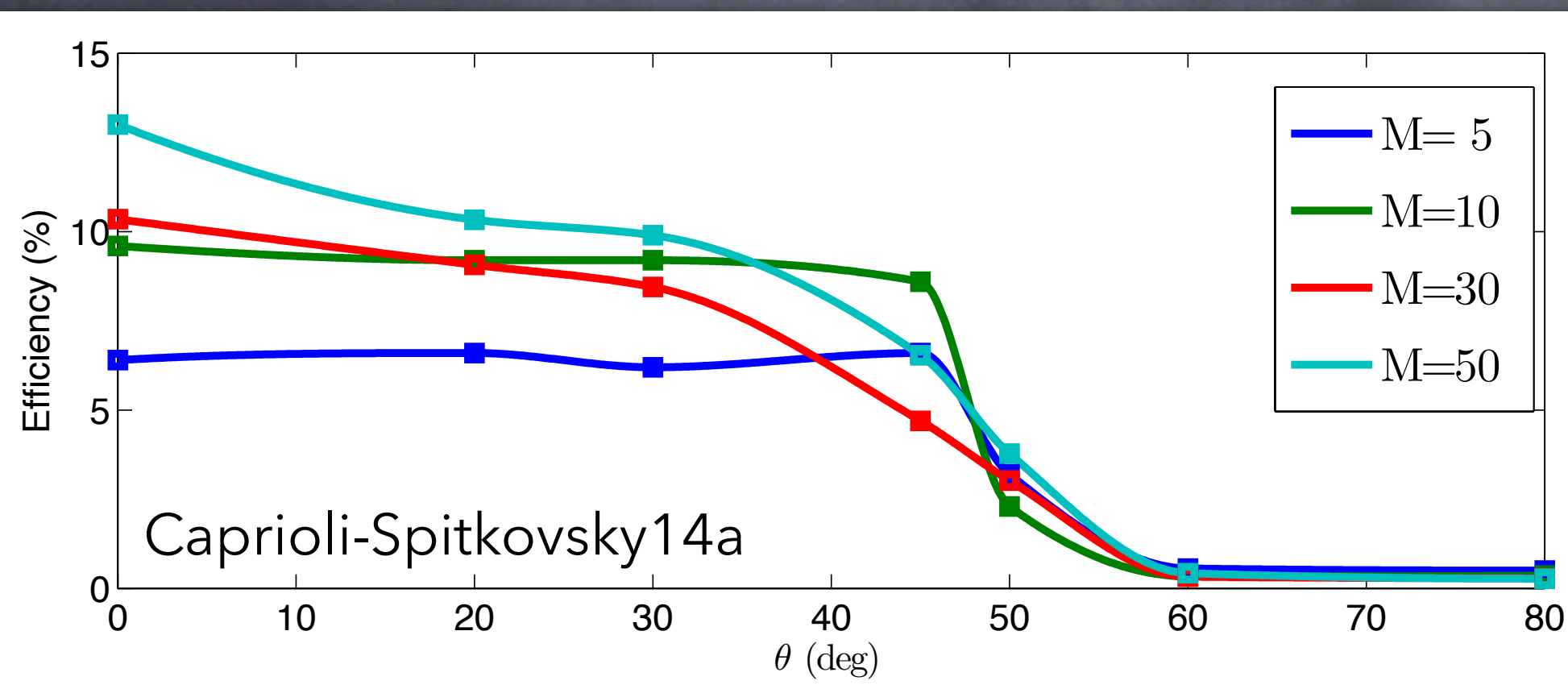


# DSA Efficiency

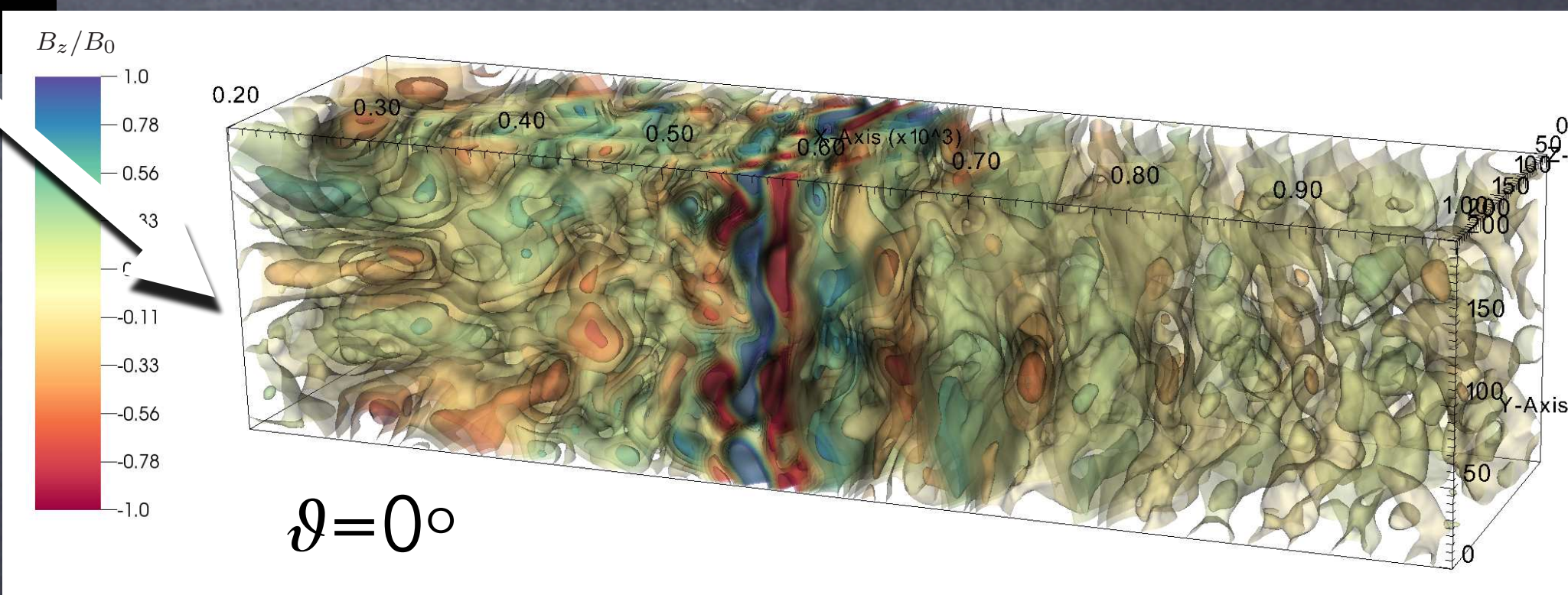
Acceleration depends on the shock **inclination**



X-ray emission:  
red=thermal  
white=synchrotron



B amplification and ion acceleration where the shock is **parallel**



Caprioli-Spitkovsky14a,b,c

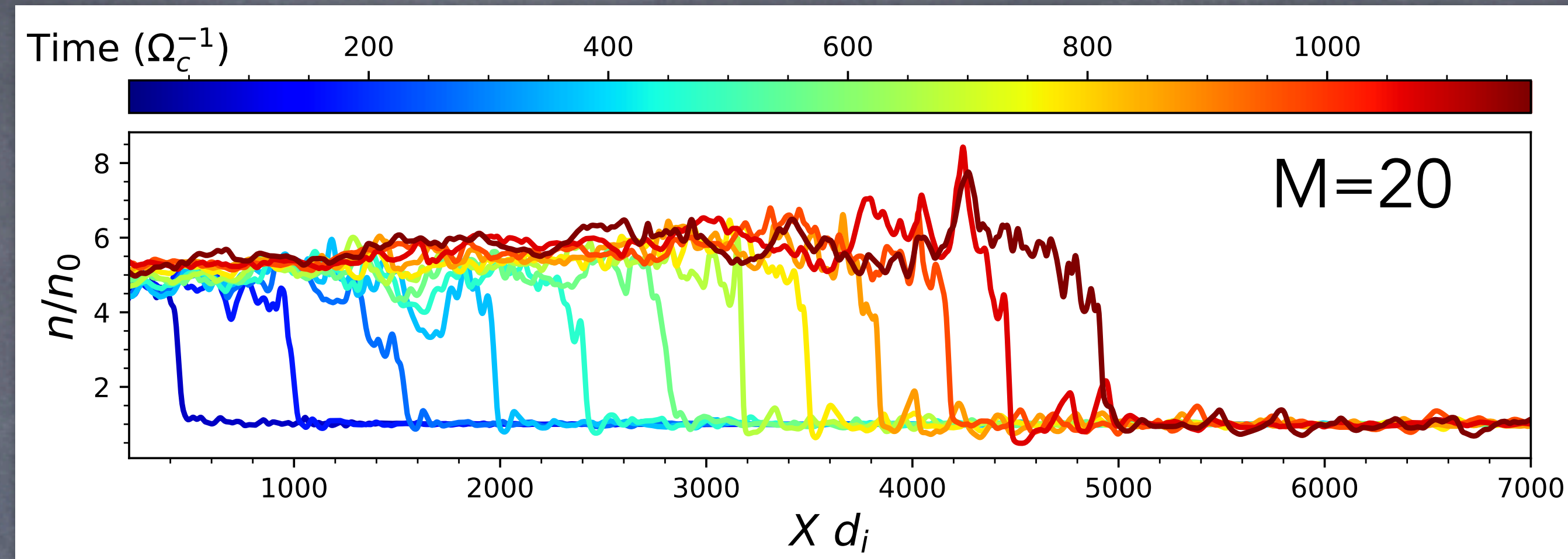
# CR-modified Shocks: Enhanced compression!

- Hybrid simulations (Haggerty-Caprioli20)

- Efficiency  $\lesssim 15\%$  at parallel shocks

- Formation of upstream precursor

- $R$  increases with time, up to  $\sim 6$



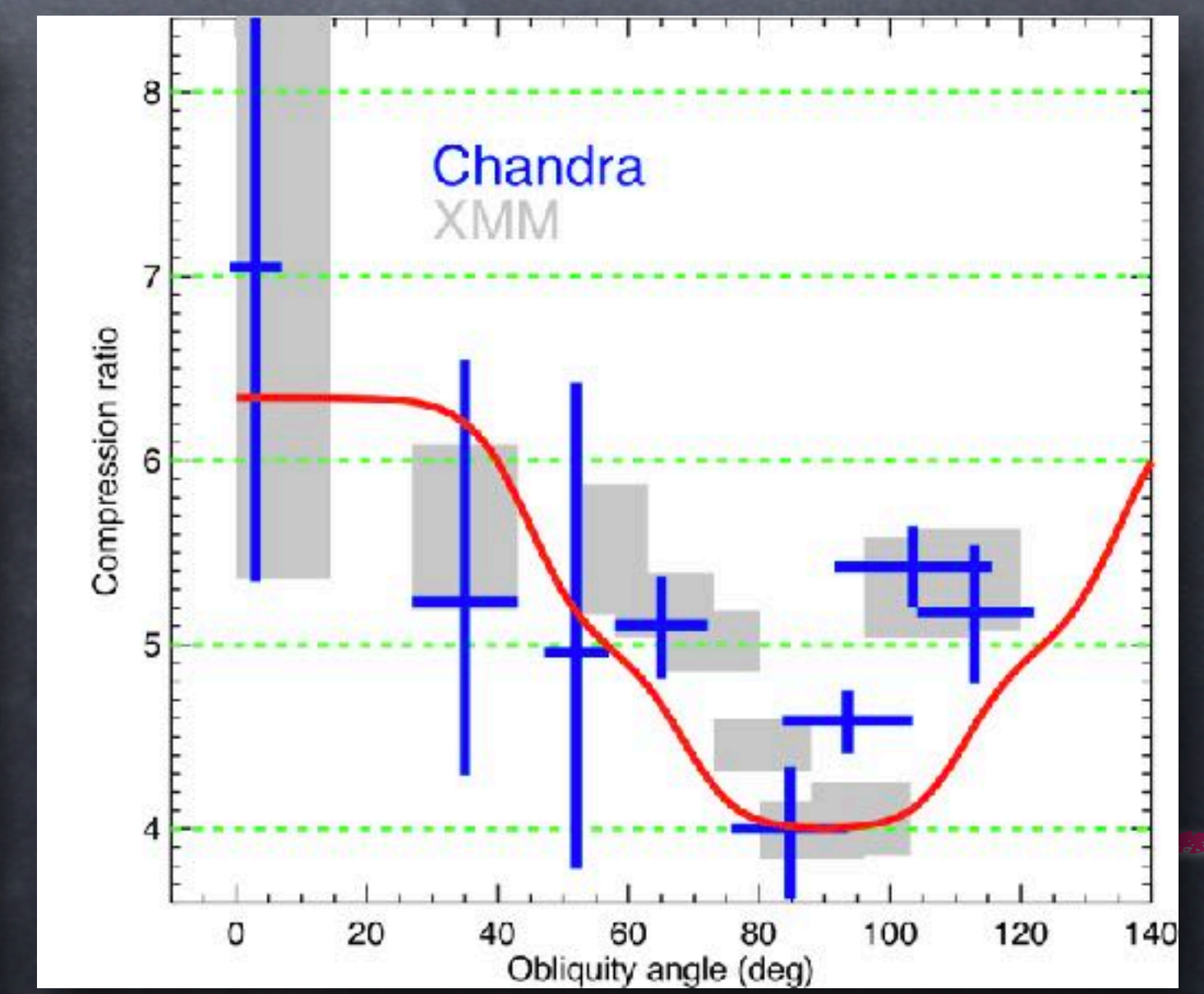
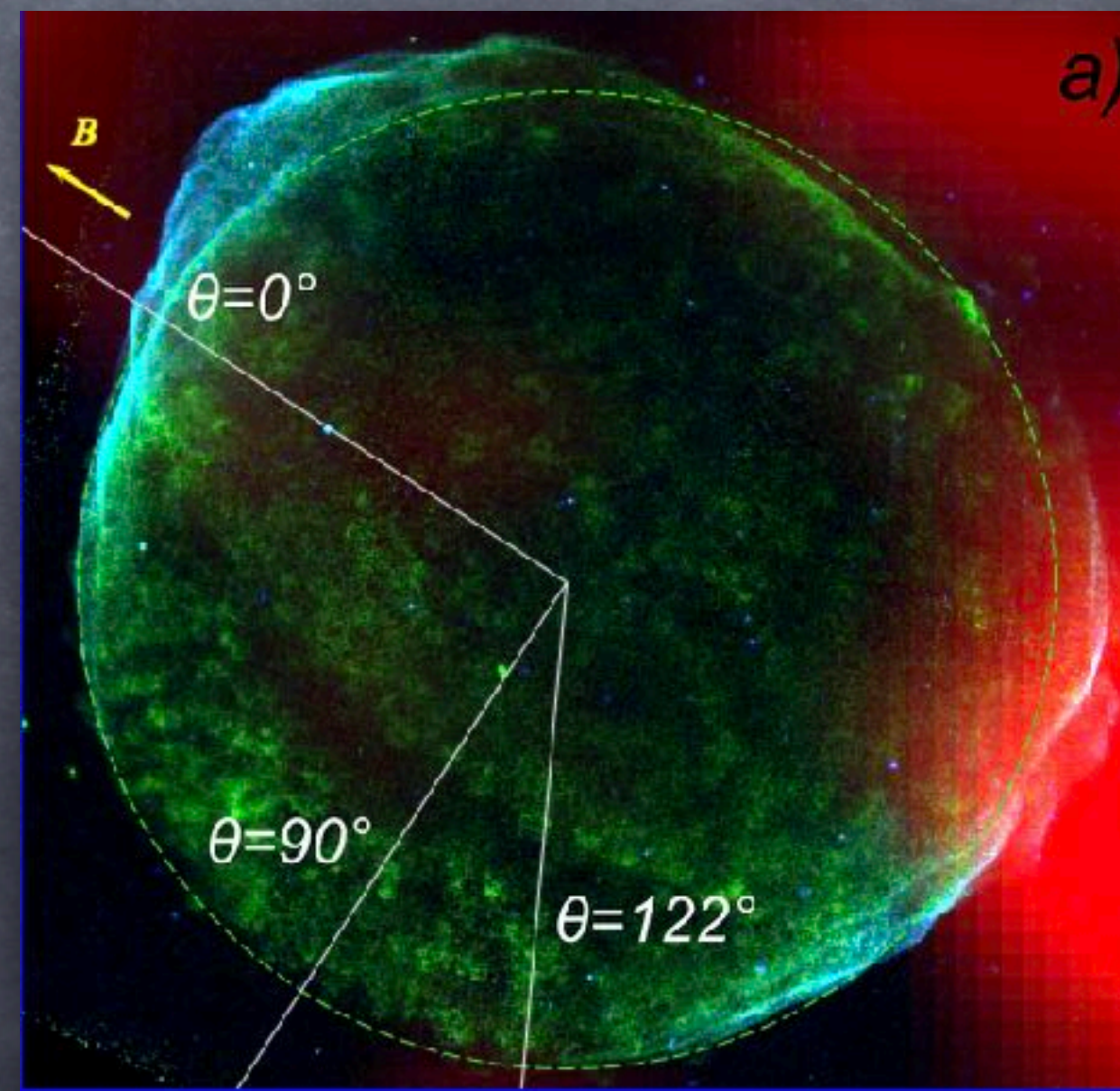
- $R \sim 6 - 7$  inferred in **Tycho** (Warren+05). In **SN1006**:  $R \sim 4 - 7$ , modulated with the azimuth/shock inclination (Giuffrida, Miceli, Caprioli+21, submitted to NatComm.)

- If  $R \simeq 7 \rightarrow q_{\text{expected}} \simeq 3.5$

- Tycho: radio to  $\gamma$ -ray observations:

$$q_{\text{inferred}} \simeq 4.3$$

A challenge to DSA theory!

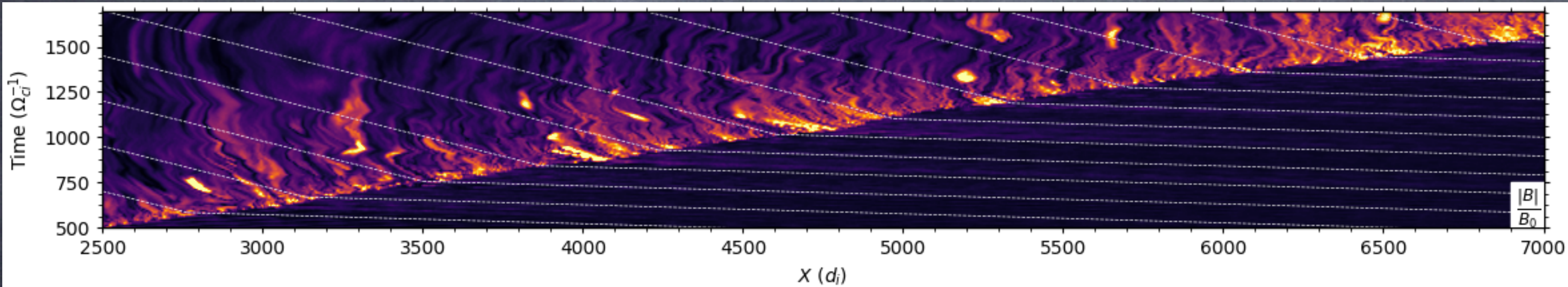
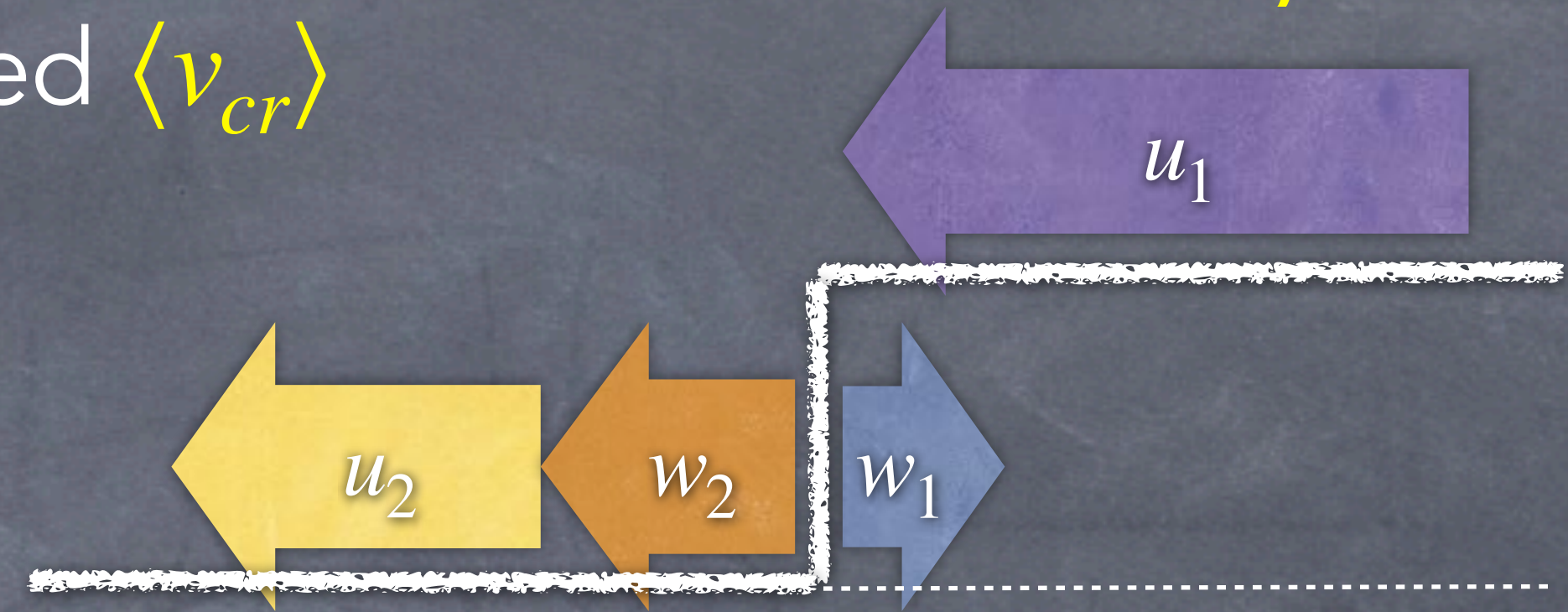


# The Role of Amplified Magnetic Fields

- CRs feel an **effective** compression  $R_{cr} = \frac{u_1 + w_1}{u_2 + w_2}$ ;  $w = \text{wave speed} \approx v_A = \frac{B}{4\pi\rho}$
- We can measure both  $w$  and the effective CR speed  $\langle v_{cr} \rangle$

- Upstream:**  $w_1 \simeq -v_{A,1}(\delta B_1) \ll u_1$

- Downstream:**  $\langle v_{cr} \rangle \simeq w_2 \simeq +v_{A,2}(\delta B_2) \equiv \alpha u_2$



Haggerty-Caprioli20

- B fields (and hence CRs) **drift** downstream with respect to the thermal gas

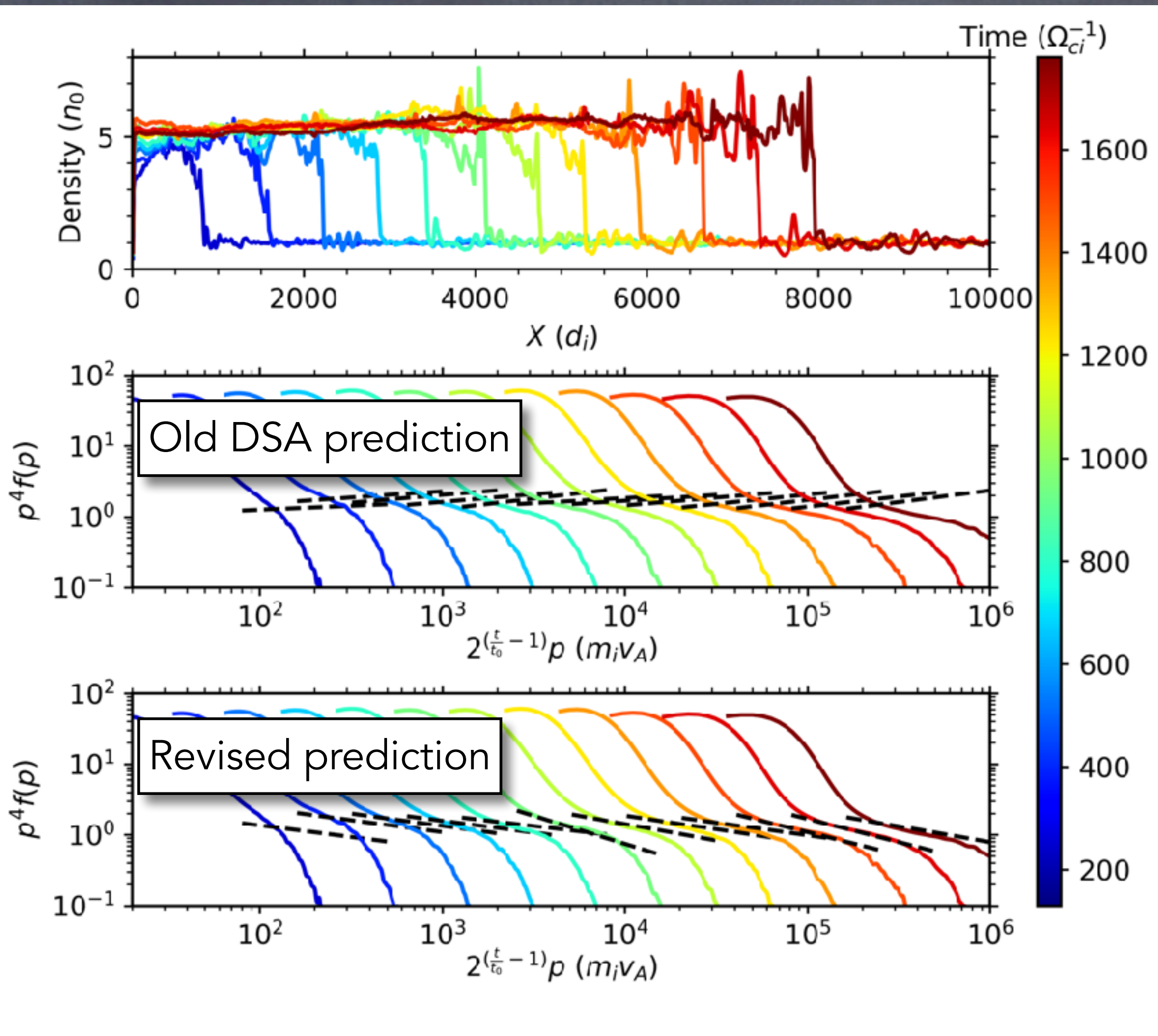
- First evidence of the formation of a **postcursor**

$$R_{cr} \simeq \frac{u_1}{u_2(1 + \alpha)} < R_{gas}$$

- CRs *feel* a compression ratio *smaller* than the gas



# A Revised Theory of Diffusive Shock Acceleration



- With the **effective** compression felt by CRs

$$q = \frac{3R_{cr}}{R_{cr} - 1} = \frac{3R_{gas}}{R_{gas} - 1 - \alpha} > q_{DSA}$$

- CRs feel  $R_{cr} < R_{gas}$ : the power-law index is *not universal, but depends on B field*
- Ab-initio* explanation for the **steep spectra observed** in SNRs, radio SNe, CRs...
- Also see **Highlight Talk** by R. Diesing (ID:488)